# Nonlocality effects of MgB<sub>2</sub> superconductor

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(Received 28 August 2023; revised or reviewed 27 September 2023; accepted 28 September 2023)

#### Abstract

Magnetic properties of MgB<sub>2</sub> superconducting powder were investigated. M(H), the magnetic field H dependence of magnetization M, was measured and analyzed using a PPMS instrument. The MgB<sub>2</sub> superconducting powder showed high critical current density  $J_c > \sim 10^7$  A/cm<sup>2</sup> and clean limit superconducting properties. The equilibrium magnetization  $M_{eq}$  properties of MgB<sub>2</sub> powders exhibiting various superconducting properties were studied. We find that the equilibrium magnetization  $M_{eq}(H)$  properties of MgB<sub>2</sub> powders showing conventional BCS properties deviate from the predictions of the standard local-London theory at temperatures below T = 19 K and are in good agreement with the generalized nonlocal-London theory. Nonlocal-London analysis was used to determine and analyze the nonlocal parameters. The temperature dependence of the London penetration depth values  $\lambda(T)$  was studied.

Keywords: MgB2 powder, equilibrium magnetization, nonlocal-london theory, local-london theory, london penetration depth

## **1. INTRODUCTION**

MgB<sub>2</sub> is a metallic two-component material and has a simple hexagonal crystal structure, but shows very diverse superconducting properties [1-3]. MgB<sub>2</sub> superconductors show conventional BCS superconducting properties similar to those of common metallic superconductors, but with a higher critical transition temperature ( $T_c \sim 38$  K) compared to BCS low-temperature superconductors. They also show high critical current density ( $J_c(0) > 10^7 \text{ A/cm}^2$ ) due to strong coupling between grain boundaries, with a superconducting coherence length ( $\xi(0) \sim 5$  nm) longer than the grain-boundary width ( $d = 1 \sim 3$  nm) [2-5]. In particular, MgB<sub>2</sub> superconductors exhibit multi-band properties with weak scattering between bands, characterized by two-energy gaps: a cylindrical 2D- $\sigma$  band  $(\Delta_{\sigma} \sim 7.0 \text{ meV})$  and an isotropic 3D- $\pi$  band  $(\Delta_{\pi} \sim 1.7 \text{ meV})$ meV) [6-12]. MgB<sub>2</sub> superconductors with two-bands and two-energy gaps exhibit a variety of superconducting properties and novel physical characteristics, and have been described by the anisotropic s-wave superconducting model of weakly coupled two-energy gaps [10]. In general, anisotropic superconducting properties are represented by a single anisotropic parameter,  $\gamma = \xi_{ab}/\xi_c = \lambda_c/\lambda_{ab}$ . However, the  $MgB_2$  superconductor with weakly coupled two-energy gaps shows anisotropic parameter characteristics of  $\gamma_{Hc2} \neq$  $\gamma_{\lambda}$ , where  $\gamma_{\text{Hc2}} = H_{\text{c2,ab}} / H_{\text{c2,c}}$  is the upper-critical magnetic field anisotropic parameter and  $\gamma_{\lambda} = \lambda_c / \lambda_{ab}$  is the London penetration depth anisotropic parameter. Here is  $H_{c2,c}$  =  $\overline{\phi}_0/2\pi\xi_{ab}^2$  and  $H_{c2,ab} = \phi_0/2\pi\xi_{ab}\xi_c$ . It is  $\gamma_{Hc2} = \sim 6.0$  and  $\gamma_{\lambda} = \sim 1.1$  near  $T = \sim 0$  K, and exhibits a single anisotropic parameter  $\gamma = \xi_{ab}/\xi_c = \lambda_c/\lambda_{ab}$  characteristic with  $\gamma_{Hc2} =$  $\gamma_{\lambda} = \sim 2.6$  near the critical transition temperature  $T_{\rm c}$  [10]. Therefore, it can be predicted that the superconducting properties of MgB<sub>2</sub> in the temperature region near the critical transition temperature  $T_c$  and in the temperature region somewhat farther away from  $T_c$  will be somewhat different from each other.

