

Quantum electrodynamical formulation of photochemical acid generation and its implications on optical lithography

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Abstract

The photochemical acid generation is refined from the first principles of quantum electrodynamics. First, we briefly review the formulation of the quantum theory of light based on the quantum electrodynamics framework to establish the probability of acid generation at a given spacetime point. The quantum mechanical acid generation is then combined with the deprotection mechanism to obtain a probabilistic description of the deprotection density directly related to feature formation in a photoresist. A statistical analysis of the random deprotection density is presented to reveal the leading characteristics of stochastic feature formation.

KEYWORDS

extreme ultraviolet lithography, optical lithography, quantum electrodynamics, quantum optics

1 | INTRODUCTION

The physics of optical lithography has steadily entered the quantum regime owing to the constant demand to reduce the physical length scale of the patterning process. In particular, the classical-to-quantum transition has been accelerated by introducing an extreme ultraviolet (EUV) exposure system with a typical wavelength of approximately 10^{-8} m.

Among other things, the quantum effect in EUV lithography has been most faithfully represented by shot noise arising from the quantum fluctuation of the incident light intensity. Such quantum fluctuation has been statistically averaged out for an exposure system having a high photon density of states (i.e., dose per energy of each photon). However, for EUV exposure, no drastic increase in the exposure dose compared to the increment in

individual photon energy gives rise to severe quantum fluctuations in light intensity.

It has been widely accepted that the fluctuations can be depicted by the randomness of the number of photons following a Poisson distribution under a given dose [1]. Nevertheless, the fully quantum mechanical exposition of shot noise in the context of optical lithography has barely been studied.

This paper provides a firm physical ground for quantum mechanical shot noise in optical lithography by employing quantum electrodynamics (QED) [2]. More precisely, we reformulate the photochemical process for acid generation in the language of QED by identifying the photochemical process with the photoelectric detection of light.

The QED formulation of acid generation merely demonstrates the well-established proportionality

between classical light intensity and photoelectric detection probability [3]. However, the exceptional merit of introducing QED to optical lithography is the capability to integrate the physical descriptions of the primary and secondary photochemical processes, such as flares and secondary electrons, into a single framework, although such secondary effects are not discussed in this work.

With probabilistic acid generation, we proceed to the stochastic deprotection mechanism of the photoresist by defining deprotection density as a random field on the spacetime points of localized acid generation. The random deprotection density then allows us to compute the probability of pixel formation at each spatial location in the resist, which leads to the probability of a feature forming in a given region.

The probabilistic feature formation in our work is closely related to the former works in [4, 5]. However, our work elaborates on discussions in those works with detailed quantum mechanical acid generation and rather refined statistical analyses.

The remainder of this paper is organized as follows. In the following section, we provide a QED formulation for photochemical acid generation, including a brief review of the construction of the QED and a revision of the photoelectric detection of light. In Section 3, we present a statistical analysis of the randomness of feature formation in a resist arising from the probabilistic nature of acid generation. Section 4 is devoted to the conclusions and outlook of the current work.

2 | QUANTUM MECHANICAL FORMULATION OF ACID GENERATION

In optical lithography, a feature on a photoresist is formed by developing deprotected polymers in the photoresist using a resist developer. Deprotected polymers are generated through a deprotection mechanism carried out by the chemical reaction between protected polymers and acids, in which the latter are produced by the photochemical process of photoacid generators (PAGs).

At the molecular level, acid generation occurs when the confined electrons of PAGs are released through interactions with the exposure light. Accordingly, the rate of acid generation can be identified with that of photoelectric detection of light, which is a well-known application of the quantum theory of light. The following subsections provide a quantum mechanical description of acid generation by reformulating the photoelectric detection of light in QED.

