Fractal analysis of mandibular trabecular bone: optimal tile sizes for the tile counting method

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ABSTRACT

Purpose : This study was performed to determine the optimal tile size for the fractal dimension of the mandibular trabecular bone using a tile counting method.

Materials and Methods : Digital intraoral radiographic images were obtained at the mandibular angle, molar, premolar, and incisor regions of 29 human dry mandibles. After preprocessing, the parameters representing morphometric characteristics of the trabecular bone were calculated. The fractal dimensions of the processed images were analyzed in various tile sizes by the tile counting method.

Results : The optimal range of tile size was 0.132 mm to 0.396 mm for the fractal dimension using the tile counting method. The sizes were closely related to the morphometric parameters.

Conclusion : The fractal dimension of mandibular trabecular bone, as calculated with the tile counting method, can be best characterized with a range of tile sizes from 0.132 to 0.396 mm. (*Imaging Sci Dent 2011; 41 : 71-8*)

KEY WORDS : Fractals; Dental Digital Radiograph; Trabecular Meshwork

Introduction

Since Mandelbrot announced the concept of the fractal geometry,¹ fractal analysis has been adapted to study the various natural structures and biosignals. It has been used to interpret and express such biological phenomena as arterial trees,² nervous system,³ electric conductivity of heart,⁴ and EEG.⁵ In the field of dentistry, there have been many attempts to analyze and predict the structure of jaw trabecular bone using the fractal analysis for the evaluation of osteoporosis⁶⁻¹⁴ and for the detection of the periodontal disease.^{15,16} Fractal analysis of the bone trabecular struc-

Department of Oral and Maxillofacial Radiology, School of Dentistry, Seoul National University, 275-1 Yeongeon-dong, Jongno-gu, Seoul 110-768, Korea Tel) 82-2-2072-3049, Fax) 82-2-744-3919, E-mail) wjyi@snu.ac.kr ture has proven to be efficient in analyzing the bone quality in clinical applications.^{17,18}

Tile-counting method has been commonly used for the fractal analysis of the jaw bone trabecular structure,^{6,10,19-21} which was not a true fractal object but natural structure. The fractal dimensions from the jaw bone show variations according to the interpretation of results from the tile counting method. One of the reasons might be that selecting the range of tile sizes greatly could influence on the final fractal dimension. Therefore, it is important to determine the optimal range of tile size in order to obtain a more truthful fractal dimension of the natural structure. A proper range of scales was suggested to analyze the trabecular structure in the histological section of cancellous bone.²²⁻²⁹ The purpose of this study was to determine the optimal range of tile size in using the tile-counting method for radiographs of the human jaw bone.

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Materials and Methods

Acquisition of digital radiographs

The digital radiographs were acquired using a Heliodent DS intraoral X-ray system (Sirona Dental System Gmbh, Bensheim, Germany) and a direct imaging sensor (Schick Technologies Inc, Long Island, NY, USA). They were taken

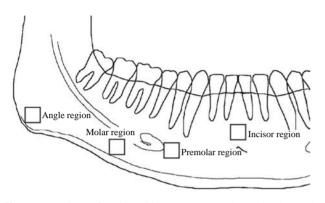


Fig. 1. Locations of region of interest (ROI) selected in the angle, the molar, the premolar and incisor regions.

from 29 human dry mandibles without any disease. Each mandible was fixed using a special positioning device. Buccal cortex was located perpendicular to the central ray and the distance between X-ray source and buccal cortex was fixed at 40 cm. The digital imaging sensor was placed under the mandible and parallel with the buccal cortex. The images were acquired from the angle, molar, and premolar regions on both sides and an incisor region of the mandible (Fig. 1). The images were taken using the system setup with cone operating at 70 kVp, 7 mA and with exposure time of 0.24 seconds for the angle regions, 0.36 for the molar, 0.24 for the premolar and 0.16 for the incisor. A total of 203 digital images (29 mandibles × 3 regions × 2 sides and 29 mandibles \times 1 region) with 862 by 574 pixels of 256 gray levels were analyzed. Each pixel size equated to $41.4 \,\mu\text{m}$ and $47.6 \,\mu\text{m}$, respectively.