On the other hand, the isotropic nature of the electrical conduction due to the long electron mean free path l and the upward curvature of the upper-critical magnetic field  $H_{c2}$ near  $T_c$ , similar to the nickel-borocarbide materials YNi<sub>2</sub>B<sub>2</sub>C and LuNi<sub>2</sub>B<sub>2</sub>C superconductors, show that MgB<sub>2</sub> superconductors have clean limit superconducting properties [13]. The temperature dependence of  $\gamma_{Hc2}$  in the MgB<sub>2</sub> superconductor and the isotropic properties of  $\gamma_{\lambda}$  (~ 1.1) in the low temperature region far from  $T_{c}$  can also be explained by the clean limit superconductivity. The flux line lattice (FLL) structure change of nickel-borocarbide YNi<sub>2</sub>B<sub>2</sub>C superconductor with clean limit superconducting properties, i.e., from a triangular structure to a square structure, is well described by the generalized nonlocal-London theory, and the equilibrium magnetization  $M_{eq}$  properties of YNi<sub>2</sub>B<sub>2</sub>C superconductor in the low-temperature regime deviate somewhat from the conventional standard local-London theory predictions and are also well described by the generalized nonlocal-London theory [14].

Therefore, similar to the analysis of boron carbide  $YNi_2B_2C$  superconductor, this paper simultaneously performs a generalized nonlocal-London theory analysis based on the clean limit superconducting properties in the low temperature region far from  $T_c$  and a conventional standard local-London theory analysis based on the dirty limit superconducting properties in the high temperature region near  $T_c$  for the equilibrium magnetization  $M_{eq}$  values of MgB<sub>2</sub> superconducting prowder samples. The

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magnetization M(H) values were measured at 2 K temperature intervals from 5 K to 37 K using a physical property measurement system (PPMS) equipment, and the equilibrium magnetization  $M_{eq}$  values of the MgB<sub>2</sub> superconducting powder samples were analyzed from these M(H) measurement data. The temperature dependence of the London penetration depth  $\lambda(T)$  values obtained by applying the generalized nonlocal-London theory and the characteristics of the nonlocal parameters obtained by the generalized nonlocal-London theory analysis were also studied.

## 2. EXPERIMENTAL PROCEDURE

The MgB<sub>2</sub> powder sample used in this study is a commercially available powder sample purchased from Alfar Aesar company. As described in a previous paper [15], the purchased  $MgB_2$  powder samples are pure  $MgB_2$ powder samples with few impurity phases in XRD analysis. The mass of the MgB<sub>2</sub> powder sample used in the experiment is 0.23 g, and the theoretical density of the  $MgB_2$  single crystal is 2.63 g/cm<sup>3</sup>, so the superconductor volume of the MgB<sub>2</sub> powder sample used in the experiment is  $V_s = 0.087$  cm<sup>3</sup>. And in the analysis using a particle size analyzer, the average size of the  $MgB_2$  powder sample is r  $= \sim 0.5 \,\mu\text{m}$ . The magnetic properties of the MgB<sub>2</sub> powder samples (powder in capsules) were measured by sweeping the magnetic field H at each temperature from 5 K to 37 K at 2 K intervals using a PPMS (Quantum Design (QD), USA). The magnetic field H applied during PPMS measurements was increased (or decreased) from 0 T to 9 T (or from 9 T to 0 T) to measure the magnetic field Hintensity dependence m(H) of the magnetic moment m at each temperature. The unit for magnetic moment *m* is [emu =  $G \cdot cm^3$ ]. The measured m(H) data were divided by the superconductor volume of the sample, i.e., a value of  $V_s =$  $0.087 \text{ cm}^3$ , to obtain the magnetic field H strength dependence M(H) of the magnetization M for the MgB<sub>2</sub> powder sample. The unit of magnetization M is [G].

