# A Contour Descriptors-Based Generalized Scheme for Handwritten Odia Numerals Recognition

Tusar Kanti Mishra\*, Banshidhar Majhi\*, and Ratnakar Dash\*

### Abstract

In this paper, we propose a novel feature for recognizing handwritten Odia numerals. By using polygonal approximation, each numeral is segmented into segments of equal pixel counts where the centroid of the character is kept as the origin. Three primitive contour features namely, distance (l), angle ( $\theta$ ), and arc-to-chord ratio (r), are extracted from these segments. These features are used in a neural classifier so that the numerals are recognized. Other existing features are also considered for being recognized in the neural classifier, in order to perform a comparative analysis. We carried out a simulation on a large data set and conducted a comparative analysis with other features with respect to recognition accuracy and time requirements. Furthermore, we also applied the feature to the numeral recognition of two other languages—Bangla and English. In general, we observed that our proposed contour features outperform other schemes.

#### Keywords

Contour Features, Handwritten Character, Neural Classifier, Numeral Recognition, OCR, Odia

# 1. Introduction

Handwritten optical character recognition (OCR) has numerous practical and commercial applications. Until now, it has been a challenging task to devise a perfect OCR for all languages. This is due to the presence of severe inter-variables existing between characters of different languages. One of the major complexities is the presence of intra-variability between writing styles among users. In India, 22 official languages with distinct characteristics are used indifferent states. Odia is one of the official languages of India that is used by 27 million people in the state of Odisha. There are 12 vowel characters and 25 consonants. Like any other language, Odia has ten numerals. The character set for the Odia language, including numerals, is given in Fig. 1.

Numerous feature extraction and selection methods have been reported in the literature on OCR [1]. The features like curvature [2,3], F-ratio [4], Zernike moments [5], discrete cosine transformation [6], and skeletal convexity [7] have been used for character recognition. In [8], the authors have used Gabor filters for extracting features from a gray-scale character image. Histogram features are extracted from the real part of the Gabor filter output which shows a satisfactory recognition performance of Chinese characters. A Bayesian decision-based neural network (BDNN) for a multi-linguistic handwritten

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Corresponding Author: Tusar Kanti Mishra (tusar.k.mishra@gmail.com)

<sup>\*</sup> Dept. of Computer Science and Engineering, National Institute of Technology Rourkela, Rourkela, Odisha 769001, India (tusar.k.mishra@gmail.com, bmajhi@nitrkl.ac.in, ratnakar.dash@gmail.com)

character recognition scheme has been proposed in [9]. It takes into account the four directional strokes of a character. The prototype system demonstrates the successful utilization of the self-growing probabilistic decision-based neural network (SPDNN) for recognizing Chinese handwritten characters. In [10], character recognition for the Hindi language using an artificial neural network where they considered the histogram based on projection and pixel values in their features part has been proposed. A commercially viable Telugu character recognizer has been reported in [11]. Wavelet multi-resolution analysis and associative memory models have been used for feature extraction and recognition purposes, respectively. For accomplishing the learning task, a Hopfield-based dynamic neural network has been used. Printed Odia characters have been successfully recognized using a combination of stroke and run-number based features [12]. These features are obtained by using the concept of water overflow in a reservoir. However, no fine-tuning of their work has been carried out. The hidden Markov model (HMM) has been used for recognizing handwritten Odia numerals [13]. HMM is generated out of the shape primitives of an individual numeral and is referred to as a template for establishing a match for probe numerals. For this matching task, its class conditional probability is found by comparing it to each HMM.

It has been observed that most of the OCR schemes reported in other studies perform well for a particular language. However, these schemes then perform poorly for other languages. Hence, there exists a potential need to devise a general scheme for the recognition of the handwritten characters of multiple languages. Furthermore, for Odia handwritten character recognition, a fewer number of schemes are available in the literature on character recognition. In this paper, we propose a contour-based feature neural classifier (CFNC), which is a simple and effective scheme for Odia handwritten numeral recognition. Simulations have been carried out on three different languages namely, Odia, Bangla, and English handwritten numerals, in order to validate the suggested scheme.