Preprocessing of images and calculation of morphometric parameters

Four regions of interests (ROIs) as a rectangular window were established in the identical anatomic locations for

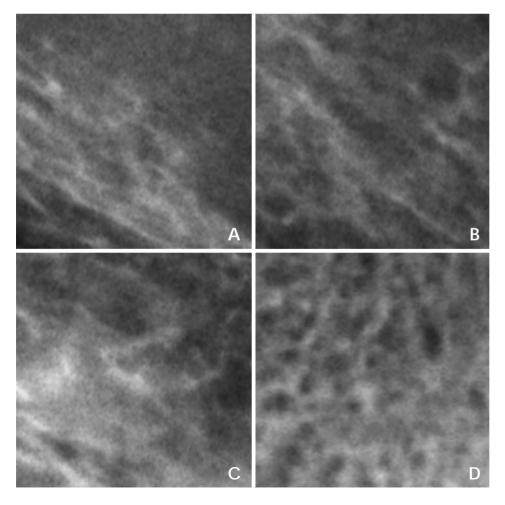


Fig. 2. The images of ROI show the trabecular bone structure. A. Mandibular angle region, B. Mandibular molar region, C. Mandibular premolar region, D. Mandibular incisor region.

all mandibles. The ROI was set adjacent to the inferior cortex of the mandibular angle for the angle region, to the inferior cortex under the first molar for the molar, to the medial side of mental foramen for the premolar, and above the mental ridge for the incisor region (Fig. 2).

A macro codes for the image analysis was developed for this study using Scion Image, an application program for image processing (Scion Corp, Frederick, Maryland, USA). To extract the trabecular bone patterns, the ROI image was first made binary using the algorithm described by Geraets et al^{30,31} and White et al.³² The image was blurred using a Gaussian filter to remove large-scale variations on the image. The blurred image (low-pass filtered image) was then subtracted from the original image, and 128 gray levels were added to each pixel of the subtraction image. The binary image was obtained by thresholding on a gray level of 128, which segmented the image into the bone (gray level of 255) and marrow (gray level of 0). The outline and skeletonized image were extracted from the binary image by mathematical morphologic operators.

Four morphometric parameters were calculated to represent the structural characteristics of the trabecular bone, which were bone area, length of skeletal structure, mean length of branch, and mean trabecular thickness. The number of black pixels in the binary image was regarded as the bone area. The length of skeletal structure was defined as the number of black pixels in the skeletonized image. From the skeletonized image, the nodes and terminals were found using a kernel of 3 by 3 pixels. The pixel with more than 3 branches was regarded as a node and the pixel with one branch as a terminal. The mean length of branches was calculated from the branches having a nod and a terminal at their ends. Mean trabecular thickness was obtained as the bone area divided by the length of skeletal structure.

Fractal dimension by modified tile counting method

The fractal dimension (FD) by tile counting method can be obtained by the classical fractal geometry theory. In the modified tile counting method, the number *N* of tiles containing any part of the structure is related to the edge length of the tile (ϵ) or scale (Eq. 1).³⁰ A straight line (Richardson plot) is obtained by taking the logarithm of *N* versus the logarithm of the inverse scale (1/ ϵ). The slope (*D*) of the linear portion of the curve is determined to the FD (Eq. 2). This FD gives the fractal information reflecting the spatial characteristics of the trabecular bone. The thickness of the tile edges is set to zero so that none of the pixels forming the structure are obscured by the edge lines.

$$N(\varepsilon) \propto \varepsilon^{-D} \tag{1}$$

$$\log N(\varepsilon) = D \log (1/\varepsilon) + c \tag{2}$$

This study applied the tile counting method to the outline image using the edge length of the tile from 1 to 49 pixels. The results were analyzed by SPSS program (ver. 8.0, SPSS Inc, Chicago, IL, USA) using the following statistics. The ANOVA test was performed among the local slopes of the Richardson plot for four anatomical regions. The bivariate correlation test was also performed between local slopes in various ranges of tile sizes.

Results

Four ROIs as 180 by 180 pixels (7.92 by 7.92 mm) were extracted in the identical locations for all mandibles (Fig. 1). Fig. 2 represents the examples of the ROI image from the four regions. These images were blurred with a Gaussian filter with a sigma of 10 pixels and a kernel size of 31 by 31 pixels. The outline and skeletonized image for fractal analysis were obtained by the mathematical morphologic operators (Fig. 3).

