

## Password-Based Key Exchange Protocols for Cross-Realm\*

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### *Cross-Realm* 환경에서 패스워드기반 키교환 프로토콜

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#### 〈Abstract〉

Authentication and key exchange are fundamental for establishing secure communication channels over public insecure networks. Password-based protocols for authenticated key exchange are designed to work even when user authentication is done via the use of passwords drawn from a small known set of values. There have been many protocols proposed over the years for password authenticated key exchange in the three-party scenario, in which two clients attempt to establish a secret key interacting with one same authentication server. However, little has been done for password authenticated key exchange in the more general and realistic four-party setting, where two clients trying to establish a secret key are registered with different authentication servers. In fact, the recent protocol by Yeh and Sun seems to be the only password authenticated key exchange protocol in the four-party setting. But, the Yeh-Sun protocol adopts the so called "hybrid model", in which each client needs not only to remember a password shared with the server but also to store and manage the server's public key. In some sense, this hybrid approach obviates the reason for considering password authenticated protocols in the first place; it is difficult for humans to securely manage long cryptographic keys. In this work, we introduce a key agreement protocol and a key distribution protocol, respectively, that requires each client only to remember a password shared with its authentication server.

Key Words : Key exchange, Authentication, Password, Public key, Cross-realm

## I. 서론

Password-based protocols for authenticated key

exchange are designed to work even when user authentication is done via the use of passwords drawn from a small known set of values. There have been many protocols proposed over the years for password authenticated key exchange in the three-party scenario, in which two clients attempt to establish a secret key

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interacting with one same authentication server [1, 13, 15, 17, 19]. However, little has been done for password authenticated key exchange in the more general and realistic four-party setting, where two clients trying to establish a secret key are registered with different authentication servers [12, 21]. In fact, the recent protocol by Yeh and Sun seems to be the only password authenticated key exchange protocol in the four-party setting [20]. But, the Yeh-Sun protocol adopts the so called “hybrid model”, in which each client needs not only to remember a password shared with the server but also to store and manage the server’s public key [10]. In some sense, this hybrid approach obviates the reason for considering password authenticated protocols in the first place; it is difficult for humans to securely manage long cryptographic keys. In this work, we propose new protocols designed carefully for four-party password authenticated key exchange that requires each client only to remember a password shared with its authentication server.

From the viewpoint of the session key creation, key exchange protocols can be broadly subdivided into two categories: key distribution protocols and key agreement protocols. In key distribution protocols (e. g., “Star Based System” of [6]), the session key is created by one party and securely transmitted to other parties. In key agreement protocols, more than one party contributes information to generate the common session key. In this paper, we introduce a key agreement protocol [16] and a key distribution protocol, respectively.

The rest of this paper is organized as follows. We begin by setting up some notation and definitions in Section 2. We continue in Section 3 with the description of our proposed four-party password authenticated key

agreement protocol [16] and analyze the security of the proposed protocol. Then in Section 4, we present the description and the security analysis of the proposed password authenticated key distribution protocol. Finally, we conclude this work in Section 5.

## II. Protocol Preliminaries

We begin with the requisite definitions. There are four entities involved in the protocol: two clients  $A$  and  $B$ , and two authentication servers  $SA$  and  $SB$  respectively of  $A$  and  $B$ . We denote by  $IDA$ ,  $IDB$ ,  $IDSA$ , and  $IDSB$ , the identities of  $A$ ,  $B$ ,  $SA$ , and  $SB$ , respectively.

### 2.1 Computational Diffie–Hellman (CDH) Assumption.

Let  $g$  be a fixed generator of the finite cyclic group  $Z_p^*$ . Informally, the CDH problem is to compute  $gab$  given  $ga$  and  $gb$  where  $a$  and  $b$  were drawn at random from  $\{1, \dots, |Z_p^*|\}$ . Roughly stated,  $Z_p^*$  is said to satisfy the CDH assumption if solving the CDH problem in  $Z_p^*$  is computationally infeasible for all probabilistic polynomial time algorithms.