2.1 | Quantum theory of light: A brief review

The quantum theory of light and its interaction with charged particles has been most successfully formulated in the quantum field theory (QFT) framework, ensuring the manifest spacetime Lorentz symmetry and the unitarity of quantum mechanics. In this subsection, we briefly review the formulation of the QFT for light and charged particles, called QEDs, following the notations and conventions of [6].¹

In the QFT framework, the elementary quantum state relevant to light is an excited quantum state over the ground state $|0\rangle$, called the photon. Photons can be created and annihilated by the set of creation and annihilation operators $\{a(p, \sigma), a^\dagger(p, \sigma)\}$, where $p = (p^0, p^1, p^2, p^3)$ and $\sigma = \pm 1$ denote the four-vector momentum and intrinsic spin of the photon, respectively.

The four-vector momentum p satisfies the massless condition

$$0 = (p^1)^2 + (p^2)^2 + (p^3)^2 - (p^0)^2, \quad (1)$$

together with $p^0 \geq 0$, where p^0 is the photon energy. The creation–annihilation pair satisfies the following commutation relation:

$$[a(\mathbf{p}, \sigma), a^\dagger(\mathbf{p}', \sigma')] = \delta_{\sigma\sigma'} \delta(\mathbf{p} - \mathbf{p}') \quad (2)$$

for $\mathbf{p} = (p^1, p^2, p^3)$ and $\mathbf{p}' = (p'^1, p'^2, p'^3)$.

The creation–annihilation pair forms the quantum field $A^\mu(x)$ ($\mu = 0, 1, 2, 3$) via

$$A^\mu(x) = A_{(+)}^\mu(x) + A_{(-)}^\mu(x), \quad (3)$$

where

$$A_{(+)}^\mu(x) = (2\pi)^{-3/2} \sum_{\sigma=\pm 1} \int \frac{d^3p}{\sqrt{2p^0}} e^{i\mu}(\mathbf{p}, \sigma) a(\mathbf{p}, \sigma) e^{ipx}, \quad (4a)$$

$$A_{(-)}^\mu(x) = (2\pi)^{-3/2} \sum_{\sigma=\pm 1} \int \frac{d^3p}{\sqrt{2p^0}} e^{\mu*}(\mathbf{p}, \sigma) a^\dagger(\mathbf{p}, \sigma) e^{-ipx}, \quad (4b)$$

with the polarization vector e^μ and its complex conjugate $e^{\mu*}$.

¹In particular, Planck's constant \hbar and the speed of light c are taken to be unity. We also use the Einstein summation convention for repeated indices.

The massless condition in (1) is translated into the equations of motion for A^μ as follows:

$$\square A^\mu = 0, \quad (5)$$

which is a homogeneous wave equation. Also, the Lorentz symmetry implies the dynamics of A^μ to be invariant under the gauge transformation given by

$$A^\mu(x) \mapsto A^\mu(x) + \partial^\mu \Omega(x), \quad \partial^\mu = \frac{\partial}{\partial x_\mu}. \quad (6)$$

To construct the dynamics of A^μ consistent with the gauge symmetry, we introduce the field strength

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu \quad (7)$$

showing the linear relation between the field strength F and A .² The most general form of the action is given by

$$S = \int d^4x \mathcal{L}, \quad \mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + J_\mu A^\mu + \mathcal{L}_{\text{matter}}, \quad (8)$$

where $J_\mu = J_\mu(\psi)$ is the current written in some charged matter fields ψ and $\mathcal{L}_{\text{matter}}$ is the Lagrangian for the charged particles represented by ψ .

The dynamical system of A_μ represented by (8) is a constrained system owing to the gauge symmetry in (6). Consequently, only A_m ($m = 1, 2, 3$) are dynamical, and we have to choose an appropriate gauge to exhaust gauge freedom. Here, we choose the Coulomb gauge

$$\partial_m A^m = 0, \quad m = 1, 2, 3. \quad (9)$$

Altogether, the Hamiltonian of the system is obtained as follows:

$$H = \int d^3x \left(\frac{1}{2} E^m E_m + \frac{1}{2} B^m B_m + J^m A_m \right) + H_{\text{matter} \oplus \text{Coul}}, \quad (10)$$

where

$$F^{0m} = E^m, \quad F^{mn} = \epsilon^{mnp} B_p, \quad m, n, p = 1, 2, 3 \quad (11)$$

and

$$H_{\text{matter} \oplus \text{Coul}} = H_{\text{matter}} - \frac{1}{2} \int d^3x d^3y \frac{J^0(x) J^0(y)}{4\pi |\mathbf{x} - \mathbf{y}|}. \quad (12)$$

Having the Hamiltonian H in (10) for light and charged matter, one can compute the evolution of a quantum state given at the initial time. A detailed discussion of the quantum evolution of a physical system can be found in the standard literature, such as [7].