The paper is organized as follows: Section 2 deals with the proposed scheme, which includes feature extraction, selection, and classification phases. Section 3 describes the simulation results that were performed on numerals from three different languages. Our performance comparison with two other existing schemes is given in Section 4. Finally, we provide our concluding remarks in Section 5.



Fig. 1. Character set for the Odia language.

# 2. Proposed Scheme

The proposed scheme, CFNC, involves preprocessing, feature extraction, and recognition phases and its overall block diagram is shown in Fig. 2. Each character is represented as a  $30\times30$  (pixel) image. In the preprocessing phase, several tasks, such as noise removal, standardization, and normalization [14-16], are performed using standard schemes on the image prior to feature extraction. Our scheme focuses mostly on feature extraction and recognition. The character is represented by a one dimensional contour descriptor  $T = (t_1, t_2 \dots, t_m)$ , which is an ordered set of *m* real valued variables that are taken clockwise from the contour [17, 18]. Polygonal approximation is applied to the contour descriptor to generate three basic feature vectors to represent the numeral image. Subsequently, these feature sets are used to classify the numeral using the back propagation neural network (BPNN). The feature extraction and recognition steps are discussed below sequentially.

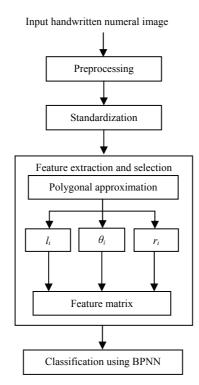


Fig. 2. Block diagram of the proposed scheme. BPNN=back propagation neural network.

### 2.1 Feature Extraction

The overall process of feature extraction has been described in Algorithm 1. The numeral images are subjected to pre-processing, such as binarization and a thinning operation, prior to the contour descriptor being extracted. Polygonal approximation has been conducted on the pre-processed image. By using polygonal approximation, each numeral is segmented into *S* different segments of equal pixel counts where the centroid of the character is kept as the origin. To help illustrate and clarify our point, we have shown the segments of the Odia number '3' in Fig. 3. Three primitive features, distance  $(l_i)$ ,

angle ( $\theta_i$ ), and ratio ( $r_i$ ), are extracted from these segments. The distance feature  $l_i$  represents the distance between the centroid and the starting point ( $p_i$ ) of the *i*<sup>th</sup> segment. The angle feature,  $\theta_i$ , is the angle between  $l_i$  and chord  $v_i$ , which lies between the *i*<sup>th</sup> and (i + 1) <sup>th</sup> segment, and the ratio,  $r_i$ , represents the ratio between the chord  $v_i$  and arc  $S_i$ . Thus, we have a 1 × S dimension of each primary feature and if we arrange the three different features in rows, the feature vector  $f_v$  of dimension 3 × S for each numeral is generated, which is given as:

$$f_{v} = \begin{pmatrix} l_{1} & l_{2} & \cdots & l_{i} & l_{i+1} & l_{s} \\ \theta_{1} & \theta_{2} & \cdots & \theta_{i} & \theta_{i+1} & \theta_{s} \\ r_{1} & r_{2} & \cdots & r_{i} & r_{i+1} & r_{s} \end{pmatrix}$$
(1)

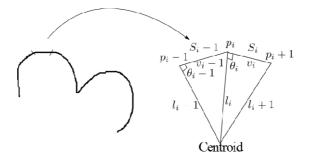


Fig. 3. Polygonal approximation of the Odia numeral '3'.

