

# Generation of Business Process Reference Model Considering Multiple Objectives

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## ABSTRACT

The implementation of business process management (BPM) systems in large number of business organizations transforms BPM system into such a level of maturity and tends to collect large repositories of business process (BP) models. This issue encourages BP flexibility that leads to a large number of process variants derived from the same model, but differing in structure, to be stored in the large repositories of BP models. Therefore, the repositories may include thousands of activities and related business objects with variation of requirements and quality of service. It is a common practice to customize processes from reference processes or templates in order to reduce the time and effort required to design and deploy processes on all levels. In order to address redundancy and underutilization problems, a generic process model, called as reference BP, is absolutely necessary to cover the best of process variants. This study aims to develop multiple-objective business process genetic algorithm (MOBPGA) to find a set of non-dominated (Pareto) solutions of business reference model to enhance conventional approach which considered only a single objective on creating BP reference model by using proximity score measurement. A mixed-integer linear program is constructed to evaluate performance of the proposed MOBPGA on small-scale problems by using standard measures for multiple-objective techniques. The results will show the viability of applying MOBPGA in terms of simultaneously maximizing proximity score measurement, minimizing total duration, and total costs of the selected reference model.

Keywords: Business Process Management, Business Process Reference Model, Multi-Objective, Genetic Algorithm

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## 1. INTRODUCTION

It is a common practice to customize processes from reference processes or templates in order to reduce the time and effort required to design and deploy processes on all levels (Lu and Sadiq, 2006). In order to address redundancy and underutilization problems, a generic process model, called as business process (BP) reference, is absolutely necessary to cover the best of process vari-

ants. Industrial process model collections and reference process models (e.g., ITIL, SCOR, eTOM) are some related concepts, practices and standards for developing such a process model. However, those concepts are settled as a high-level model without considering the customization implementation. Customization is a major trend that occurs in many industries and markets resulting from the customer's specific demand on goods and services.

The notion of BP variant is important in explaining the customization in this study. We use the terminology of BP variant to represent the different kind of customized BP with almost similar business objectives. For example, a supplier offers, specifies, produces and delivers different kinds of products to its customers, or suppliers have different kinds of actor relationships that separate orders and frame contracting. Due to the different kinds of BP, there will be a problem in resolving which process is appropriate to a given organization. The difficulty derives from the fact that the activities involved in taking an account to contribute in two or more than hundreds of process. It is certain that a "good" process should be obtained. In order to obtain a "good" process, it is necessary to find a generic process, later called as reference model, that considers a part of sequential view of process with an understanding of the business properties included in the activity.

Approaches to the generation of BP reference models have been explored. Previous work on BP reference model generation has utilized proximity score measurement (PSM) and dealt with activity proximity and frequency as well as validity (Yahya *et al.*, 2010). A reference model with only a single alternative solution is equally unsatisfactory to stakeholder. Cost and duration, indeed, are two additional important factors relevant to business objectives. In contrast to the single-objective case, a multi-objective approach can be used to simultaneously optimize, subject to certain constraints, two or more conflicting objectives so as to find a valid and representative BP reference model. Multi-objective optimization is the process of simultaneously optimizing two or more conflicting objectives subject to certain constraints. By using multi-objective optimization, it may bring some advantages in finding a valid and representative BP reference models compared with single objective problem.

This study presents a method of solving the multi-objective optimization problem by using forms of genetic algorithms. In multi-objective genetic algorithms we attempt to optimize not only one fitness parameter but also a collection of them. To achieve this, we generate a method of measuring the overall fitness of the set of objectives.

This paper is organized as follows. Section 2 discusses works related to this study. The proposed approach is described in Section 3. The result of experiments is presented in Section 4 and Section 5 concludes this study.