2.2 | Photoelectric detection probability

As indicated at the beginning of this section, acid generation can be identified by the photoelectric detection of light. In this process, the exposure system can be represented by the Hilbert space \mathcal{H} , which is the product space $\mathcal{H}_\gamma \otimes \mathcal{H}_\psi$ of the space of photons \mathcal{H}_γ and charged particles \mathcal{H}_ψ . At the initial time t_0 , two systems are completely disentangled [8], so that the initial state $|\Psi(t_0)\rangle \in \mathcal{H}$ is given by

$$|\Psi(t_0)\rangle = |\chi\rangle \otimes |\psi\rangle, \quad |\chi\rangle \in \mathcal{H}_\gamma \text{ and } |\psi\rangle \in \mathcal{H}_\psi. \quad (13)$$

For the detection of light, we are only interested in the occurrence of an interaction between light and charged matter at a given time $t > t_0$. Accordingly, we do not need to specify the states in \mathcal{H}_ψ at t_0 and t if they satisfy the following conditions:

$$|\psi\rangle \perp |\bar{\psi}\rangle \Leftrightarrow \langle \bar{\psi} | \psi \rangle = 0, \quad |\psi\rangle, |\bar{\psi}\rangle \in \mathcal{H}_\psi. \quad (14)$$

where $|\bar{\psi}\rangle$ denotes the state of charged matter at time t . Also, we trace \mathcal{H}_γ out at t since the final state of light is not a concern.

Altogether, we have the transition amplitude $T(t, t_0)$ equivalent to the probability of a photochemical interaction as follows:

$$T(t, t_0) = \sum_{\substack{\psi, \bar{\psi} \in \mathcal{H}_\psi \\ \psi \perp \bar{\psi}}} \text{Tr}(|\bar{\psi}\rangle \langle \bar{\psi}| \rho_\psi(t)), \quad (15)$$

where $\rho_\psi(t)$ denotes the density matrix obtained by tracing out \mathcal{H}_γ as

$$\rho_\psi(t) = \text{Tr}_{\mathcal{H}_\gamma} \rho(t), \quad \rho(t) = |\Psi(t)\rangle \langle \Psi(t)|. \quad (16)$$

In perturbative expansion, the first nonvanishing contribution to $T(t, t_0)$ is given by [8]

²The linearity between a given quantum field and its field strength reflects the abelian nature of the gauge transformation in (6). In addition, linearity ensures no self-interaction between photons; therefore, photons can only interact with each other through charged particles.

$$T(t, t_0) \simeq \sum_{\substack{\psi, \bar{\psi} \in \mathcal{H}_\psi \\ \psi \perp \bar{\psi}}} \int_{t_0}^t d^4 x_2 \int_{t_0}^{t_2} d^4 x_1 T^{(2)}(\psi, \bar{\psi}, J, A; x_1, x_2) + c.c., \quad (17)$$

where $c.c.$ denotes the complex conjugate of the previous term and

$$T^{(2)}(\psi, \bar{\psi}, J, A; x_1, x_2) = \langle \bar{\psi} | J_m(x_1) | \psi \rangle \langle \psi | J_n(x_2) | \bar{\psi} \rangle \times \langle \chi | A^m(x_1) A^n(x_2) | \chi \rangle. \quad (18)$$

To simplify the transition amplitude in (17), we impose the following assumptions arising from a typical exposure process:

1. The wave vector \mathbf{k} and wave frequency ω of light sharply peak around \mathbf{k}_0 and ω_0 (i.e., quasi-monochromatic) so that the investigated physical scale of the spacetime satisfies

$$|\Delta \mathbf{x}| \ll \left| \frac{1}{\Delta \mathbf{k}_0} \right|, \quad |\Delta t| \ll \left| \frac{1}{\Delta \omega_0} \right|, \quad (19)$$

where $\Delta \mathbf{k}_0 = \mathbf{k} - \mathbf{k}_0$ and $\Delta \omega_0 = \omega - \omega_0$. The first condition in (19) reflects our interest in the spatially localized detection of light achieved by restricting the spatial integration domain in (17). Therefore, unless otherwise specified, the spatial integration domain in (17) in the below is taken to be small enough to satisfy the condition in (19).