Meanwhile, the critical transition temperature,  $T_c$ , of the MgB<sub>2</sub> powder sample (powder in capsules) was determined by measuring and analyzing the temperature dependence of the magnetic moment, m(T), under zero field cooling (ZFC) measurement conditions, i.e., decreasing the temperature, T= 5 K, without applying a magnetic field, then fixing it by applying a magnetic field, H = 10 G, and then increasing the temperature, T. And the magnetization M(H) data was analyzed using the background magnetization M(H) values measured at a temperature higher than the critical transition temperature  $T_c$  of the MgB<sub>2</sub> powder sample as correction values. The magnetic properties of the MgB2 powder samples were analyzed by converting the measured magnetization M data into irreversible magnetization  $\Delta M$ data. The irreversible magnetization  $\Delta M = [M(H_{dec}) M(H_{inc})$ ] value, defined as the difference between the magnetization M values in the increasing and decreasing magnetic field regions, is the physical quantity associated with the critical current density  $J_c$  of the MgB<sub>2</sub> powder sample, and it can be used to predict the critical current

density  $J_c(H)$  through the Bean critical state model, i.e., the  $J_c = 20\Delta M/r$  relation [16]. Where *r* is the mean grain radius, the average radius of the polycrystalline MgB<sub>2</sub> powder sample used in this study is  $r = \sim 0.5 \,\mu\text{m}$ . In addition, the magnetic properties of MgB<sub>2</sub> powder samples were analyzed by obtaining the magnetic field *H* dependence  $M_{eq}(H)$  of the equilibrium magnetization  $M_{eq}$  by using the magnetiz field *H* dependence M(H) data of the magnetization *M* for MgB<sub>2</sub> powder samples. Here, the equilibrium magnetization  $M_{eq}$  value, defined as the average value of the magnetic field regions, was obtained by the formula  $M_{eq} = [M(H_{dec}) + M(H_{inc})]/2$ .

### **3. RESULTS AND DISCUSSION**

A common measurement for investigating the magnetic properties of a superconducting sample using a PPMS magnetometer instrument is the m(H) graph, which is the dependence of the magnetic field H on the magnetic moment m. For the MgB<sub>2</sub> superconducting powder sample, m(H) graphs were measured at specific temperatures from 5 K to 37 K in 2 K intervals, respectively. That is, by measuring the change in m(H) while increasing the magnetic field H intensity applied to the MgB<sub>2</sub> superconducting powder sample from 0 G to 9 T, and then measuring the change in m(H) while decreasing the magnetic field H intensity from 9 T to 0 G, keeping each specific temperature in the 2 K interval constant, independent m(H) graphs were obtained for each specific temperature in the 2 K interval. The magnetic moment m(H) data were divided by the superconductor volume of the sample,  $V_s = 0.087 \text{ cm}^3$ , to obtain M(H) graphs, which are the magnetic field H dependence of the magnetization M for the MgB<sub>2</sub> superconducting powder sample. Fig. 1 shows M(H) graphs, the dependence of magnetization M on magnetic field H, for a sample of MgB<sub>2</sub> superconducting powder at each specific temperature. As can be seen in Fig. 1, the M(H) graphs are nearly top-to-bottom symmetric at M = 0 G. For most temperatures, the M(H) data exhibit both irreversible ( $\Delta M \neq 0$ ) and reversible ( $\Delta M \approx$ 0) magnetization properties.



Fig. 1. The superconductive magnetization M versus magnetic field H of the pure MgB<sub>2</sub> powder, for temperatures from 5 K to 37 K in steps of 2 K.



Fig. 2. The critical current density  $J_c$  versus magnetic field H of the pure MgB<sub>2</sub> powder, for temperatures from 5 K to 37 K in steps of 2 K.