#### Algorithm 1. Feature\_Extraction\_and\_Selection

Step 1. Initialize feature vector,  $f_v \leftarrow$  NULL

Step 2. For each character image  $c_i$  from dataset D do

Step 3. Set counter,  $cnt \leftarrow 1$ 

Step 4. While  $cnt \le S$ ; where S is the number of segments

Step 5. Extract features  $l_{cnt}$ ,  $\theta_{cnt}$  and  $r_{cnt}$  per segment as:

(a)  $l_{cnt} \leftarrow$  length measure from centre of  $c_i$  to the segment

(b)  $\theta_{cnt} \leftarrow$  angle between corresponding chord and  $l_{cnt}$  at the current segment

(c)  $r_{cnt} \leftarrow$  ratio between current segment chord and corresponding arc

Step 6. Create column vector,

$$cl_{cnt} = \begin{pmatrix} l_{cnt} \\ \theta_{cnt} \\ r_{cnt} \end{pmatrix}$$

Step 7. 
$$f_v \leftarrow \text{concatenate} (f_v, cl_{cnt})$$
  
Step 8. Increment counter,  $cnt \leftarrow cnt + 1$ 

Step 9. End While

Step 10. End For

These feature descriptors are unique to a particular character. For choosing the starting pixel in the profile, one can choose the farthest or nearest pixel from the centroid. If more than one point exists (e.g., with a circular character), then any of these two points can be selected. In our case, the leftmost isolated point on the contour has been chosen as the starting point for segmentation. The algorithm for

(2)

feature point selection has a time complexity of  $O(n_c)$  where  $n_c$  is the number of contour points. The selection of the number of segments is a heuristic choice, and it should be selected in such a manner where the average smoothness factor, r (ratio between chord and arc), should be above 75% to keep the quality of the perfect polygonal approximation contour description.

### 2.2. Recognition by Classification Using BPNN

The neural network has been successfully utilized for pattern classification and recognition [19-21]. For the purpose of recognition in our case, we used a feed forward neural structure for classifying the numerals. A set of feature vectors collected from numerals, along with a corresponding numeral as the target, constitute the training patterns. For training, the back propagation, which is based on conjugate gradient algorithm (CGA), has been used and the update equations are defined as:

$$E_{qw}(y) = E(w) + E'(w)^{T}y + \frac{1}{2}y^{T}E''(w)y$$
(3)

$$E'_{qw}(y) = E''(w)y + E'(w)$$
(4)

Where, E(w) is the error function,  $E_{qw}$  and is the quadratic approximation to in a neighborhood of point 'w'. The set of steps involved in carrying out the conjugate gradient (CG) is listed in Algorithm 2. Using a step size scaling mechanism makes it possible to avoid a time-consuming line search in every iterations of the training and it achieves a faster convergence.

Algorithm 2. Conjugate\_Gradient\_Algorithm (CGA)

 $\begin{array}{ll} Step \ 1. & Chose initial weight vector, w_1 \\ Step \ 2. & Set \ p_1 = r_1 = -E(w_1), k = 1 \\ Step \ 3. & Calculate second order information: \ E^H(w_k)p_k \ and \ d_k = \ p_k'(s_k) \\ Step \ 4. & Calculate step size \ \mu_k = \ p_k'r_k \ and \ \alpha_k = \ \mu_k/d_k \\ Step \ 5. & Update weight vector \ w_{k+1} = \ w_k + \ \alpha_k p_k \ and \ r_{k+1} = \ E'(w_{k+1}) \\ Step \ 6. & If \ k \ mod \ m = 0 \ then \ restart \ algorithm: \ p_{k+1} = \ r_{k+1}, \ where \ m \ is \ the \ number \ of \ weights \\ Step \ 7. & Else \ create \ new \ conjugate \ direction: \ \beta_k = \ \frac{r_{k+1}^2 - r_{k+1}'r_k}{\mu_k} \\ Step \ 8. & \ p_{k+1} = \ r_{k+1} + \ \beta_k p_k \\ Step \ 9. & If \ the \ steepest \ descent \ direction \ r_k \neq 0 \ then \ set \ k = k + 1 \ and \ go \ to \ step -2 \\ Step \ 10. \ Else \ return \ w_{k+1} \ as \ desired \ minimum \ and \ terminate \end{array}$ 

### 3. Experimental Evaluation

To validate our proposed CFNC scheme, simulations were carried out with handwritten numerals from the Odia, Bangla, and English languages. The overall simulation was divided into two different experiments to study the various aspects of the CFNC scheme. The experiments are discussed below in detail.