### 2.2 Symmetric Encryption Scheme.

A symmetric encryption scheme is a triple of polynomial time algorithms  $\Gamma = (K, e, D)$  such that:

- The key generation algorithm  $K$  is a randomized algorithm that returns a key  $k$ . Let  $\text{Keys}(\Gamma)$  be the set of all keys that have non-zero probability of

being output of  $K$

- The encryption algorithm  $E$  takes as input a key  $k \in Keys(\Gamma)$  and a plaintext  $m \in \{0, 1\}^*$ . It returns a ciphertext  $e_k(m)$  of  $m$  under the key  $k$ . This algorithm might be randomized or stateful.
- The deterministic decryption algorithm  $D$  takes as input a key  $k \in Keys(\Gamma)$  and a purported ciphertext  $c \in \{0, 1\}^*$ . It returns  $D_k(c)$ , which is a plaintext  $m \in \{0, 1\}^*$  or a distinguished symbol  $\perp$ . The return value  $\perp$  indicates that the given ciphertext  $c$  is invalid for the key  $k$ .

We say, informally, that a symmetric encryption scheme  $\Gamma$  is secure if it ensures confidentiality of messages under chosen-ciphertext attack (CCA) and guarantees integrity of ciphertexts [18]. As shown in [2, 14], this combination of security properties implies indistinguishability under CCA which, in turn, is equivalent to non-malleability [9] under CCA.

### 2.3 Signature Scheme.

A digital signature scheme is a triple of algorithms  $\Sigma = (\varsigma, S, V)$  such that:

- The probabilistic key generation algorithm  $G$  on input a security parameter  $1^l$ , outputs a pair of matching public and private keys  $(PK, SK)$ .
- The signing algorithm  $S$  is a probabilistic polynomial time algorithm that, given as input a message  $m$  and a key pair  $(PK, SK)$ , outputs a signature  $\sigma$  of  $m$ .

- The verification algorithm  $V$  is a polynomial time algorithm that on input  $(m, \sigma, PK)$ , outputs 1 if  $\sigma$  is a valid signature of the message  $m$  with respect to  $PK$ , and 0 otherwise.

We say that a signature scheme  $\Sigma$  is secure if the probability of succeeding with an existential forgery under adaptive chosen message attack [11] is negligible for all probabilistic polynomial time attackers.

### 2.4 Initialization.

During some initialization phase, two servers  $SA$  and  $SB$  agree on the following public parameters: a large prime  $p$ , a generator  $g$  of  $Z_p^*$  satisfying the CDH assumption, a one-way hash function  $H$ , a secure symmetric encryption scheme  $\Gamma = (K, \varepsilon, D)$ , and a secure signature scheme  $\Sigma = (\varsigma, S, V)$ . In addition, public/private key pairs are generated for each server by running the key generation algorithm  $\varsigma(1^l)$ . We denote by  $(PK_X, SK_X)$  the public/private keys of the server  $X$  for  $X \in \{SA, SB\}$ . As part of the initialization, the client  $A$  (resp.  $B$ ) registers with server  $SA$  (resp.  $SB$ ), by choosing  $PW_A$  (resp.  $PW_B$ ) and sending it to the server via a secure channel.

## III. A Four-party Password Authenticated Key Agreement Protocol(PAKA)

In this section we present a new four-party password authenticated key agreement protocol PAKA [16] in which two clients wishing to agree on a session key do not need to store any public key of their authentication server but only need to share a short,

easy-to-remember password with the server. In describing the protocol PAKA, we will omit ‘mod  $p$ ’ from expressions for notational simplicity. The PAKA protocol is outlined in <Fig. 1> and a more detailed description is as follows:

### 3.1 Description of PAKA Protocol

**Step 1.** Two clients  $A$  and  $B$  first need to inform each other of their respective authentication server. To this end,  $A$  sends to  $B$  the message  $\langle ID_A, ID_{SA}, ID_B \rangle$  and  $B$  sends to  $A$  the message  $\langle ID_B, ID_{SB}, ID_A \rangle$ .