Fig. 4 shows the mean Richardson plots after applying the tile counting method to the outline images using the edge length of the tile from 1 to 49 pixels. This represents the mean number of the tiles containing any part of the outline against the edge length of the tile in 4 anatomical regions. All Richardson plots show lines with a little curvature. They present relations between the size of bone trabecular structure and the edge length of tiles. The selected tile sizes from 1 to 49 pixels were sufficient to provide the fractal dimension of the trabecular structure from the ROI of 180 by 180 pixels.

In large tile sizes, the Richardson plots show the line with a slope of 2 as all the tiles contain any part of the outline. The resultant data from this range do not contain any information about the bone trabecular structure. When the tile size was larger than 13 pixels (range (A) in Fig. 4), the number of tiles containing the outline coincided with the total number of tiles. Therefore, the slopes of Richardson plots for tile sizes not larger than 13 pixels were considered for analysis. We divided it into 6 ranges of scales 1-3, 3-5, 5-7, 7-9, 9-11, and 11-13 pixels (range (B) in Fig. 4) for the sake of convenience. When all the ranges are considered, the same result will be obtained as in Richardson plots in Fig. 4.

Fig. 5 shows the box plots of the local slopes for the ranges. The ANOVA test for 4 anatomical regions was per-

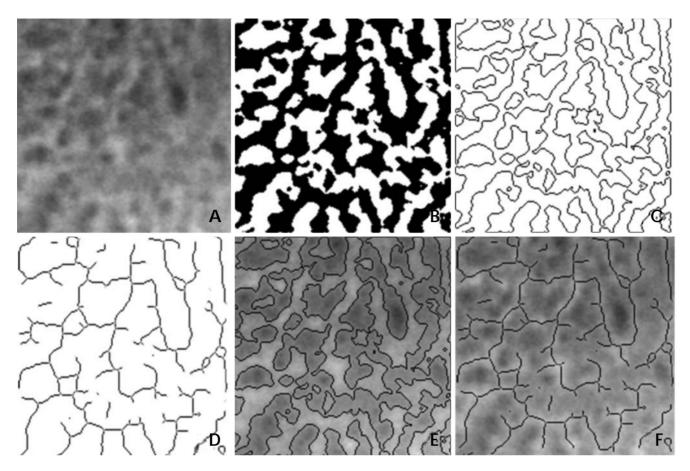


Fig. 3. Image processing procedures. A. Raw image before processing, B. Binary image, C. Outline image, D. Skeletonized image after preprocessing, E. Composition image of raw and outline images, F. Composition image of raw and skeletonized images.

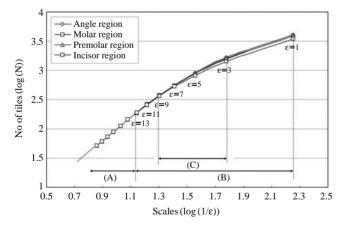


Fig. 4. Mean number of tiles containing any part of the outline against the edge length of the tile or scale from 1 to 49 pixels in 4 anatomical regions. A. A range of scales with local slope of two, B. A range of scales considered for analysis, C. A determined range of scales significant for the fractal dimension.

formed among the local slopes in all the ranges considered. In 3 ranges of 3-5 to 7-9 pixels (range (C) in Fig. 4), the slopes of the angle and the incisor region respectively showed statistically significant differences with the molar and premolar region (p < 0.05). In all ranges, the slopes between the molar and premolar regions did not show any statistically significant difference.

Theoretically, the Richardson plot exhibits a perfect straight line in all ranges of scales. In the ranges, the local slopes must show a positive correlation between ranges. The slopes from these ranges provide the fractal dimension which is significant in finding out the structures of the trabecular bone. We performed the bivariate correlation tests between local slopes in various ranges of scales. The Pearson correlation value between local slopes was over 0.5 in 3 ranges of 3-5 to 7-9 pixels in Table 2. From these results, the range of scales significant for the fractal dimension was determined as ranges from 3 pixels (0.132 mm) to 9 pixels (0.396 mm). The upper level of the scales was very similar to the mean trabecular thickness (9.25 pixels). The means of morphometric parameters from 203 ROIs are summarized in Table 1.

In the range of 3-9 pixels, the fractal dimensions for the 4 anatomical regions were calculated by a linear regression.