## 2. LITERATURE REVIEW

Many efforts have been made on BP modeling research and research on finding reference BP based on BP models is on the increase. van der Aalst *et al.* (2005) discussed configurable process models as a basis for reference modeling. Li *et al.* (2009) extended previous

research by proposing a heuristic approach to discovering reference models using a measurement to analyze the distance of change operations in modeling. It updates process configurations and produces new reference models based on a minimum edit distance from initial reference processes. A mathematical programming approach to discovering new reference models was introduced to address the issue of creating reference processes without initial reference information or process reconfiguration. There remain problems in the presentational and validation aspects of the process using interger programming formulations, which this study attempted to overcome with a genetic algorithm approach in (Yahya *et al.*, 2010).

Multi-objective genetic algorithms (MOGA) have been widely used in many areas including order allocation (Wu *et al.*, 2012), scheduling problem (Zinflou *et al.*, 2008; Minella *et al.*, 2008), human resource planning (Abboud *et al.*, 1998; Hajri-Gabouj, 2003) or design and planning problem (Zhou *et al.*, 2003; Gen *et al.*, 2009). Deb *et al.* (2002) used genetic algorithm to solve multi-objective problems and develop non-dominated sorting and further brought up the idea of using the elitist strategy may have a better convergence when using the genetic algorithm (GA). Research using GA on graph topology is limited to supply chain network (Wang *et al.*, 2010). Hence, this study proposes a novel approach on BP modeling domain.

In the domain of BP, Quan and Tian (2009) presented a research on business processes' multi-objective optimization to point out at three criteria of variables: processing time, process cost, and quality. The proposed research used simulation as the result experiments. Vergidis *et al.* (2006, 2007) carried out researches on BP improvement using multi-objective optimization and composite BP using an approach of evolutionary multi-objective optimization approach. Neubauer and Heurix (2008a, 2008b) discussed a case study a multi-objective decision support for defining secure BP. However, none of those studies point out variables related to the process structure behavior which is one of the important aspects on generating reference model.

## 3. PROPOSED APPROACH

### 3.1 Mixed-Integer Linear Programming Model

This section provides definitions of process model and structural schema to describe a formal model of BP.

#### Definition 1 (Process model).

We define a process model  $p^k$  as the  $k$ -th process in a process repository. It can be represented as a tuple of  $\langle A^k, L^k \rangle$ , each element of which is defined below.

- $A^k = \{a_i | i = 1, \dots, I\}$  is a set of activities where  $a_i$  is the  $i$ -th activity of  $p^k$  and  $I$  is the total number of activities in  $p^k$ .

- $\mathbf{A}$  is defined as a set of all activities in the process repository, where  $A$  is the union of all  $A^k$ ,  $\mathbf{A} = \bigcup_{k=1}^K A^k$
- $L^k \subseteq \{l_{ij} = (a_i, a_j) \mid a_i, a_j \in A^k\}$  is a set of links where  $l_{ij}$  is the link between two activities  $a_i$  and  $a_j$  in the  $k$ -th process. The element  $(a_i, a_j)$  represents the fact that  $a_i$  immediately precedes  $a_j$ .
- $a_{i+}$  is the activity following  $a_i$  and  $a_{i-}$  is the activity preceding  $a_i$
- $\mathbf{L}$  is a set of all links in the process repository, where  $\mathbf{L}$  is the union of all  $L^k$ ,  $k = 1, \dots, K$ , i.e.,  $\mathbf{L} = \bigcup_{k=1}^K L^k$
- For a split activity  $a_i$ , such that  $|N_i| > 1$ , where  $N_i = \{a_{j+} \mid (a_i, a_{j+}) \in L\}$ ,  $f(a_{i+}) = \text{'AND'}$  if all  $a_{i+}$  should be executed; otherwise,  $f(a_{i+}) = \text{'XOR'}$ .
- For a merge activity  $a_i$ , such that  $|M_i| > 1$ , where  $M_i = \{a_{j-} \mid (a_{j-}, a_i) \in L\}$ ,  $f(a_{i-}) = \text{'AND'}$  if all  $a_{i-}$  should be executed; otherwise,  $f(a_{i-}) = \text{'XOR'}$ .
- In order to collect information on the variety of start and end activities among process variants, we define  $\mathbf{A}_S$  and  $\mathbf{A}_E$  as the sets of start and end activities, respectively.
- $\mathbf{A}_S = \{a_i \mid a_i \in A^k, |M_i| = 0, \forall k \in K\}$  is a set of start activities in all  $K$  process variants where  $a_i$  is an activity in  $p^k$  with an empty set of preceding activities,  $|M_i| = 0$ .
- $\mathbf{A}_E = \{a_i \mid a_i \in A^k, |N_i| = 0, \forall k \in K\}$  is a set of end activities in all  $K$  process variants where  $a_i$  is an activity in  $p^k$  with an empty set of succeeding activities,  $|N_i| = 0$ .