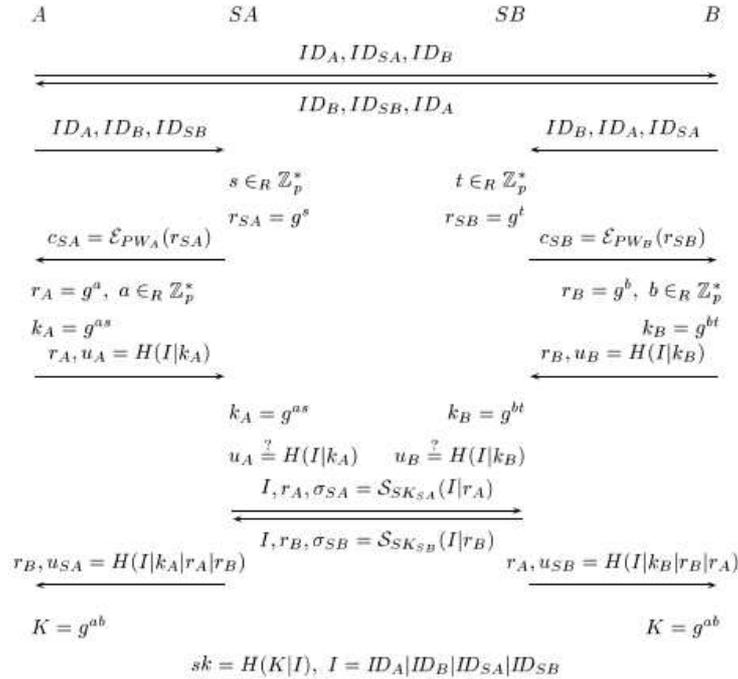
**Step 2.** The clients request the assistance of their respective server in establishing a session key between them. Client  $A$  (resp.  $B$ ) does this by sending the

message  $\langle ID_A, ID_B, ID_{SB} \rangle$  (resp.  $\langle ID_B, ID_A, ID_{SA} \rangle$ ) to the server  $SA$  (resp.  $SB$ ).

**Step 3.** Server  $SA$  chooses a random number  $s \in R Z_p^*$ , computes  $r_{SA} = g^s$  and  $c_{SA} = \mathcal{E}_{PW_A}(r_{SA})$ , and sends the ciphertext  $c_{SA}$  to  $A$ . Similarly, server  $SB$  chooses a random number  $t \in R Z_p^*$ , computes  $r_{SB} = g^t$  and  $c_{SB} = \mathcal{E}_{PW_B}(r_{SB})$ , and sends the ciphertext  $c_{SB}$  to  $B$ .

**Step 4.** After receiving  $c_{SA}$  client  $A$  recovers  $r_{SA}$  by decrypting  $c_{SA}$  i. e.,  $r_{SA} = DPWA(c_{SA})$ , and chooses a random number  $a \in R Z_p^*$ . Given  $r_{SA}$  and  $a$ , client  $A$  computes the one time key  $k_A$  to be shared with the server  $SA$  as

$$k_A = g^{as} = (r_{SA})^a.$$



<Fig. 1> Four-party password authenticated key agreement protocol

Additionally,  $A$  computes  $r_A = g^a$  and  $u_A = H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_A)$ . Then  $A$  sends the message  $\langle r_A, u_A \rangle$  to the server  $SA$ .

Meanwhile, client  $B$ , having received  $c_{SB}$ , computes  $r_{SB} = D_{PW_B}(c_{SB})$  and chooses a random number  $b \in R$ . From  $r_{SB}$  and  $b$ ,  $B$  computes the one time key  $k_B$  to be shared with  $SB$  as

$$k_B = g^{bt} = (r_{SB})^b.$$

$B$  also computes  $r_B = g^b$  and  $u_B = H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_B)$  and then sends  $\langle r_B, u_B \rangle$  to  $SB$ .

**Step 5.** Upon receiving  $\langle r_A, u_A \rangle$ , server  $SA$  first computes the one time key  $k_A = g^{at}$  shared with  $A$  and then verifies that  $u_A$  from  $A$  equals the hash value  $H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_A)$ . If the verification fails,  $SA$  stops executing the protocol; otherwise,  $SA$  believes that client  $A$  is genuine.  $SA$  then sends the message  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, r_A, \sigma_{SA} \rangle$  to the server  $SB$ , where  $\sigma_{SA}$  is the signature on  $ID_A/ID_B/ID_{SA}/ID_{SB}/r_A$  generated by the signing algorithm  $S$  using the private key  $SK_{SA}$ , namely,

$$\sigma_{SA} = S_{SK_{SA}}(ID_A|ID_B|ID_{SA}|ID_{SB}|r_A).$$

Similarly, upon receiving  $\langle r_B, u_B \rangle$ , server  $SB$  computes the one time key  $k_B = g^{bt}$  shared with  $B$  and verifies that  $u_B$  from  $B$  equals  $H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_B)$ . If the verification fails,  $SB$  aborts the protocol; otherwise,  $SB$  believes client  $B$  as authentic. Then  $SB$  sends the message  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, r_B, \sigma_{SB} \rangle$  to  $SA$ , where  $\sigma_{SB}$  is the signature on  $ID_A/ID_B/ID_{SA}/ID_{SB}/r_B$  generated by  $S$  using the private key  $SK_{SB}$ , namely,