# 3.1. Experiment 1: Study of Training Convergence Characteristics

Handwritten Odia numerals were collected from various individuals at different times and a dataset size of 3,000 [22] was created. Each numeral has been represented as a 30×30 (pixel) image. The feature vector of  $f_v$ , for each numeral was extracted by using Algorithm 1. A total of 34 segments were chosen for each numeral and hence, the feature vector is a 3×34 matrix of distance ( $l_i$ ), angle ( $\theta_i$ ), and ratio ( $r_i$ ) as row vectors, respectively. For experimental evaluation, a set of 200 samples was randomly selected and the training patterns( $f_v$ )<sub>j</sub>:  $t_j$ , j = 1, 2, ... 200) are were used for training. The neural network structure with the node specification of 102-30-10 is shown in Fig. 4. To enhance the reliability and faster convergence of back propagation training, a conjugate gradient was used. The convergence characteristic is shown in Fig. 5.

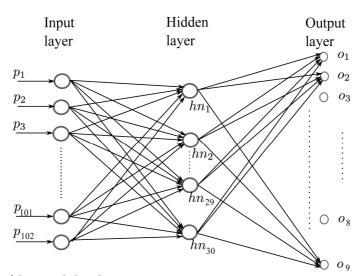
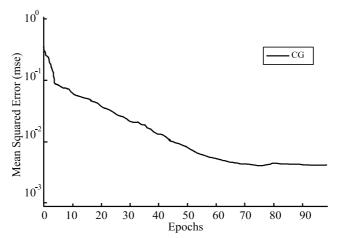


Fig. 4. Structure of the neural classifier.



**Fig. 5.** Convergence characteristics of back propagation neural network (BPPN) training using Odia numerals. CG=conjugate gradient.

### 3.2. Experiment 2: Performance Analysis on Odia Numerals

Two hundred handwritten numerals were randomly selected from the dataset for each numeral that was not used during training of the classifier. This was done in order to evaluate the performance of the proposed feature along with the neural classifier. An accuracy comparison of the proposed scheme was carried out with state-of-the-art approaches like Zernike moments, the curvature feature, and discrete cosine transformation (DCT) features, as shown in Table 1. It has been observed that for all numerals, the proposed CFNC scheme outperforms other schemes.

To show the impact of illumination variance on numerals, samples of unequal illuminations were considered and the output results for the Odia number '2' are shown in Fig. 6. It was observed that even if there is a change in illumination, the handwritten numeral '2' has been correctly recognized. However, a misclassification had also been observed. For example, the numeral '6' was recognized as '7,' due the similarity between the two numerals, as shown in Fig. 7.

The experimental evaluation was then extended to the numerals of two other languages, Bangla and English, for which corresponding data samples were collected from [22] and [23], respectively. Handwritten numerals from both of the languages were used with different features and two neural classifiers were devised for recognizing the numerals in these two languages. The overall comparative analysis for Odia, Bangla, and English is shown in Table 2. Furthermore, the time requirement for classifying the test dataset was also computed for all of the features.