**Definition 2 (Structural flow schema).**

A structural schema is a set of tuples, each of which has an index and link information. A structural schema ( $\mathbf{H}$ ) required for the chromosome generation is defined as

$$\mathbf{H} = \{(s, l_{ij}) \mid s = 1, 2, \dots, S, \text{ and } l_{ij} \in \mathbf{L}\}$$

The value of  $s$  will start from 1 and increase accordingly until all links are assigned. The value of  $s$  increases in different ways according to control flow types, sequential flow and split-merge flow. For each  $l_{ij}$  in a sequential flow, increasing number of  $s$  will be assigned, and each  $l_{ij}$  has a unique integer value of  $s$ . For all  $l_{ij}$ 's from a split activity or to a merge activity, a single value of  $s$  will be assigned.

**Index and subscript**

- $K$  : the number of process variants
- $k$  : process variant index,  $k = 1, \dots, K$
- $S$  : structural flow schema index,  $s = 1, \dots, S$
- $i, j, r, t$  : activity index

**Set**

- $p^k$  : process  $k$  in a process repository
- $A^k$  : a set of activities in process  $k$
- $L^k$  : a set of links in process  $k$
- $\mathbf{A}$  : a set of all activities in the process repository
- $\mathbf{A}_S$  : a set of start activities among  $K$  processes
- $\mathbf{A}_E$  : a set of end activities among  $K$  processes
- $\mathbf{L}$  : a set of all links in the process repository
- $\mathbf{H}$  : a set of structural flow schema in a group of process variants

- $\mathbf{P}_i$  : a set of immediately preceding activities (predecessors) of activity  $i$  in the process repository
- $\mathbf{S}_i$  : a set of immediately succeeding activities (successors) of activity  $i$  in the process repository

**Parameter**

- $C_i$  : expected cost to execute  $i$ -th activity
- $C_{ij}$  : proximity score for executing a link  $(a_i, a_j) (\in \mathbf{L})$
- $E_i$  : expected time to execute  $i$ -th activity
- $N_i$  : number of predecessors of  $i$ -th activity
- $M_i$  : number of successors of  $i$ -th activity
- $V_s$  : coordination time between activities in schemes.
- $W_s$  : average coordination time.  $W_s = V_s / \sum_{(s, l_{ij}) \in \mathbf{H}} 1$  (derived from average duration divided by number of links in one structural scheme)
- $M$  : big M, a very large positive
- $r_i$  : ready time for  $i$ -th activity
- $f_i$  : finish time for  $i$ -th activity. Particularly,  $f_i = r_i + E_i$

**Decision variable**

- $v_i$  : equals to 1 if activity is selected,  $a_i \in \mathbf{A}$ ; 0, otherwise
- $y_i$  : equals to 1 if activity  $a_i \in \mathbf{A}_S$  is a start activity and an element of the set of start activities; 0, otherwise
- $z_i$  : equals to 1 if activity  $a_i \in \mathbf{A}_E$  is an end activity and an element of the set of end activities; 0, otherwise
- $x_{ij}^s$  : equals to 1 if activity  $a_i$  immediately precedes activity  $a_j$  in scheme  $s$ ,  $(a_i, a_j) \in \mathbf{L}$ ,  $(s, l_{ij}) \in \mathbf{H}$ ; 0, otherwise

$$\min \sum_{(a_i, a_j) \in \mathbf{L}} \left[ (K - C_{ij}) \sum_{(s, l_{ij}) \in \mathbf{H}} x_{ij}^s + C_{ij} (1 - \sum_{(s, l_{ij}) \in \mathbf{H}} x_{ij}^s) \right] \quad (1)$$