Fig. 2 is a graph of  $J_c(H)$ , the dependence of the critical current density  $J_c$  on the magnetic field H, for the MgB<sub>2</sub> superconducting powder sample. The critical current density,  $J_c$ , is one of the typical physical quantities of superconducting materials in general. By applying the data obtained from PPMS magnetization M(H)measurements to the Bean critical state model, the critical current density  $J_c$  values of MgB<sub>2</sub> superconducting powder samples can be predicted and determined. The Bean critical state model is represented by  $J_c = 20\Delta M/r$  [16], where r is the mean grain radius, and  $\Delta M$  is the irreversible magnetization, which is the difference between the magnetization  $M(H_{inc})$  value in the magnetic field region where the magnetic field strength applied to the sample increases and the magnetization  $M(H_{dec})$  value in the magnetic field region where the magnetic field strength decreases, i.e.,  $\Delta M = [M(H_{dec}) - M(H_{inc})]$ . As shown in Fig. 2, it shows high critical current density  $(J_c > \sim 10^7 \text{ A/cm}^2)$ characteristics due to strong coupling between grain boundaries. However, the critical current density  $J_c$ characteristic of MgB<sub>2</sub> superconducting powder samples without introducing artificial flux pinning defects is significantly degraded with increasing applied magnetic field *H* strength, showing  $J_c \sim 0$  in the region of H > 4 T and above.

Fig. 3 is a graph of m(T) obtained by measuring the dependence of the magnetic moment m on temperature T under ZFC (zero field cooling) conditions. First, after lowering to a temperature T = 5 K below the critical transition temperature  $T_c$  with no magnetic field H applied, and then a magnetic field strength of H = 10 G is applied at temperature T = 5 K. Under these ZFC conditions, keeping H = 10 G, the magnetic moment m is measured with slowly increasing the temperature T from 5 K to 50 K, that is, a graph of m(T) is obtained. As shown in Fig. 3, the temperature at which the diamagnetic or Meissner effect characteristics (m(T) < 0) start in the m(T) graph is determined as the critical transition temperature  $T_c$ , and the  $T_c$  of the MgB<sub>2</sub> superconducting powder sample is 38.0 K.

As described in the introduction, MgB<sub>2</sub> superconductors exhibit conventional BCS electron-phonon mechanism superconducting properties [17], but due to the nature of the two bands and two energy gaps, they exhibit a variety of



Fig. 3. The ZFC curve as the function of temperature *T* for the pure MgB<sub>2</sub> powder, with H = 10 G. The  $T_c$  was defined by the onset temperature.

novel superconducting and physical properties [2-12]. The temperature-dependent  $\lambda(T)$  characteristics of London penetration depth  $\lambda$  are related to the size of the energy gaps: in the high temperature region near the critical transition temperature  $T_c$ , the  $\lambda(T)$  is strongly influenced by the wide energy gap of the 2D- $\sigma$  band ( $\Delta_{\sigma} \sim 7.0$  meV), while in the low temperature region,  $T \ll T_c$ , the  $\lambda(T)$  is strongly influenced by the narrow energy gap of the 3D- $\pi$ band ( $\Delta_{\pi} \sim 1.7$  meV) [8-11]. In addition, one of the interesting properties of MgB<sub>2</sub> superconductors is the change in their anisotropic superconducting properties. The two bands and two energy gaps characterize anisotropic superconductivity as  $\gamma_{Hc2} \neq \gamma_{\lambda}$  in the low temperature region, which is  $T \ll T_c$ , and as  $\gamma_{Hc2} = \gamma_{\lambda}$  in the high temperature region near  $T_c$ , that is, a single anisotropic parameter  $\gamma = \xi_{ab}/\xi_c = \lambda_c/\lambda_{ab}$  characteristic [10]. Therefore, we can predict that there are different superconducting mechanisms in the two temperature regions, one at  $T \ll T_c$ and the other near  $T_{\rm c}$ .