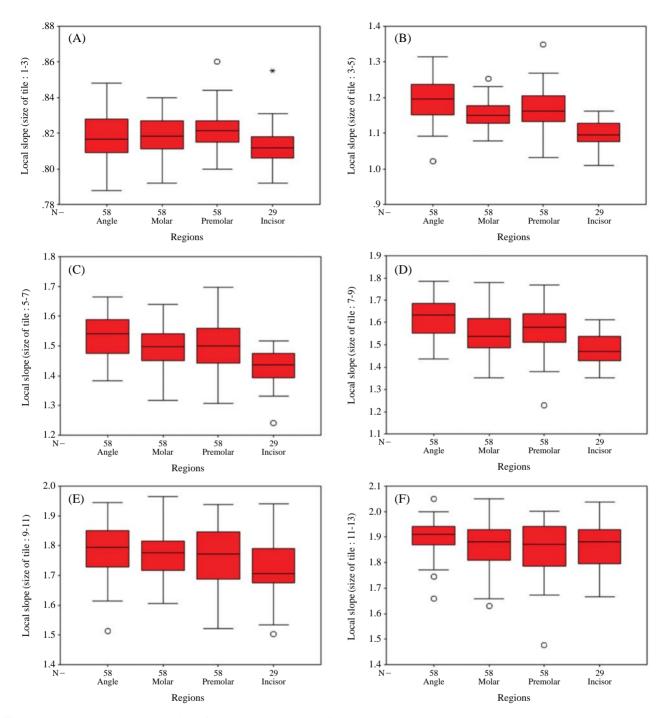


Fig. 5. Box plots show the distribution of local slopes in ranges of scales. A. 1 to 3 pixels, B. 3 to 5 pixels, C. 5 to 7 pixels, D. 7 to 9 pixels, E. 9 to 11 pixels, F. 11 to 13 pixels. No significant differences among the regions in slopes of 1-3, 9-11, and 11-13. There are significant differences among the regions in slopes of 3-5, 5-7, and 7-9 (p < 0.05).

The dimensions of the trabecular bone structure were 1.45 ± 0.05 at the angle, 1.40 ± 0.06 at the molar, 1.42 ± 0.07 at the premolar, and 1.34 ± 0.04 at the incisor region. The angle and the incisor region showed statistically significant difference with the molar and premolar region (p<0.05). However, the fractal dimensions between the molar and premolar region showed no statistically significant difference with the molar statistically significant difference with the molar and premolar region (p<0.05).

ence. The angle region showed significantly the largest fractal dimension and the incisor region showed the least. This is caused by the different bone trabecular structure at each region. It can be verified by the examples of the ROI image from the 4 regions in Fig. 2. The image of an angle region shows a thin and complex trabecular structure (Fig. 2A). On the other hand, the incisor region shows a thick

 Table 1. Means of morphometric parameters extracted from ROIs

 of 180 by 180 pixels (7.92 by 7.92 mm) established in four anatomic regions

Brightness	130±28 gray level
Bone area	16,463±760 pixels
Length of skeletal structure	$1,808 \pm 258$ pixels
Mean length of branch	12.2 ± 1.7 pixels
Mean trabecular thickness	9.3 ± 1.1 pixels

Table 2. Bivariate correlation tests between local slopes of Richard-
son plot in various ranges of scales. Pearson correlation is over 0.5
in 3 ranges of 3-5, 5-7 and 7-9 pixels showing strong linear cor-
relations (indicated by *)

Scales (pixels)	1-3	3-5	5-7	7-9	9-11	11-13
1-3	1.000	0.242	0.309	0.116	-0.029	0.081
3-5		1.000	0.568*	0.543*	0.234	0.125
5-7			1.000	0.547*	0.268	0.118
7-9				1.000	0.021	0.222
9 - 11					1.000	0.222
11-13						1.000

and simple trabecular structure (Fig. 2D). The molar and the premolar region are in the middle of the two (Figs. 2B and C). This difference in the shape of trabecular structure is related with physical properties of the bone.

Discussion

Fractal dimension of the trabecular bone structure has been proven to have evident correlation with the physical property of the bone in many studies.⁶⁻²³ However, the fractal dimensions from these studies showed large variations even in the same anatomical region as in the jaw bone of 1.26 to 2.682.^{12-14,17,20,30} These variations were mainly caused by the problems of the fractal analysis itself rather than by different materials used in each study. Cha et al¹⁹ and Geraets et al³⁰ mentioned that 'different method', 'fitting a straight line', 'noise sensitivity' and 'standardization of filming method and exposure' were the problems in applying the fractal analysis to clinical applications. The problem of 'fitting a straight line' is caused by selecting the proper range of scales providing data for the least squares of the linear regression. True fractal objects have the property of self-similarity over all possible range of scales. On the other hand, natural fractal structures show the self-similarity in a limited range of scales. As a result, the Richardson plot represents a true slope or fractal dimension in the specified ranges of scales. Paumgartner et al,²² Caligiuri et al,²³ and Parkinson et al²⁴ stated that even though the