2. The charged medium (i.e., the photoresist) is isotropic on the orthogonal plane of \mathbf{k}_0 . For notational simplicity, we assume \mathbf{k}_0 to be along the z -direction so that xy -plane is the orthogonal plane of \mathbf{k}_0 .

Condition 1 implies that the correlation of light in (17) is [8]

$$\langle \chi | A_m(x_1) A_n(x_2) | \chi \rangle \approx \langle \chi | A_m^{(-)}(x_0) A_n^{(+)}(x_0) | \chi \rangle \times 2 \cos\left(k_0^\mu(x_1 - x_2)_\mu\right), \quad (20)$$

where $k_0^\mu = (\omega_0, \mathbf{k}_0)$ for a spacetime point $x_0 = (\mathbf{x}_0, t_0)$ in the integration domain of (17). In turn, (17) can be expressed as follows:

$$T(t, t_0) = \langle \chi | A_{(-)}^m(x_0) A_{(+)}^n(x_0) | \chi \rangle \kappa_{mn} \quad (21)$$

where

$$\kappa_{mn} = 2 \sum_{\substack{\psi, \bar{\psi} \in \mathcal{H}_\psi \\ \psi \perp \bar{\psi}}} \int_{t_0}^t d^4 x_1 \int_{t_0}^t d^4 x_2 \langle \bar{\psi} | J_m(x_1) | \psi \rangle \times \langle \psi | J_n(x_2) | \bar{\psi} \rangle \cos\left(k_0^\mu(x_1 - x_2)_\mu\right). \quad (22)$$

Since κ_{mn} is symmetric in its indices, the isotropy of the charged medium, together with the Coulomb gauge condition and condition 1, indicates that

$$\kappa_{mn} = \delta_{mn} \eta, \quad \eta = \frac{1}{3} \text{Tr}(\kappa_{mn}). \quad (23)$$

Therefore, one finds

$$T(t, t_0) = \eta \langle \chi | A_{(-)}^m(x_0) A_m^{(+)}(x_0) | \chi \rangle. \quad (24)$$

Finally, the optical equivalence theorem [9, 10] implies that $A_{(-)}^m(x_0) A_m^{(+)}(x_0)$ is proportional to the quantum correspondence $I(x_0)$ of the classical light intensity. Absorbing the proportional factor into η , we obtain the previously established photoelectric detection probability [3]

$$p_{x_0} = \eta \langle I(x_0) \rangle. \quad (25)$$

where η denotes the quantum efficiency.

Furthermore, by applying Poisson statistics to p_{x_0} , we can obtain the detection probability for n photons in a spatial region V and time interval Δt as [11]

$$p_{\gamma, E=(V, \Delta t)}(n) = \left\langle \mathcal{T} \frac{W^n e^{-W}}{n!} \right\rangle, \quad (26)$$

where \mathcal{T} denotes the time ordering and

$$W = \int_V d^3 x \int_{\Delta t} dt \eta(\mathbf{x}, t) I(\mathbf{x}, t). \quad (27)$$

corresponding to the total intensity absorbed by $(V, \Delta t)$. The Poisson-like distribution $p_{\gamma, E}(n)$ in (26) is often approximated as

$$p_{\gamma, E}(n) \simeq \frac{\langle W \rangle^n e^{-\langle W \rangle}}{n!}, \quad (28)$$

which reproduces the Poisson distribution of the number of photons in [1].

3 | ANALYSIS OF PROBABILISTIC FEATURE FORMATION

As outlined in the previous section, stochastic acid generation can be integrated with a chemical kinematic model to establish a mechanism for deprotection. In this section, we delve into a simple deprotection mechanism characterized by randomness arising exclusively from the photoelectric probability.