Accuracy (%)

98.5

95.5

96.5

95

89

88

87

89.5

93

92.5

94

94

97

96

97.5

92

98

96

97.5

92

			_		
Digit/class	Scheme	Accuracy (%)		Digit/class	Scheme
0	CFNC	98.5			CFNC
	Zernike	91			Zernike
	DCT	94 8		8	DCT
	Curvature	91			Curvature
و	CFNC	96	ې		CFNC
	Zernike	92			Zernike
	DCT	93.5			DCT
	Curvature	90			Curvature
	CFNC	97.5			CFNC
9	Zernike	92.5	୭		Zernike
	DCT	95.5			DCT
	Curvature	90			Curvature
	CFNC	97.5	r		CFNC
60	Zernike	95			Zernike
୩	DCT	95			DCT
	Curvature	94			Curvature
۵	CFNC	98	¢		CFNC
	Zernike	96.5			Zernike
	DCT	97.5			DCT
	Curvature	92.5			Curvature

Table 1. Performance comparison for handwritten Odia numerals on 200 samples

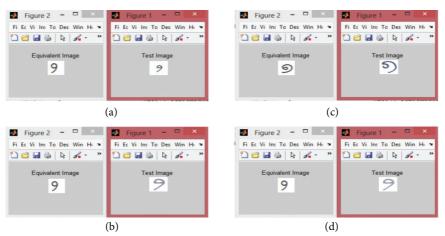


Fig. 6. Impact of illumination variation on numerals.



Fig. 7. Similarity between the '6' and '7' of the Odia language.

Table 2. Overa	ll performance	comparison
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Language/ feature	Training samples	Testing samples	DCT		Zernike moments		Curvature feature		Contour descriptor	
			Time (sec)	Accuracy (%)	Time (sec)	Accuracy (%)	Time (sec)	Accuracy (%)	Time (sec)	Accuracy (%)
Odia	1,000	2,000	1,640	92	275	93.5	412	94.8	70	96.25
Bangla	500	1500	1,320	87.66	244	92	405	93.3	58	94.22
English	1,000	2,000	1,628	91.5	270	92.2	410	94	65	95

It has been observed that the proposed contour feature has outperformed three state-of-the-art features (Table 2) with respect to time requirement and accuracy. Hence, our proposed feature can be considered as an alternative for the numeral recognition of any language. The overall accuracy rates for recognizing Odia numerals when using CFNC, Zernike moments, and the curvature feature were found to be 96.25%, 93.5%, and 94.8%, respectively.

# 5. Conclusion

In this paper, we propose a novel feature for recognizing the numerals of any language. In particular, more focus was placed on recognizing Odia numerals. Three primary features of length, angle, and ratio, were extracted from segments that had been derived from the contour of a numeral. The contour was further decided based on the polygonal approximation on a numeral image. These features were then used in a neural classifier to recognize the numerals. Other existing features were also considered for recognition in the neural classifier, in order to perform a comparative analysis. In general, it has

been observed from our exhaustive simulation study that the proposed feature outperforms other features with respect to recognition accuracy and time requirements. Furthermore, the feature was also applied to the numeral recognition of two other languages—Bangla and English. Our proposed feature also demonstrated a similar performance with these two languages. Hence, the proposed feature can be considered as a generalized alternative for the numeral recognition of any language. The scheme can also be extended for conducting the recognition of any character.

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#### Tusar Kanti Mishra http://orcid.org/0000-0002-4665-6625

He received his B.Tech degree with honours in Computer Science and Engineering from Biju Patnaik University of Technology, Odisha, India in 2004. He received his M.Tech degree in 2011 and is currently a Ph.D. research scholar in the Department of Computer Science and Engineering at the National Institute of Technology Rourkela, India. His research interests are in the areas of computer vision, image processing and pattern recognition.



#### Banshidhar Majhi http://orcid.org/0000-0002-2843-1908

He is presently working as a professor in the Department of Computer Science and Engineering, NIT Rourkela. He has 24 years of teaching and research experience and 3 years of industry experience. His research interests include image processing, computer vision, cryptographic protocols and iris biometrics. He has guided 10 doctora lworks and published 45 articled in referred journals.



#### **Ratnakar** Dash

He earned his B.Tech degree from National Institute of Science and Technology, India, in 2002 and M.Tech degree from University College of Engineering, India in 2005. He is currently pursuing his Ph.D. degree in image processing at National Institute of Technology Rourkela, India. His research interest also includes digital signal processing and communication.