



Investigation on structural symmetry of CsCoCl₃·2H₂O crystals by magic-angle spinning ¹H and static ¹³³Cs nuclear magnetic resonance

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Abstract The phase transition temperatures of CsCoCl₃·2H₂O crystals are investigated via differential scanning calorimetry (DSC) and thermogravimetric analysis (TGA). Three endothermic peaks at temperatures of 370 K (=T_{C1}), 390 K (=T_{C2}), and 416 K (=T_{C3}) were observed for phase transitions from CsCoCl₃·2H₂O to CsCoCl₃·1.5H₂O, to CsCoCl₃·H₂O, and then to CsCoCl₃·0.5H₂O, respectively. In addition, the spin-lattice relaxation time T_{1ρ} in the rotating frame and T₁ in the laboratory frame as well as changes in chemical shifts for ¹H and ¹³³Cs near T_{C1} were found to be temperature dependent. Our analyses results indicated that the changes of chemical shifts, T_{1ρ}, and T₁ are associated with structural phase transitions near temperature T_{C1}. The changes of chemical shifts, T_{1ρ}, and T₁ near T_{C1} were associated with structural phase transitions, owing to the changes in the symmetry of the structure formed of H₂O and Cs⁺ ions. Consequently, the structural symmetry in CsCoCl₃·2H₂O crystals based on temperature is discussed by the environments of their H and Cs nuclei.

Keywords CsCoCl₃·2H₂O, spin-lattice relaxation time, thermal property, nuclear magnetic resonance

Introduction

Lower-dimensional magnetic systems have attracted significant attention from researchers.¹⁻¹¹ In particular, these materials show significant results in the field of physical chemistry; considerable attention is focused on the development of materials suitable for strong energy absorption by solar collectors. However, systems that exhibit one-dimensional Heisenberg-like behavior, such as CsMnCl₃·2H₂O, have been the primary focus of these researches. When the Mn²⁺ ion in CsMnCl₃·2H₂O is replaced with a Co²⁺ ion, anisotropic effects that yield Ising-like behavior are typically observed in the resulting compound.¹²⁻¹⁵ The crystal structure of CsCoCl₃·2H₂O was first determined by Thorup and Soling;¹ they reported that its crystal structure was identical to that of CsMnCl₃·2H₂O. In particular, at room temperature, the space group of CsCoCl₃·2H₂O was *Pcca* with lattice constants *a*=0.8914 nm, *b*=0.7174 nm, *c*=1.1360 nm, and *Z*=4. Thus, CsCoCl₃·2H₂O can be considered as an example of an Ising-like chain antiferromagnet. The crystal structure of orthorhombic CsCoCl₃·2H₂O at room temperature is shown in Fig. 1; as shown in the figure, the Co²⁺ ions in the compound are arranged in the form of -Co-Cl-Co- chains along the *a*-axis such that each Co²⁺ ion is surrounded by an octahedral coordination

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consisting of four Cl^- ions and two O_2^- ions. The chains along the b -axis are separated by layers consisting of Cs ions, while those along the c -axis were hydrogen-bonded as $\text{Cl}\cdots\text{H}-\text{O}-\text{H}$.¹¹ Thus, the resulting octahedral structure of $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ is such that each Cs^+ ion is surrounded by eight Cl^- ions as their nearest neighbors.

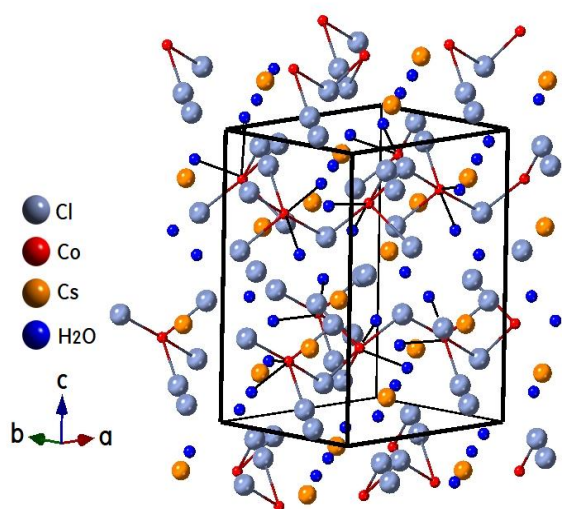


Figure 1. Orthonormal structure of a $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ crystal at room temperature (CCDC: 1593038).¹