3.1 | Random deprotection density and probabilistic feature formation

Given localized acid generation, the deprotection mechanism can be effectively depicted by a chemical kinetics model, as in [12]. In such a kinetics model, the density of the deprotected polymer at (\mathbf{x}, t) arising from acid-catalyzed deprotection with respect to each localized acid generation at (\mathbf{x}_j, t_j) , $j = 1, 2, \dots, n$ is given by $\rho_D(\mathbf{x}, t; \mathbf{x}_j, t_j)$, so that the total deprotection density $\rho_{D,\text{total}}$ is determined by [4]

$$\rho_{D,\text{total}}(\mathbf{x}, t; \mathbf{x}_j, t_j, n) = \sum_{j=1}^n \rho_D(\mathbf{x}, t; \mathbf{x}_j, t_j). \quad (29)$$

Here, ρ_D denotes the diffusion of acid during the exposure process and subsequent post-exposure baking. The probability of photoelectric detection exclusively governs the stochastic nature of the diffusion. Practically, such diffusion is influenced by various base effects such as photodecomposable quenchers (PDQs) and neutralization, which may introduce additional stochasticity to the deprotection density [13].

The quantum mechanical description of acid generation in the previous section indicates that acid generation at a given spacetime occurs with probability $p_{\mathbf{x},t}$ in (25). Moreover, given a spacetime region E , one can easily find the probability distribution function for local generations of acid at (\mathbf{x}_j, t_j) , $j = 1, 2, \dots, n$ as

$$p_\gamma(\mathbf{x}_j, t_j, n) = p_{\gamma,E}(n) \prod_{k=1}^n \hat{p}_\gamma(\mathbf{x}_k, t_k) \quad (30)$$

with $\hat{p}_\gamma(\mathbf{x}, t) = \frac{p_{\mathbf{x},t}}{W}$ with the relative probability $p_{\mathbf{x},t_j}$ of the acid generation at each (\mathbf{x}_j, t_j) . The total deprotection density $\rho_{D,\text{total}}(\mathbf{x}, t; \mathbf{x}_j, t_j, n)$ can then be regarded as a random field $\rho_{D,\text{total}}(\mathbf{x}, t; \mathbf{X}_j, T_j, N)$ over the spacetime derived from random variables

$$(\mathbf{X}_j, T_j, N) \sim p_\gamma(\mathbf{x}_j, t_j, n), \quad (31)$$

where \sim denotes the corresponding probability density function.

Using the relation between $p_{\mathbf{x},t}$ and the aerial intensity $i_{\text{aerial}}(\mathbf{x}, t) = \langle I(\mathbf{x}, t) \rangle$ in (25), we have the expectation of $\rho_{D,\text{total}}$ as

$$\begin{aligned} E[\rho_{D,\text{total}}(\mathbf{x}, t)] &= (\eta \rho_D \otimes i_{\text{aerial}})(\mathbf{x}, t) \\ &\equiv \int d^4x \eta \rho_D(\mathbf{x}, t; \mathbf{x}', t') i_{\text{aerial}}(\mathbf{x}', t'). \end{aligned} \quad (32)$$

to which $\rho_{D,\text{total}}$ converges for a large absorption W of open dose. The form (32) implies that the expectation of $\rho_{D,\text{total}}$ corresponds to the convolution imaging of i_{aerial} often taken as the nominal intensity i_{resist} of the resist image.

In the patterning process, a pixel on a photoresist is formed if the density of the deprotected polymer exceeds a certain threshold τ at the development process [4, 5]. Thus, the probability of generating a pixel at a given position \mathbf{x} is given by

$$p_{\text{pixel}}(\mathbf{x}) = P[\rho_{D,\text{total}}(\mathbf{x}, t_f) \geq \tau], \quad (33)$$

where $P[\dots]$ denotes the probability of condition $[\dots]$ and t_f is the final time for the exposure process.