$$\min C_{\max} \quad (2)$$

$$\min \sum_{i(a_i \in \mathbf{A})} C_i v_i \quad (3)$$

Note that a tri-objective integer programming model for generating a BP reference model is provided as an extension of a single objective problem. First, it attempts to find the maximum proximity score, (notice that it has been converted into a minimization problem), among the links existing in the process variants. The BP reference should satisfy the business requirements, which are defined as duration (2) and cost (3). Activity duration, called makespan, is a measure to evaluate the expected execution time of a BP reference model. In respect to cost, it will sum the costs of all selected activities for the best BP reference model.

In particular, the constraint can be decomposed into four segments; scheme (4)-(5), predecessors (6)-(9), successors (10)-(13), and predefined duration (14)-(16), respectively. Scheme constraint (4) specifies that a scheme behavioral relation of an activity should be less than or equal to 1. Among all structural schema relations, it sho-

uld be a scheme that is consistent with (5). With regard to predecessors, constraint (6) expresses that there should be at least one link entering activity  $i$  if activity  $i$  exists and activity  $i$  is not a start activity. To find a start activity, there should be a constraint to certify that there are no immediate predecessors to activity  $i$  (7). Certainly, activity consistency constraint (8) is necessary, that is, that an (start) activity is selected in the BP reference. In addition, we apply constraint (9) to specify that only an activity from a set of start activities ( $A_S$ ) can be a start activity, thereby restricting others (10).

Constraints

$$\sum_{s,j} x_{ij}^s \leq 1, \forall (s, l_j) \in \mathbf{H} \quad (4)$$

$$x_{ij}^s = x_{ji}^s, \forall s, (s, l_j), (s, l_i) \in \mathbf{H} \quad (5)$$

$$y_i + \sum_{s,j} x_{ji}^s \geq v_i, \forall a_i \in \mathbf{A}, (s, l_j) \in \mathbf{H}, N_i > 0 \quad (6)$$

$$N_i y_i + \sum_{s,j} x_{ji}^s \leq N_i v_i, \forall a_i \in \mathbf{A}, (s, l_j) \in \mathbf{H}, N_i > 0 \quad (7)$$

$$y_i = v_i, \forall a_i \in \mathbf{A}, N_i = 0 \quad (8)$$

$$\sum_i y_i = 1, \forall a_i \in A_S \quad (9)$$

$$\sum_i y_i = 0, \forall a_i \notin A_S \quad (10)$$

$$z_i + \sum_{s,j} x_{ij}^s \geq v_i, \forall a_i \in \mathbf{A}, (s, l_j) \in \mathbf{H}, M_i > 0 \quad (11)$$

$$M_i z_i + \sum_{s,j} x_{ij}^s \leq M_i v_i, \forall a_i \in \mathbf{A}, (s, l_j) \in \mathbf{H}, M_i > 0 \quad (12)$$

$$z_i = v_i, \forall a_i \in \mathbf{A}, M_i = 0 \quad (13)$$

$$\sum_i z_i = 1, \forall a_i \in A_E \quad (14)$$

$$\sum_i z_i = 0, \forall a_i \notin A_E \quad (15)$$

$$M(\sum_{s,j} x_{ij}^s - 1) + f_i + \sum_s W_s \sum_{s,r} x_{rs}^s \leq r_j, \forall (a_i, a_j) \in \mathbf{L}, (s, l_j), (s, l_r) \in \mathbf{H} \quad (16)$$

$$r_i + E_i = f_i, \forall a_i \in \mathbf{A} \quad (17)$$

$$f_i \leq C_{\max}, \forall a_i \in \mathbf{A} \quad (18)$$

$$x_{ij}^s \in \{0, 1\}, \forall (s, l_j) \in \mathbf{H} \quad (19)$$

$$v_i, y_i, z_i \in \{0, 1\}, \forall a_i \in \mathbf{A} \quad (20)$$

Subsequently, with regard to successors, constraint (11) expresses that there should be at least a link leaving activity  $i$  if activity  $i$  exists and activity  $i$  is not an end activity. To find an end activity, there should be a constraint to certify that there are no immediate successors to activity  $i$  (12). Certainly, we need to apply activity consistency constraint (13) to ensure that an (end) activity is selected in the BP reference. In addition, we set constraint (14) to specify that an activity can be an end activity only if it is from a set of end activities ( $A_E$ ), and restrict, thereby, others (15).