Herweijer et al.³ studied the magnetic properties of $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ via specific heat, nuclear magnetic resonance (NMR), magnetic susceptibility, magnetization, and antiferromagnetic resonance measurements. In addition, an antiferromagnetic transition at $T_N=3.4$ K was also previously observed in $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ using NMR techniques.^{2,4} Moreover, the spin-lattice relaxation time T_1 of ^{133}Cs in $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ was measured near T_N in the laboratory frame by Goto and Kawai.⁹ Recently, ^{133}Cs NMR measurements have proved to be valuable in the research on novel materials,^{16, 17} and quantum chemical calculations have demonstrated their utility in realizing the structural interpretation of ^{133}Cs NMR spectra.^{18, 19}

In this study, the crystal structure of laboratory-grown $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ was investigated via X-ray diffraction experiments. Moreover, the phase transition temperatures and thermodynamic property

of the $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ crystals were analyzed through differential scanning calorimetry (DSC) and thermogravimetric analysis (TGA). Furthermore, the spin-lattice relaxation times $T_{1\rho}$ in the rotating coordination for ^1H and T_1 in the laboratory coordination for ^{133}Cs in $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ crystals according to the temperature are discussed. Finally, the structural symmetry of $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ crystals based on temperature is discussed by the environments of their H and Cs nuclei. The key objective of this study is to clarify the effects of temperature and paramagnetic ions on $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ crystals with water molecules.

Experimental Procedures

In the experiments, $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ single crystals were obtained by slow evaporating an aqueous solution containing CsCl and $\text{CoCl}_2\cdot 6\text{H}_2\text{O}$ in the molar ratio of 1:1. The resulting crystals were light blue in color.

The structure of a single $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ crystal was confirmed using an X-ray diffractometer (XRD) (Korea Basic Science Institute, Seoul Western Center, Seoul). In addition, the phase transition temperatures were measured using a DSC instrument (TA, DSC 25) by increasing the temperature from 150–600 K; these measurements were conducted at a heating rate of $10^\circ\text{C}/\text{min}$. Furthermore, a TGA device (TA, Q600) was used to perform TGA experiments in order to understand the decomposition phenomena under a N_2 atmosphere at different temperatures with the same heating rate as in the case of the DSC measurements. The changes in the appearance of $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ single crystals with increasing temperature were captured using an optical polarization microscope wherein the as-grown crystal was placed on a Linkam THM-600 heating stage.

Magic angle spinning (MAS) ^1H NMR spectra and $T_{1\rho}$ values for the $\text{CsCoCl}_3\cdot 2\text{H}_2\text{O}$ crystal were obtained using a 400-MHz Avance II+ Bruker NMR spectrometer equipped with 4-mm MAS probes (Korea Basic Science Institute, Seoul Western Center). The Larmor frequency $\omega_0/2\pi$ in the MAS ^1H

NMR experiment was set to 400.13 MHz; in addition, the MAS rate was set to 10 kHz to minimize spinning sidebands. The NMR chemical shifts were recorded by using tetramethylsilane (TMS) as the standard. In addition, the static ¹³³Cs NMR spectra and T₁ for the ¹³³Cs nuclei in CsCoCl₃·2H₂O single crystal were measured using the same spectrometer; herein, the magnetic field strength was set to 9.4 T with the Larmor frequency $\omega_0/2\pi$ for ¹³³Cs nuclei set to 52.485 MHz. The resonance frequency was recorded using CsCl as the standard. The temperature dependences for ¹H and ¹³³Cs were measured by increasing the temperature from 180–430 K. For the NMR measurements, the temperature of the sample was kept constant with an accuracy of $\pm 0.5^\circ\text{C}$ while N₂ gas and heater current were passed through the device.

Experimental Results and Discussion

Our X-ray diffraction measurement results showed that the CsCoCl₃·2H₂O crystals had an orthorhombic structure with cell parameters $a=0.9218$ nm, $b=0.7288$ nm, and $c=1.1083$ nm; these results are consistent with those previously reported by Thorup and Soling.¹ Three endothermic peaks were observed at 370 K, 390 K, and 416 K in the DSC results as shown in Fig. 2. The mass of the powdered CsCoCl₃·