Similarly, a feature in the exposed region E corresponds to a three-dimensional object $P \in E$ such that for any $\mathbf{x} \in P$,

$$\rho_{D,\text{total}}(\mathbf{x}, t_f) \geq \tau. \quad (34)$$

In turn, the probability of feature formation in a given region P can be formally written as

$$p_{\text{feature}} = P[\inf_{\mathbf{x} \in P} \rho_{D,\text{total}}(\mathbf{x}, t_f) \geq \tau]. \quad (35)$$

Similarly, we may consider the probability of no feature formation in P :

$$p_{\text{missing}}(P) = 1 - P\left[\sup_{\mathbf{x} \in P} \rho_{D,\text{total}}(\mathbf{x}, t_f) \geq \tau\right], \quad (36)$$

in which $P[\sup_{\mathbf{x} \in P} \rho_{D,\text{total}}(\mathbf{x}, t_f) \geq \tau]$ is often called the excursion probability.

The formal probabilities in (35) and (36) enable us to define the probabilities of various printing failures. For instance, the probability of unexpected patterning (resp. missing) in a given region P corresponds to p_{feature} (resp. p_{missing}) [5]. However, it should be noted that the

computation of the excursion probability for a given random field is somewhat nontrivial, and its analytic formula has been known only for a few exceptional cases [14].

3.2 | Asymptotic analysis of probabilistic feature formation

We now discuss the asymptotic behavior of the probability density $\rho_{D,\text{total}}$ of a deprotected polymer for a large absorption W in (26). A sufficiently large absorption can be achieved by increasing the exposure dose or the area of the exposed area of interest.

For a large W , only a large number N of photoelectric interactions contributes significantly to the probability distribution of $\rho_{D,\text{total}}$. For such a large N , we can apply the central limit theorem so that

$$\rho_{D,\text{total}}(\mathbf{x}, t_f) \sim \mathcal{N}\left(\frac{n}{W}i_{\text{resist}}(\mathbf{x}, t_f), n\sigma_D^2(\mathbf{x}, t_f)\right)p_{\gamma,E}(n), \quad (37)$$

where σ_D^2 denotes the variation in ρ_D given by

$$\sigma_D^2 = E[\rho_D^2(\mathbf{x}, t_f)] - E[\rho_D(\mathbf{x}, t_f)]^2 \quad (38)$$

and $\mathcal{N}(\mu, \sigma^2)$ is a normal distribution with mean μ and variance σ^2 .

By denoting the cumulative distribution function of the normal distribution in (37) as Φ , we can obtain the probability of pixel formation at \mathbf{x} as

$$p_{\text{pixel}}(\mathbf{x}) = \sum_{n=0}^{\infty} (1 - \Phi(\tau; n))p_{\gamma,E}(n). \quad (39)$$

As a simple example illustrating the stochastic analysis, we consider a family of static single-line patterns (i.e., the corresponding light intensity is constant in time) defined by aerial intensities in the form of

$$i_{\text{aerial}}(x) = i_0 \text{sinc}(2\pi x)^2, \quad \text{sinc}(x) = \frac{\sin(x)}{x}, \quad (40)$$

which are classified by the relative intensity i_0 at $x = 0$.

For simplicity, we set the quantum efficiency $\eta = 1$ and employ a normalized Gaussian kernel for the deprotection kernel, that is,

$$\rho_D(x) = \mathcal{N}(x, h^2) \quad (41)$$

in which $h = 1/50$ satisfies our purpose here. Subsequently, given the threshold τ , the critical dimension (CD) of a single line is determined by the interval $\{x \in \mathbb{R} | \rho_{D,\text{total}}(x) \geq \tau\}$ (see Figure 1).

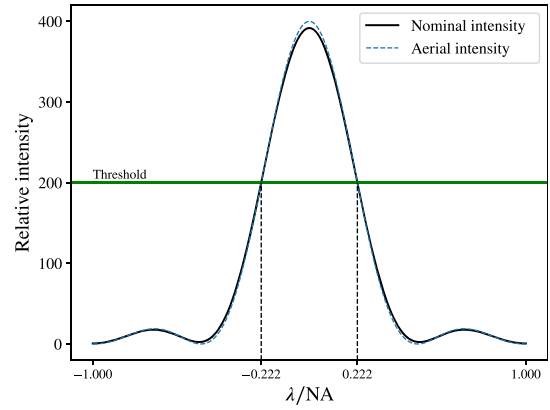


FIGURE 1 The simplest family of single-line patterns defined by aerial intensity. The dashed and solid lines indicate the aerial and resist image intensities, respectively. The interval determined by the threshold (green line) corresponds to the nominally patterned region.