It can be predicted that MgB<sub>2</sub> superconductor is a clean limit superconductor because of its long electron mean free path l and upward curvature characteristic in the upper critical magnetic field  $H_{c2}$ . If the superconductivity of clean-limit MgB2 is truly nonlocal, then its equilibrium mixed-state (vortex-state) properties, like those of borocarbide clean-limit YNi<sub>2</sub>B<sub>2</sub>C superconductors, are very difficult to explain with the conventional local-London theory and must be explained with a generalized nonlocal-London theory [14]. Therefore, it should be shown that the equilibrium magnetization  $M_{eq}$ properties of MgB<sub>2</sub> superconducting powder samples deviate from the predictions of the local-London theory and are in good agreement with the predictions of the generalized nonlocal-London theory. Therefore, to obtain  $M_{eq}(H)$ , the magnetic field H dependence of the equilibrium magnetization  $M_{eq}$  for the MgB<sub>2</sub> powder sample, we used the M(H) data, the magnetic field H dependence of the magnetization M shown in Fig. 1. Here, the equilibrium magnetization  $M_{eq}$  value is defined as the average value of the magnetization M values in the increasing and decreasing magnetic field regions, and is obtained using the  $M_{eq} = [M(H_{dec}) + M(H_{inc})]/2$  equation. Fig. 4 shows the semi-logarithmic relationship between the



Fig. 4. A semilogarithmic plot of equilibrium magnetization  $M_{eq}$  versus magnetic field *H* of the pure MgB<sub>2</sub> powder, for temperatures from 5 K to 35 K.

equilibrium magnetization,  $M_{eq}$ , and the magnetic field, H, for temperatures from T = 5 K to 35 K. As can be seen in Fig. 4, there is a clear distinction between non-linear graphs for temperatures below T = 19 K and linear graphs for temperatures above T = 21 K. In general, linear graphs above temperature T = 21 K are well explained by the standard local-London theory, and nonlinear graphs below temperature T = 19 K can be explained relatively well by the generalized nonlocal-London theory.

According to standard local-London theory, in a magnetic field region of  $H_{c1} \ll H \ll H_{c2}$ , the relation between the equilibrium magnetization  $M_{eq}$  and the magnetic field H is expressed as  $M_{eq} = -M_0 \ln(\eta H_{c2}/H)$  [18]. Where  $M_0$  is the  $M_0 = \phi_0/32\pi^2\lambda_{ab}^2$ ,  $H_{c1} = \phi_0 \ln(\lambda_{ab}/\xi)/4\pi\lambda_{ab}^2$ is the lower-critical magnetic field,  $H_{c2} = \phi_0/2\pi\xi^2$  is the upper-critical magnetic field, ris a constant of base unit size,  $\lambda_{ab}^2$  is the London penetration depth, and  $\xi$  is the Ginzburg-Landau coherence length. Thus, as shown in Fig. 4, the linear graphs above temperature T = 21 K are well described by the standard local-London theory of a logarithmic magnetic field (lnH) dependence on the equilibrium magnetization  $M_{eq}$ , i.e., a proportional relationship of  $M_{\rm eq} \propto \ln H$ . At temperatures above T = 21 K in Fig. 4, the slope of the linear graph is equal to the  $M_0$ value. Therefore, we can obtain the slope values at each temperature above T = 21 K in Fig. 4, and apply these slope values to the  $M_0 = \phi_0/32\pi^2\lambda_{ab}^2$  equation to predict the London penetration depth  $\lambda_{ab}^2$  at each temperature. We will return to this discussion when we describe Fig. 6.