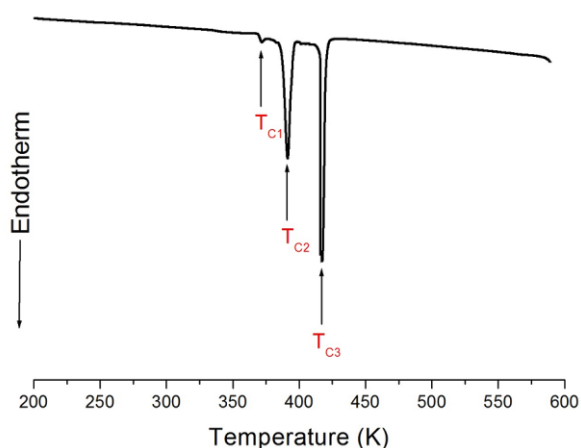


Figure 2. DSC thermogram of CsCoCl₃·2H₂O crystals.

2H₂O sample used for DSC measurements was 4.11

mg. In addition, TGA was used to determine whether these three peaks represented structural phase transitions or phase melting temperatures. The TGA curve for CsCoCl₃·2H₂O is shown in Fig. 3; herein, the mass of CsCoCl₃·2H₂O sample used was 7.08 mg. The loss in mass during the TGA experiment was first noted at approximately 350 K. This aspect was characterized by a loss in the weight of the compound. The loss in the weight of CsCoCl₃·2H₂O (M_w=334.23 mg) was observed at high temperatures. The amount of the obtained solid residues was calculated considering the molecular weight of the compound by using Eq. (1)

$$[\text{CsCoCl}_3 \cdot 1.5\text{H}_2\text{O} (\text{s}) + 0.5\text{H}_2\text{O} (\text{g})] / \text{CsCoCl}_3 \cdot 2\text{H}_2\text{O} = 97.30 \%$$

$$[\text{CsCoCl}_3 \cdot \text{H}_2\text{O} (\text{s}) + \text{H}_2\text{O} (\text{g})] / \text{CsCoCl}_3 \cdot 2\text{H}_2\text{O} = 94.61 \%$$

$$[\text{CsCoCl}_3 \cdot 0.5\text{H}_2\text{O} (\text{s}) + 1.5\text{H}_2\text{O} (\text{g})] / \text{CsCoCl}_3 \cdot 2\text{H}_2\text{O} = 91.91 \%$$

$$[\text{CsCoCl}_3 (\text{s}) + 2\text{H}_2\text{O} (\text{g})] / \text{CsCoCl}_3 \cdot 2\text{H}_2\text{O} = 89.22 \%$$

(1)

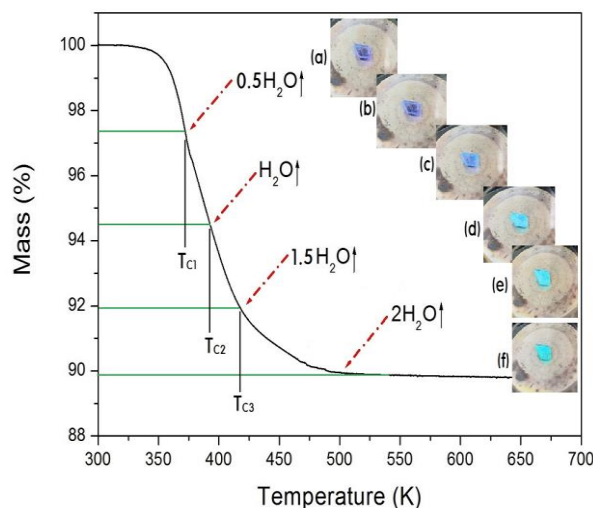


Figure 3. TGA curve of CsCoCl₃·2H₂O single crystals. Inset: The color variation of the crystals at temperatures of (a) 293 K, (b) 353 K, (c) 373 K, (d) 403 K, (e) 473 K, and (f) 573 K obtained using an optical polarization microscope.