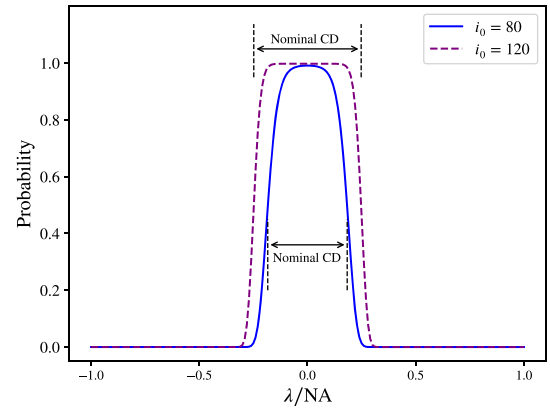


FIGURE 2 Probabilities for a single-pixel formation of a single line under two relative intensities.

For a large i_0 , we may approximate $\rho_{D,\text{total}}$ as in (37). Figure 2 illustrates the probability of pixel generation at each point on x with two different relative intensities: $i_0 = 80$ and $i_0 = 120$.

Finally, we consider the pattern-missing probability for a nominally patterned region. As noted above, the exact computation of excursion probability is highly demanding. However, the lower bound of an excursion probability can be computed if a unique peak in P exists in the second moment of the Gaussian random field. Explicitly,

$$P\left[\sup_{x \in P} \rho_{D,\text{total}}(\mathbf{x}, t_f) \geq \tau\right] \geq \Phi\left(\frac{\tau}{\left(\sup_{x \in P} E[\rho_{D,\text{total}}^2(x)]\right)^{1/2}}\right). \quad (42)$$

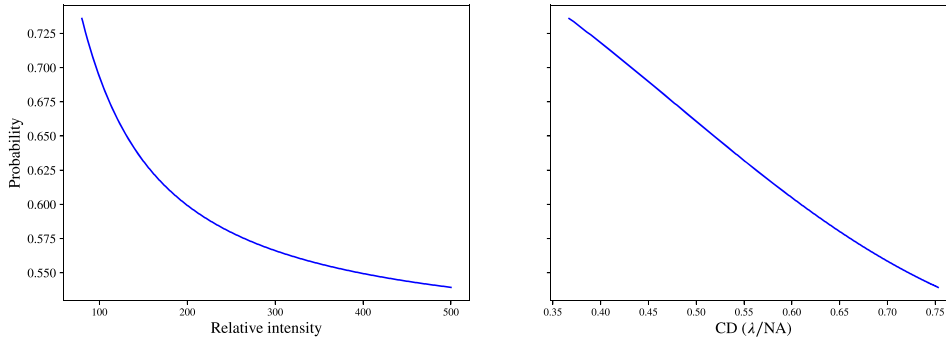


FIGURE 3 Probability of no patterning in the region reserved by the nominal resist intensity with respect to the relative dose (left) or nominal critical dimension (CD) (right).

The lower bound of the excursion probability on P then provides the upper bound of the missing probability as

$$p_{\text{missing}}(P) \leq 1 - \Phi \left(\frac{\tau}{\left(\sup_{x \in P} E[\rho_{D,\text{total}}^2(x)] \right)^{1/2}} \right). \quad (43)$$

Figure 3 shows the relation between the probability of no patterning in the nominally patterned area and the relative intensity (left) or nominal CD (right). As shown in both figures, our simple example qualitatively captures the characteristics of the stochastic printing failures in [15].

Another consequence of a large W condition is the probabilistic deviation of the boundary of a given feature from its nominal boundary. For this, let \mathbf{x}_0 be the nominal boundary of the feature, so that for a given threshold τ , $E[\rho_{D,\text{total}}(\mathbf{x}_0)] = \tau$.