On the other hand, the properties of nonlinear graphs at temperatures below T = 19 K in Fig. 4 cannot be explained by the proportional relationship of  $M_{eq} \propto \ln H$ , the standard local-London theory. The generalized nonlocal-London theory of Kogan-Gurevich is obtained by introducing a nonlocality-radius  $\rho$  that depends on the mean free path *l*, and applying a new concept of  $H_0 = \phi_0/2\pi^2 3^{1/2}\rho^2$  magnetic field instead of  $H_{c2} = \phi_0/2\pi\xi^2$  for the equilibrium magnetization  $M_{eq}$  [19-20]. Here, the nonlocality radius  $\rho$  slowly decreases with increasing temperature, which is the opposite property of the Ginzburg-Landau coherence length  $\xi$ . According to the generalized nonlocal-London theory applying these length  $\rho$  and magnetic field  $H_0$  scales,

the relationship between the equilibrium magnetization  $M_{eq}$ and the magnetic field *H* in the  $H_{c1} \ll H \ll H_{c2}$  magnetic field region is expressed as  $M_{eq} = -M_0[\ln(H_0/H + 1) H_0/(H_0+H) + \zeta$ ] [19-20]. Here  $M_0 = \phi_0/32\pi^2\lambda_{ab}^2$  is the same as in the local-London theory, the new magnetic field scale magnetic field  $H_0$  is  $H_0 = \phi_0/2\pi^2 3^{1/2} \rho^2$ , and the dimensionless quantity  $\zeta$  is  $\zeta(T) = \eta_1 - \ln(H_0/\eta_2 H_{c2} + 1)$ represented by the basic unit size constants  $\eta_1$  and  $\eta_2$ . From Fig. 4, it can be seen that in the temperature region below T = 19 K, the nonlinear graphs are in good agreement with the generalized nonlocal-London theory, and as the temperature increases, the degree of curvature of the nonlinear graphs in the  $H_{c1} \ll H \ll H_{c2}$  magnetic field region gradually decreases and becomes increasingly linear, and near the critical transition temperature  $T_c$ , the graphs are almost completely linear. It can be seen that the clean limit MgB<sub>2</sub> superconducting properties exhibit nonlocal superconducting properties in the temperature region of T $\ll$  T<sub>c</sub>, and then the nonlocal superconducting properties



Fig. 5. Parameters from nonlocal London analysis versus temperatures for the pure MgB<sub>2</sub> powder: (a) the field scale  $H_0$  and product  $\gamma H_0$ , (b) the magnetization  $M_0$ , and (c) dimensionless quantity  $\zeta$ .

gradually disappear with increasing temperature, and change to fully local superconducting properties near  $T_c$  in the high temperature region.

In Fig. 4, the nonlinear graphs in the temperature region below T = 19 K can be applied to the generalized nonlocal-London theoretical relation to obtain three nonlocal parameters:  $H_0$ ,  $M_0$ , and  $\zeta$ . This means that the values of the parameters  $H_0$ ,  $M_0$ , and  $\zeta$  can be determined for each temperature by substituting the nonlinear graph data for each temperature into the generalized nonlocal-London theoretical expression and fitting those. Fig. 5 shows the temperature dependence of the nonlocal parameters, namely  $H_0(T)$ ,  $M_0(T)$ , and  $\zeta(T)$  graphs. When T = 5 K from the  $H_0 = \phi_0/2\pi^2 3^{1/2} \rho^2$  relational expression, nonlocality-radius  $\rho$  is calculated to be  $\rho \approx 7.40 \times 10^{-8}$  m. Since the nonlocal-radius  $\rho$  depends on the mean free path *l*, we can predict the long mean free path l of the MgB<sub>2</sub> powder sample, and thus predict that the MgB<sub>2</sub> powder sample has clean limit superconducting properties.