The thermal decompositions around 370 K and 390 K, which were also indicated via the obtained DSC peaks, were accompanied by partial escape of

0.5H₂O and H₂O, respectively. The residue of the partial products was 97.30 % and 94.61 %, which suggests that CsCoCl₃·2H₂O undergoes decomposition during the dehydration process; in particular, it was observed that CsCoCl₃·2H₂O loses 1.5 molecules of water of crystallization transforming to CsCoCl₃·0.5H₂O at 416 K. Furthermore, the original CsCoCl₃·2H₂O sample underwent complete thermal decomposition to CsCoCl₃ near 500 K. Based on the obtained DSC and TGA results, the endothermic peaks near 370 K (=T_{C1}), 390 K (=T_{C2}), and 413 K (=T_{C3}) for CsCoCl₃·2H₂O decomposition could be attributed to the incremental loss of H₂O molecules from the crystal. Our optical polarization microscopy results for CsCoCl₃·2H₂O showed that the crystals are light blue in color at room temperature and that this color changes as the temperature is increased. In particular, the crystals retain their light blue color between 293 and 373 K, and start turning slightly opaque at approximately 403 K, before becoming fully opaque around 573 K. These changes in color with increasing temperature can also be attributed to the loss of H₂O molecules from the crystal.

The temperature dependences of the chemical shifts in the MAS ¹H NMR spectrum of CsCoCl₃·2H₂O crystals were recorded; these are shown in the inset in Fig. 4. In the temperature range of 180 K–370 K, the ¹H chemical shift was nearly constant at 7 ppm, however, above 370 K, the ¹H chemical shift increased rapidly to approximately 25 ppm. This phenomenon could be attributed to the effect of the paramagnetic (Co²⁺ ions) near H as a certain amount of H₂O was lost.

The T_{1ρ} values were obtained using a π/2–τ sequence by changing the spin-locking pulses: the π/2 pulse widths for ¹H were 26 μs and 9 μs below and above 370 K, respectively. It was observed that the areas of the MAS ¹H NMR spectra for different delay times at each temperature followed a single exponential function. The corresponding decay curve for spin-locked proton magnetization is characterized by T_{1ρ} as follows:^{20–22}

$$P(\tau) = P(\infty)\exp(-\tau/T_{1\rho}), \quad (2)$$

where P(τ) and P(∞) are the areas under the NMR signal at times τ=0 and τ=∞, respectively. Using the slopes of the plots for the area under the NMR signal for different delay times, the ¹H T_{1ρ} data for CsCoCl₃·2H₂O was obtained for each temperature; as shown in Fig. 4, the ¹H T_{1ρ} values were in the range of 5–20 μs and were dependent on temperature. It can also be observed that T_{1ρ} decreases abruptly after T_{C1} at which temperature the last remaining 0.5H₂O is lost. Similar to the rapid change in the ¹H chemical shift above T_{C1}, the reduction in ¹H T_{1ρ} is likely a result of the effect of the presence of the paramagnetic Co²⁺ ion in the vicinity as a certain amount of H₂O is lost. The ¹H T_{1ρ} values in the case of the paramagnetic ions are smaller than those in the absence of paramagnetic ions because T_{1ρ} is inversely proportional to the square of the magnetic moment of the paramagnetic ions.^{19, 23} Thus, the ¹H T_{1ρ} values were driven by fluctuations in the magnetic dipole of the paramagnetic Co²⁺ ions.

The static NMR spectra of ¹³³Cs (I=7/2) in a

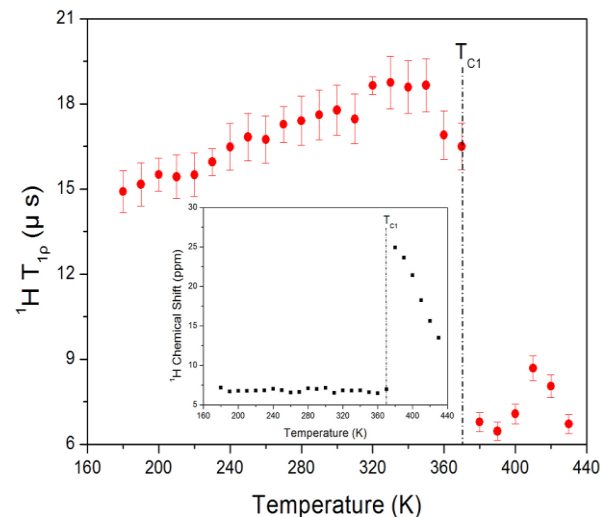


Figure 4. MAS ¹H NMR spin-lattice relaxation times T_{1ρ} in CsCoCl₃·2H₂O with increasing temperature. Inset: Temperature dependency of ¹H chemical shifts as a function of temperature.