For a large W condition, we may consider the probabilistic deviation of the boundary of a given feature from its nominal boundary. For this, let \mathbf{x}_0 be the nominal boundary of the feature, so that for a given threshold τ , $E[\rho_{D,\text{total}}(\mathbf{x}_0)] = \tau$.

Then for a small deviation $\delta\mathbf{x}$, we have the condition

$$\begin{aligned} \tau &= \rho_{D,\text{total}}(\mathbf{x}_0 + \delta\mathbf{x}, t; \mathbf{X}_j, T_j) \\ &\simeq \rho_{D,\text{total}}(\mathbf{x}_0, t; \mathbf{X}_j, T_j) + \delta x^m \partial_m \rho_{D,\text{total}}(\mathbf{x}_0, t; \mathbf{X}_j, T_j) \end{aligned} \quad (44)$$

to $\mathbf{x}_0 + \delta\mathbf{x}$ be a deviated boundary. Therefore, by defining the line edge roughness (LER) as

$$\text{LER} = E[\delta x^2], \quad (45)$$

one finds

$$\text{LER} \simeq \frac{W \sigma_D^2}{\partial_m^i i_{\text{resist}}(\mathbf{x}_0) \partial_m i_{\text{resist}}(\mathbf{x}_0)} \quad (46)$$

which reproduces the result of [4].

4 | CONCLUSION AND OUTLOOK

In this work, we have applied QED to obtain a fully quantum mechanical description of photochemical acid generation identified with the photoelectric detection of light. We have seen that the well-known proportionality between the probability of acid generation and the intensity of incident light can be reproduced under certain assumptions in the QED framework.

Although we have focused merely on the occurrence of acid generation, a more detailed analysis is available in the QED framework by emphasizing the dynamics of charged matter and the final state of the exposure system. For instance, one may split the final state of the photons by the momentum of a state having an acute angle with respect to the incident wave vector to investigate the rate of flare generation during exposure. Also, by specifying the dynamics of charged matter to be that of electrons through the spin 1/2-field, one can determine the rate of generation of secondary electrons having sufficient energy to further trigger the deprotection mechanism. In this sense, the QED formulation provides an integrated framework for investigating secondary effects, which will be discussed in future studies.

Using probabilistic acid generation, we have constructed a probabilistic description of deprotection density in the photoresist, as reported by [4, 5]. The probabilistic nature of the deprotection density reveals the relationship between the expectation of deprotection and the resist image intensity in convolution imaging.

In addition, the explicit form of the deprotection density allows us to perform an asymptotic analysis under a large absorption condition, which refines the work of [4, 5]. In particular, under asymptotic conditions, we have found that deprotection density can be depicted by a Gaussian random field, enabling the simulation of randomness in the resist image using a Monte Carlo type simulation.

In a typical lithography process, a large absorption condition can be achieved by enlarging the exposed area of interest, and an asymptotic analysis can thus be used to construct a simulation model for quantum fluctuations in

the patterning process. In particular, by approximating the deprotection blur $\kappa = (\int_E d^4x \eta) \times (\int_E d^4y \rho_D^2(y))$ as a constant, we can express the asymptotic formula as follows:

$$\rho_{D,\text{total}}(\mathbf{x}, t_f) \sim \mathcal{N}(i_{\text{resist}}(\mathbf{x}, t_f), \kappa i_{\text{aerial}}(\mathbf{x}, t_f)), \quad (47)$$

so that κ is fitted by measurement under the given resist image intensity and aerial intensity computed by a conventional simulation model. This simulation model is conceptually similar to that in [5], which has been widely applied to construct EUV stochastic models [16–19].

Finally, the parameter κ can be considered as the leading characteristic of the photoresist, which governs the sensitivity of the resist under quantum fluctuations. Thus, κ can be considered a physically refined parameter of the k_4 factor in [20].

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CONFLICT OF INTEREST STATEMENT

The authors declare no potential conflicts of interest.

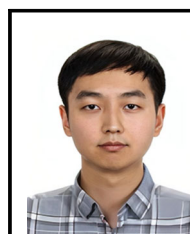
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