As shown in Fig. 5(a), we can see that the  $H_0(T)$  value increases as the temperature increases. The temperature dependence of the calculated  $\gamma H_0$  value is shown in Fig. 5(a) by selecting the  $\gamma(T)$  value of the clean limit condition which is  $\xi/l \approx 0$ , from the  $\gamma(T)$  values calculated by V. G. Kogan [20]. For the borocarbide clean limit YNi<sub>2</sub>B<sub>2</sub>C superconductor, the  $\gamma H_0$  value is constant with increasing temperature, as predicted by the generalized nonlocal-London theory [14], but for our clean limit MgB<sub>2</sub> powder sample, the  $\gamma H_0$  value increases rather weakly with increasing temperature. These results are considered to be due to irreversible characteristics in a wide magnetic field region, as shown in the magnetization M(H) graph of the clean limit MgB<sub>2</sub> powder sample. In general, the generalized nonlocal-London theory can be applied to clean limit superconductors that exhibit a large region of reversibility in the magnetization M(H) graph, and their experimental results are well explained by nonlocality. On the other hand, similar to the nonlocality results of borocarbide  $YNi_2B_2C$ superconductors and HTS superconductors [14], it can be seen that the  $M_0(T)$  and  $\zeta(T)$ values gradually decrease with increasing temperature, as shown in Figs. 5(b) and 5(c). By applying and analyzing the generalized nonlocal-London theory, we can predict the London penetration depth  $\lambda_{ab}{}^2$  for each temperature from the  $M_0 = \phi_0/32\pi^2\lambda_{ab}^2$  values obtained in the lower temperature regime below T = 19 K. This will be discussed in conjunction with the London penetration depth  $\lambda_{ab}^2$  for each temperature in the higher temperature region above T= 21 K obtained by applying standard local-London theory when explaining Fig. 6.

Fig. 6 shows the temperature dependence of  $1/\lambda^2$  for a clean limit MgB<sub>2</sub> superconducting powder sample. As explained earlier and shown in Fig. 6, the  $1/\lambda^2$  values for the temperature region below T = 19 K are obtained by applying the generalized nonlocal-London theory, while the  $1/\lambda^2$  values for the temperature region above T = 21 K are obtained by applying the standard local-London theory. Furthermore, as shown in the inset of Fig. 6, it can be seen that the temperature dependence of the  $1/\lambda^2$  values obtained



Fig. 6. The temperature dependence of London penetration depth  $\lambda$  for the pure MgB<sub>2</sub> powder. In inset, the straight line shows Ginzburg-Landau behavior near  $T_{\rm c}$ , for data obtained from standard London analysis.

by applying the standard local-London theory near the criti cal transition temperature  $T_c$  is almost linear, as predicted by the Ginzburg-Landau theory [21-23], which predicts tha t the MgB<sub>2</sub> powder sample exhibits clean limit BCS conve ntional superconducting properties.

### 4. SUMMARY

In the low temperature region away from the critical transition temperature  $T_c$ , i.e., at temperatures below T = 19K, where  $T \ll T_c$ , the equilibrium magnetization  $M_{eq}$ properties of the clean limit MgB2 superconducting powder sample deviated from the predictions of the standard local-London theory, but agreed with the predictions of the generalized nonlocal-London theory with some accuracy. However, at temperatures above T = 21 K, the equilibrium magnetization  $M_{eq}$  properties of the clean limit MgB<sub>2</sub> superconducting powder sample were in exact agreement with the predictions of the conventional standard local-London theory. The nonlocal-London effect, which appears at temperatures below T = 19 K, gradually disappears at temperatures above T = 21 K. In the temperature region near the critical transition temperature  $T_{\rm c}$ , the results are fully consistent with the standard local-London theory. Meanwhile, the London penetration depth  $\lambda_{ab}^2$  of the clean limit MgB<sub>2</sub> superconducting powder sample was obtained by applying the nonlocal-London theory at temperatures below T = 19 K and the local-London theory at temperatures above T = 21 K, respectively. The linear temperature dependence of  $1/\lambda^2$ obtained by applying the local-London theory in the temperature region near the critical transition temperature  $T_{\rm c}$  is similar to the results predicted by the Ginzburg-Landau theory.

# ACKNOWLEDGMENT

This work was supported by a grant from the Basic Science Research Program, administered through the National Research Foundation of Korea (NRF) and funded by the Ministry of Education (NRF-2021R1A2C1094771).

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