Constraints (16)-(19) relate to process duration. Constraint (16) denotes that the ready time of activity  $j$  should be greater or the same as the finish time of activity  $I$ , including the coordination time and the average duration that may occur during split or merge. Constraint

(17) defines the relations among ready time, execution time and finish time. Constraint (18) specifies the make-span. Constraint (19) ensures that the adjacent relationship of activities  $i$  and  $j$  includes a binary value element. Constraint (20) specifies that all activities (including start and end activities) has a binary value element.

### 3.2 Multiple-Objective BP Genetic Algorithm

This section proposes a solution to the BP reference selection problem, using a multi-objective genetic algorithm with maximizing proximity score measurement, cost minimization and duration minimization objectives (MOBPGA). MOBPGA considers four parameters, including generation size (*gen\_size*), population size (*pop\_size*), crossover rate ( $r_1$ ), and mutation rate ( $r_2$ ) (Gen and Cheng, 2000). The generation, denoted by  $t$ , represents the number of computation iterations of the GA. It contains a set of solutions that collectively corresponds to a population, denoted as  $P(t)$ . Chromosomes, which represent the solution, consist of genes that encode genotypes for evolution, and should be evaluated based on specific measures of fitness during each generation. In order to generate new offspring  $O(t)$ , a new generation of chromosomes, MOBPGA employs crossover and mutation operations.

#### Procedure: Multi-objective business process genetic algorithm (MOBPGA)

```

begin
    initialize  $P(t)$ ;
    evaluate  $P(t)$  based on the NSGAI;
    generate Pareto solutions;
    for  $t = 1$  to gen_size do
        recombine  $P(t)$  to yield  $O(t)$  based on the partial-mapped crossover and random key representation mutation;
        evaluate  $O(t)$  based on the NSGAI;
        update Pareto solutions;
        select  $P(t+1)$  from  $P(t)$  and  $O(t)$  based on the composite Pareto ranking selection (cPrs);
    end
end
    
```

The MOBPGA begins with initialization and ends when the number of run generations reaches the generation size. Following several generations of evolution, the algorithms improve solution quality and, in some cases, converge to the optimal solutions of the problem. Increasing the population size, generation size, crossover rate, or mutation rate explores more of the solution space while requiring greater computational effort. The final decision is made by the decision makers, who manually select the preferred Pareto solution according to their preference structures.

The proposed MOBPGA includes specific random key representation for encoding and decoding, partially mapped crossover, random key representation mutation,

an algorithm for efficient Pareto sorting (NSGAI), and composite Pareto ranking selection (cPrs) (Goldberg, 1989). Figure 1 shows the random key representation of encoding method used in this study.

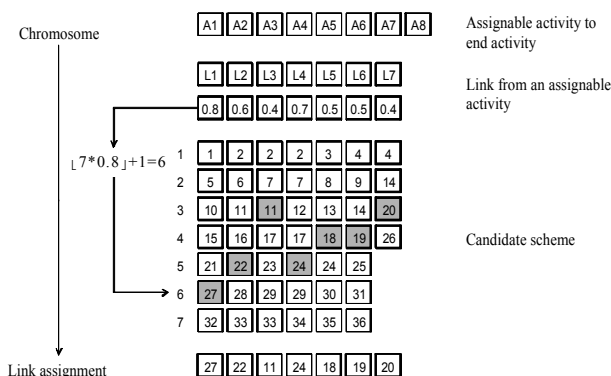


Figure 1. Random key representation encoding method.