CsCoCl₃·2H₂O single crystal at various temperatures were measured at a Larmor frequency ω₀/2π = 52.485 MHz; these are as shown in Fig. 5. The seven

resonance lines are due to the quadrupole interaction of the ¹³³Cs nucleus; consequently, the NMR spectrum for ¹³³Cs consists of six satellite resonance lines and one central resonance line. The resonance frequencies for ¹³³Cs obtained via NMR were measured in the temperature range of 180–430 K. The Cs NMR spectra were obtained using CsCl as the reference; their resonance frequencies were recorded with increasing temperature in the high frequency direction by the paramagnetic Co²⁺ ions. These shifts in the ¹³³Cs signal are caused by dipole-dipole interactions between the magnetic moments of the paramagnetic Co²⁺ atoms and those of the Cs⁺ nuclei. Seven Cs resonance lines were observed in the NMR spectra for temperatures in the range of 180–360 K, while only one Cs resonance line was observed above 370 K. The realization of only one Cs resonance line at temperatures above T_{C1} indicates that the phase transition above this temperature is the dynamic averaging of the crystal electric field and the cubic symmetry field around Cs,

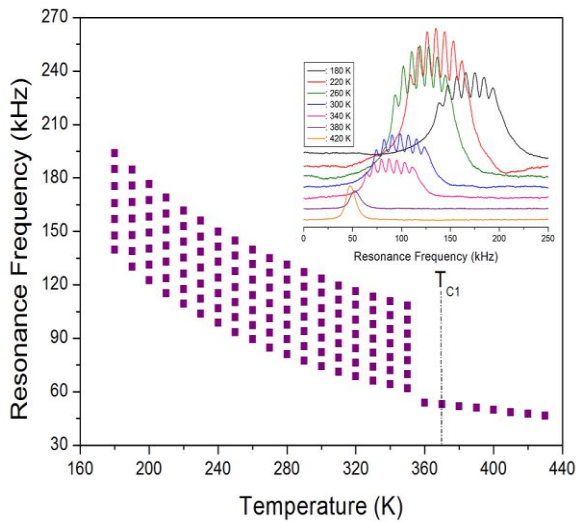


Figure 5. Static ¹³³Cs NMR resonance frequencies for a CsCoCl₃·2H₂O crystal with increasing temperature. Inset: ¹³³Cs NMR spectra at several temperatures.

which, in turn, conveys that the surrounding Cl⁻ sites around Cs⁺ in CsCoCl₃·2H₂O are symmetrical above T_{C1} . Further, the changes in the structural geometry of the surrounding sites around Cs are caused by the loss of water molecules around the Cs nucleus, and

they play an important role at high temperature.

The magnetization recovery trace for ¹³³Cs in the CsCoCl₃·2H₂O crystals with quadrupole relaxation is represented as the sum of four exponential functions and can be expressed as follows:^{24, 25}

$$\begin{aligned} [P(\infty) - P(\tau)] / P(\infty) = & 0.048 \exp(-0.476 P_1\tau) + 0.818 \\ & \exp(-1.333 P_1\tau) + 0.050 \exp(-2.381 P_1\tau) + 0.084 \\ & \exp(-3.810 P_1\tau) \end{aligned} \quad (3)$$

where $P(\tau)$ is the nuclear magnetization of the central transition among several transitions and P_1 is the transition probability for $\Delta m = \pm 1$. The return to thermal equilibrium is characterized by the four terms in Eq. (3). However, because the spin system rapidly returned to thermal equilibrium depending on the spin temperature similar to our high-temperature experiments, the relaxation is described using just a single relaxation time T_1 . Thus, the saturation recovery data at high temperatures can be satisfactorily fitted using the following relationship with a single exponential function:^{26, 27}

$$[P(\infty) - P(\tau)]/P(\infty) = \exp(-P\tau). \quad (4)$$

Thus, the relaxation time T_1 for ¹³³Cs can be obtained in terms of $1/P$.

The T_1 values for the ¹³³Cs nuclei in the crystals were measured using the $\pi/2 - \tau - \pi/2$ pulse sequence method. The nuclear magnetization $P(\tau)$ of the ¹³³Cs nuclei at time τ after the application of $\pi/2$ pulses was obtained based on the saturation recovery sequence. The width of $\pi/2$ pulses used for ¹³³Cs in our experiment was 4.1–6 μ s. The saturation curves of the ¹³³Cs nuclei were measured at various delay times; in addition, the slopes of these curves were obtained as a function of delay time in the range of 1 μ s–400 ms as shown in Fig. 6. The relaxation time, T_1 , was calculated directly from the slope of the plot for $\log [P(\infty) - P(\tau)] / P(\infty)$ versus time τ . The saturation curve for the central line of ¹³³Cs is represented by a combination of four exponential functions. The temperature dependences of the ¹³³Cs transition rates P_1 and P_2 were fitted using Eq. (3), while the ¹³³Cs relaxation times at low temperatures were obtained in terms of P_1 ($T_1 = 1/1.333P_1$).