natural structure had the fractal characteristics, it was not true mathematical fractal geometry but it well conformed with the fractal behavior in the specific range of scales. Eventually, the Richardson plot from the natural structure showed straight line only in one or some of specific range of scales. The range exhibiting true self-similarity was influenced by the structural and functional properties of the analyzed structure.

It is imperative to determine the range of scales showing the true fractal dimension in the Richardson plot. In our results, the Richardson plots showed the lines with a little curvature over the scales considered. In the lower ranges of scales, the true fractal dimension was subjected to restriction by the limitation of resolution and increased influence of high frequency noise. In the higher ranges, it was influenced by the rough structural features of the object. As all the tiles would contain any part of the outline in the higher ranges, the slopes of Richardson plot converge on 2 gradually. In this study, all the tiles with the scale of over 13 pixels contained any part of the outline. Therefore, the local slopes from the scales of 1 to 13 pixels were analyzed. In the range of scales from 3 to 9, the slopes of the angle and the incisor region showed statistically significant differences with the molar and premolar region. In the correlation test between the local slopes of various scales, only those from the scales of 3 to 9 pixels represented values over 0.5. Finally, we determined the significant upper level of the scale as 0.396 mm (9 pixels), the lower level as 0.132 mm (3 pixels), and the range as 0.308 mm (7 pixels) to provide the fractal dimension in finding out the structures of the trabecular bone. The scales determined as significant are closely related to the morphometric parameters. The mean length of branch of 12.2 ± 1.71 pixels almost coincides with the maximum scale at which the number of tiles containing any part of the outline differs from the total number of tiles. The mean trabecular thickness of 9.3 ± 1.1 pixels almost coincides with the significant upper level of scales.

In a study of histological sections of the trabecular bone, Parkinson et al²⁴ suggested three sectional fractal dimensions for the trabecular bone, which was multifractal as fractal one, two, and three. The fractal one was estimated from tile sizes ranging from 0.025 to 0.15-0.35 mm, the fractal two from 0.15-0.35 to 0.5-1 mm, and the fractal three from 0.5-1.0 to 4.25 mm. The range of the fractal one encompassed the size range of resorption pits. The dimension of the fractal one described the surface texture of individual trabeculae. The range of fractal two encompassed the size range of individual trabecular elements, and this fractal described the shape or form of trabeculae. The range of fractal three encompassed several structural units of the cancellous architecture, and this fractal described the overall spatial arrangement of cancellous bone. The significant range of scales by ours conforms partly to those of the fractal one and two respectively, although our object of study (from jaws) was different from that by Parkinson et al (from femoral head and iliac crest). The shape of the trabecular bone structure has been known to be different according to the anatomical regions. The fractal dimension from the significant range of scales can describe more exactly the shape of trabeculae in the jaw bone from digital intraoral radiographs.

In the image processing for fractal analysis, it is important to remove the low frequency noise from the radiographs. The mandible regions are surrounded by cortical bone and soft tissue with various thicknesses. They influence the mean gray level significantly and exhibit a low frequency noise. To remove the noise, we subtracted the blurred image obtained by Gaussian filtering, a kind of low pass filtering, from the original image. If the sigma value (standard deviation) of Gaussian filer increases, more of low frequency noise is removed from the image. The proper sigma value of Gaussian filter may differ according to the image resolution, size of object to be analyzed, or quality and quantity of the noise. After adding 128 gray levels to the subtraction image, a standardized image was obtained for the fractal analysis.

In dental clinics, the fractal analysis of trabecular bone structure of jaws using digital intraoral radiographs can be used in evaluating pathological bone change and preimplant bone quality. It can be an inexpensive and convenient screening tool for the diagnosis of general diseases accompanying various bone changes. The important prerequisites for fractal analysis are to standardize the acquisition and processing of images and to determine the fundamental and significant range of scales in the Richardson plot. We determined the significant range of scales for the fractal dimension to describe more exactly the shape of trabeculae in the jaw bone from digital intraoral radiographs processed by the automated image processing.

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