Due to the random genetic processes (crossover and mutation) that might produce an invalid result, it is necessary to verify the process for further generation. We apply the soundness properties of business processes to verify the process well-formedness. For a business process model to be sound, three properties are required (van der Aalst, 2000): 1) for every activity  $a_j$  that is reachable from  $a_i$ , there exists a sequence to the next activity until a preferred end activity  $a_E$  is reached, 2) a preferred end activity  $a_E$  is the activity that should be reachable from a start activity  $a_S$ , and 3) there is no activity that is never processed in any execution of the model (there are no needless elements).

In order to generate a valid BP, there should be a decoding mechanism that follows some procedures. In this approach, there are three important mechanisms of decoding mechanism for establishing a valid BP. First, it checks the *start* and *end* activity. Second, it should check the *scheme* (mapping processes and links). Finally, it will check the path which contains candidate links. There are four steps to execute the decoding mechanism which is as follow.

- Step 1:** Disqualify schemes flowing to *Start* of flowing from *End*.
- Step 2:** Disqualify pair of activities that are not existed in the repository
- Step 3:** Disqualify activities that are not available in the path
- Step 4:** Restructure feasible activities and schemes

#### 4. EXPERIMENT RESULTS

In order to validate our approach, several experiments were conducted. The experiment estimates the validity of the proposed algorithm in real settings by using logistics processes that contain a various types of

process structure. Numerical analysis was performed on a desktop computer equipped with an Intel® Pentium® D 3.40GHz CPU and 2GB RAM. The commercial software LINGO 11.0 (LINGO System) was used to generate a reference set of non-dominated solutions, **R**, utilizing embedded integer programming (IP) packages. For each scenario, LINGO solved the weighted-sums problem with objectives (1)-(3) subject to (4)-(20), which was recognized as ILP (shown in Lingo) and terminated at local optimal solutions. For each problem instance, a local optimal solution was collected within various ranges of computation time. Hence, each scenario has a set of non-dominated solutions for further comparison. The performance metrics discussed above were used to compare the performances of MOBPGA and multi-objective mixed integer linear programming (MoMILP).

We conducted an experiment with various numbers of activities among four process groups (PG). Four groups from PG-I to PG-IV, each consisting of ten process variants ( $p_1-p_{10}$ ), were formed. Process variants are generated from a single process model, each of which fits a certain scenario and context; in other words, the configuration of a particular process variant reflects the specific requirement and circumstance of the process. The gradual increase in the number of activities of each process group is shown in Table 1. Since there is no exact cost and duration time data on our logistics process models, we express them using random integer values representing units of metric rather than real numbers for any currency or time.

Table 1. Mean number of activities in each group of 4 processes

Process group	PG-I	PG-II	PG-III	PG-IV
Mean no. of activities	6.1	10.4	14.8	19
Max no. of activities	7	11	15	20

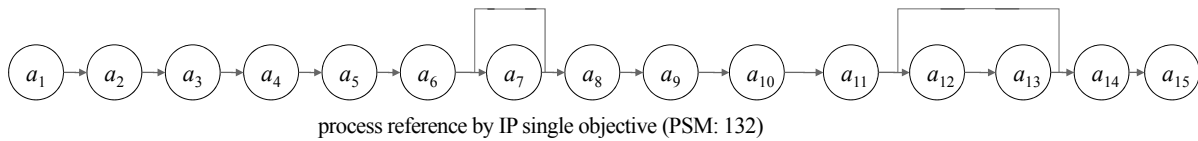
Based on our results using process group III (PG-III), the single-objective approach can produce only a single process reference model, with no guarantee of meeting some requirements (Figure 2). Our proposed approach has several alternatives for decision makers. For example, a process manager might want to select a BP reference model for duration of less than 30 units of time. Some of these alternative candidates are shown in Figure 3. The choice of generating given alternatives will correspond to the stakeholders' business requirements and will accrue benefits to business organizations in terms of strategic competitiveness.