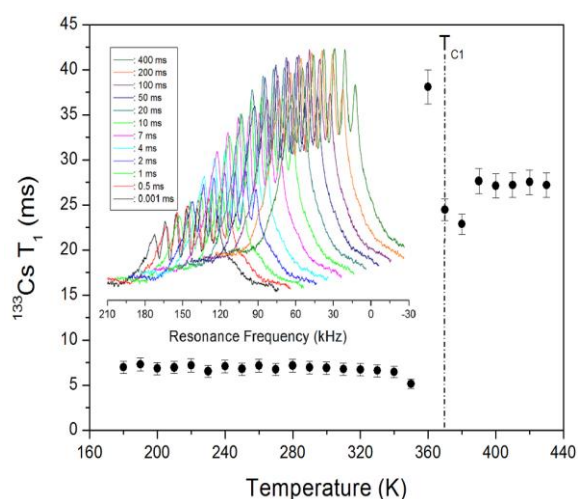


Figure 6. Temperature dependency of the spin-lattice relaxation time T_1 for ^{133}Cs in a $\text{CsCoCl}_3 \cdot 2\text{H}_2\text{O}$ single crystal. Inset: Saturation curves for ^{133}Cs with delay times of 1 μs –400 ms at 300 K.

These temperature dependence plots of the ^{133}Cs T_1 for $\text{CsCoCl}_3 \cdot 2\text{H}_2\text{O}$ crystals is shown in Fig. 6; in particular, the T_1 values of the ^{133}Cs nuclei were nearly constant below 360 K. However, T_1 changes suddenly at the phase transition temperature of 370 K ($=T_{\text{Cl}}$), which is consistent with the ^{133}Cs NMR spectra and DSC results. T_1 value increases near 360 K and then decrease again near 370 K. Above that temperature, it remains at a similar value. The increase in T_1 at 360 K is thought to be due to the breaking of the bond before loss of H_2O around Cs. As previously indicated, the change of T_1 near T_{Cl} ($=370$ K) is related to the changes in the geometry of the H_2O and Cl^- surrounding the Cs^+ ions. Moreover, the rapid increase in T_1 above 370 K indicates that H_2O is lost around Cs, which hinders the energy transfer compared to that at lower temperatures.

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Conclusions

The structure and lattice constants of $\text{CsCoCl}_3 \cdot 2\text{H}_2\text{O}$ crystals were determined via x-ray diffraction measurements. In addition, the thermal property and phase transition temperature of these crystals were investigated via TGA and DSC. It was observed that phase transitions occur in the crystals at temperatures of 370 K, 390 K, and 416 K. In particular, the endothermic peak at 370 K ($=T_{\text{Cl}}$) was related to the phase transition from $\text{CsCoCl}_3 \cdot 2\text{H}_2\text{O}$ to $\text{CsCoCl}_3 \cdot 1.5\text{H}_2\text{O}$. Furthermore, the changes in the temperature dependence of ^1H chemical shifts and $T_{1\rho}$ near T_{Cl} were associated with structural phase transitions owing to the loss of H_2O molecules, which, in turn, caused the distortion of the octahedral structure of H_2O molecules surrounding Co^{2+} . The resonance lines in the ^{133}Cs spectra reduced from seven to one near T_{Cl} , which could be attributed to this structural transformation. Thus, the changes in the temperature dependence of ^{133}Cs T_1 near T_{Cl} observed in our study were related to changes in the symmetry of the structure formed of the four Cl^- ions and two H_2O about the Cs^+ ion. At temperatures above T_{Cl} , the environments around H and Cs changed owing to H_2O loss; specifically, as a certain amount of H_2O was lost, ^1H $T_{1\rho}$ was considerably affected by Co^{2+} around H, and as H_2O was lost around Cs, T_1 increased owing mainly to the influence of the 4 Cl^- ions around Cs^+ . Consequently, the thermodynamic properties and structural geometry of the $\text{CsCoCl}_3 \cdot 2\text{H}_2\text{O}$ single crystals were studied by analyzing these environments.

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