When we applied process variants of activity number 20 (PG-IV), MoMILP computation time was intractable. Thus, we set a cut-off time of 21,600 seconds to obtain feasible solutions. The MOBPGA parameters operative were 1,000 generations, a population size of 20, a mutation rate of 0.8 and multiplier (set on 0.9) for the purpose of selection. Experiment result is shown in Table 2. The computational time of the approaches,

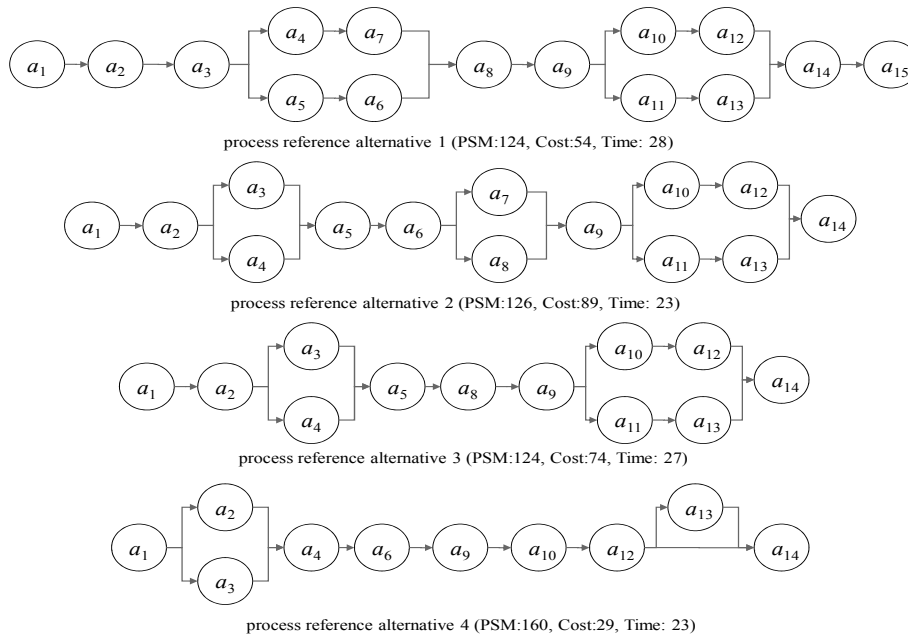
**Table 2.** Experiment result

	MoMILP			MOBPGA			Reference Pareto				MoMILP			MOBPGA			Reference Pareto		
	PSM	Cost	Time	PSM	Cost	Time	PSM	Cost	Time		PSM	Cost	Time	PSM	Cost	Time	PSM	Cost	Time
PG-I	46	22	35				46	22	35	PG-III	140	35	24				140	35	24
	48	12	22	47	34	46	48	12	22		142	59	21						
				51	12	24					142	35	34						
	54	10	21				54	10	21		144	58	23						
	56	12	19				56	12	19		144	50	26						
				57	21	13	57	21	13		144	37	28						
PG-II				57	10	21				144	34	40	144	34	40	144	34	40	
										144	37	18				144	37	18	
	61	36	35	61	36	35	61	36	35				146	53	24				
	65	33	31	65	33	31	65	33	31				148	55	18				
	65	36	29				65	36	29				148	48	25				
	69	33	25				69	33	25				150	46	23				
				75	48	27							154	42	26				
				79	45	23	79	45	23				154	33	33	154	33	33	
	81	33	22				81	33	22				156	44	20				
	81	28	54				81	28	54				156	35	27				
107	36	19				107	36	19				158	37	15					
			117	72	22							158	29	30	158	29	30		
			114	87	54	114	87	54											
			116	99	42	116	99	42											
			116	83	44	116	83	44				160	38	23					
			116	78	46	116	78	46	160	29	23				160	29	23		
			116	69	52	116	69	52											
			118	78	35	118	78	35				162	40	17					
			118	74	47	118	74	47				162	31	24					
			118	65	55	118	65	55	164	31	17				164	31	17		
			120	69	30	120	69	30				158	58	99	158	58	99		
			120	60	35	120	60	35				162	76	88	162	76	88		
			122	68	32	122	68	32				166	71	83	166	71	83		
			122	59	39	122	59	39				168	67	87	168	67	87		
122	54	41				122	54	41				168	56	102	168	56	102		
			124	74	27	124	74	27				170	68	83	170	68	83		
124	54	28				124	54	28				170	56	94	170	56	94		
			126	89	23	126	89	23				172	52	93	172	52	93		
			126	69	28				172	52	106								
			126	56	30														
126	54	25				126	54	25				174	106	77	174	106	77		
126	45	29				126	45	29				174	76	79	174	76	79		
			128	55	40							176	91	77	176	91	77		
128	45	23				128	45	23				180	67	81	180	67	81		
			130	74	24							180	56	92	180	56	92		
			132	67	25							182	84	73	182	84	73		
			132	51	36							182	61	82	182	61	82		
			132	48	61							182	50	83	182	50	83		
			134	65	26							184	83	72	184	83	72		
			134	50	43							184	62	78	184	62	78		
			134	44	49							186	104	66	186	104	66		
134	41	20										186	79	76	186	79	76		
			136	59	28							186	68	77	186	68	77		
			136	55	35							188	68	66					
			136	39	37	136	39	37	188	50	58				188	50	58		
			138	63	24							192	59	80					
			138	62	26							200	98	65					
			138	54	29				200	50	50				200	50	50		
			138	41	31							204	65	77					
			138	38	49							204	53	80					
138	35	30				138	35	30				206	55	79					
			140	108	20	140	108	20	206	56	45				206	56	45		
			140	57	27	140	57	27	210	56	45				220	101	62		
												220	101	62	220	101	62		
									226	47	99				226	47	99		

PG: process group, PSM: proximity score measurement, MoMILP: multi-objective mixed integer linear programming, MOBPGA: multi-objective business process genetic algorithm.



**Figure 2.** Generated process reference model using genetic algorithm approach (Yahya *et al.*, 2010).  
 PSM: proximity score measurement.



**Figure 3.** Some alternatives of process reference considering time <30.  
 PSM: proximity score measurement

MoMILP and MOBPGA, are listed in Table 3. MoMILP sets a cut-off time of 21,600 seconds for feasible solutions, compared with MOBPGA’s 222 seconds for an activity number of 20. Finally, the performance of the MOBPGA is robust and our performance evaluations showed little difference from MoMILP in terms of quality of the solutions.

**Table 3.** Performance evaluations of three scenarios using MoMILP and MOBPGA

Scenario	Max no. activities	Method	RT(sec)
PG-I	7	MoMILP	6.0
		MOBPGA	3.7
PG-II	11	MoMILP	107.0
		MOBPGA	13.8
PG-III	15	MoMILP	2,674.0
		MOBPGA	140.1
PG-IV	20	MoMILP	21,600.0
		MOBPGA	222.0

PG: process group, MoMILP: multi-objective mixed integer linear programming, MOBPGA: multi-objective business process genetic algorithm.

## 5. CONCLUSION

This paper proposes a MOBPGA with specific random key representation of encoding and decoding to solve the problem of BP reference model generation with objective functions maximizing process proximity while minimizing cost and duration. The proposed model meets customer requirements by coordinating objectives, specifically by incorporating the process topology into the operational objectives. It also presents a compromise approach that can facilitate decision making in the context of a large set of Pareto solutions, thereby enabling decision makers to incorporate other preferences or business concerns. By utilizing the results of non-dominated solutions both from MOBPGA and MoMILP, we can suggest alternative solutions to stakeholders based on certain conditions. Compared with the conventional approach, this provides more solutions to decision makers, enabling them to select process reference models based on their requirements.

BP reference model generation will have to be improved, considering the following limitations. First, this study employed experiments using the block concept of process structure. Whereas there are some benefits on the experiments, this approach covers a little issue with

regard to deadlock and flawless process in BP. Moreover, there are some issues remaining with regard to operation dependency within activities. Second, since the graph generation was assumed to be flawless, there is a need to carefully consider the control flow semantics such as AND or OR control-flow in generating the BP reference model. These are issues that will require further research.

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