$$\sigma_{SB} = S_{SK_{SB}}(ID_A|ID_B|ID_{SA}|ID_{SB}|r_B).$$

**Step 6.** After receiving  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, r_B, \sigma_{SB} \rangle$ ,  $SA$  first verifies the signature  $\sigma_{SB}$  using the public key  $PK_{SB}$ .  $SA$  halts immediately if the verification fails. Otherwise,  $SA$  computes

$$u_{SA} = H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_A|r_A|r_A)$$

and sends  $\langle r_B, u_{SA} \rangle$  to client  $A$ .

The server  $SB$ , upon receiving  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, r_A, \sigma_{SA} \rangle$ , verifies the signature  $\sigma_{SA}$ , and if correct, computes

$$u_{SB} = H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_A|r_A|r_A)$$

and sends  $\langle r_A, u_{SB} \rangle$  to  $B$ .

**Step 7.** The client  $A$  checks whether  $u_{SA}$  from  $SA$  equals  $H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_A|r_A|r_A)$ . If this is untrue,  $A$  aborts the protocol. Otherwise,  $A$  computes the common secret value  $K$  as

$$K = g^{ab} = r_B^a$$

Similarly, client  $B$  verifies that  $u_{SB}$  from  $SB$  equals  $H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_A|r_B|r_A)$ , and if the verification succeeds, computes the common secret value  $K$  as

$$K = g^{ab} = r_A^b$$

Finally, the clients compute their session key  $sk$  as

$$sk = H(K/ID_A/ID_B/ID_{SA}/ID_{SB}).$$

### 3.2 Security Analysis on PAKA Protocol

In this preliminary version of the paper, we only provide a heuristic security analysis of the PAKA protocol, considering a variety of attacks and security properties.

### 3.2.1 Off-line Password Guessing Attack

In this attack, an attacker may try to guess a password and then to check the correctness of the guessed password off-line. If his guess fails, the attacker tries again with another password, until he find the proper one. In the PAKA protocol, the only information related to passwords is  $c_{SA} = \varepsilon_{PW_A}(g^s)$  and  $c_{SB} = \varepsilon_{PW_B}(g^t)$ , but because  $s$  and  $t$  are chosen randomly, these values does not help the attacker to verify directly the correctness of the guessed passwords. Thus, off-line password guessing attacks would be unsuccessful against the PAKA protocol.

### 3.2.2 Explicit Authentication.

Another stronger kind of security goal for a key exchange protocol to achieve is explicit authentication, the property obtained when both implicit authentication and key confirmation hold. It is straightforward to see that PAKA does not achieve explicit authentication; that is, the client  $A$  (resp.  $B$ ) does not know whether the client  $B$  (resp.  $A$ ) has successfully computed a matching session key. However, it is easy to transform any key exchange protocol  $P$  with implicit authentication into a protocol  $\tilde{P}$  providing explicit authentication by using standard techniques [3, 5].

The transformation works as follows. Suppose that in protocol  $P$ , two clients  $A$  and  $B$  ended up with computing their session key  $sk_A$  and  $sk_B$ , respectively. In protocol  $\tilde{P}$ , client  $A$  sends one additional flow  $auth_A = H(sk_A/1)$  to  $B$  and similarly, client  $B$  sends  $auth_B \stackrel{z}{=} H(sk_B/2)$  to client  $A$ . Upon receiving  $auth_B$ , client  $A$  checks the equality  $auth_B \stackrel{z}{=} H(sk_A/2)$ . If they are equal, then  $A$  computes the final session key  $sk'$  as  $sk' = H(sk_A/0)$ . Otherwise,  $A$  aborts the protocol.

Likewise, client  $B$ , after receiving  $auth_A$ , verifies that  $auth_A$  equals  $H(sk_B/1)$ . If so, then  $B$  computes the final session key  $sk'$  as  $sk' = H(sk_B/0)$ . Otherwise,  $B$  aborts the protocol. This procedure of adding explicit authentication is outlined in Fig. 2.

## IV. A Four-Party Password Authenticated Key Distribution Protocol (PAKD)

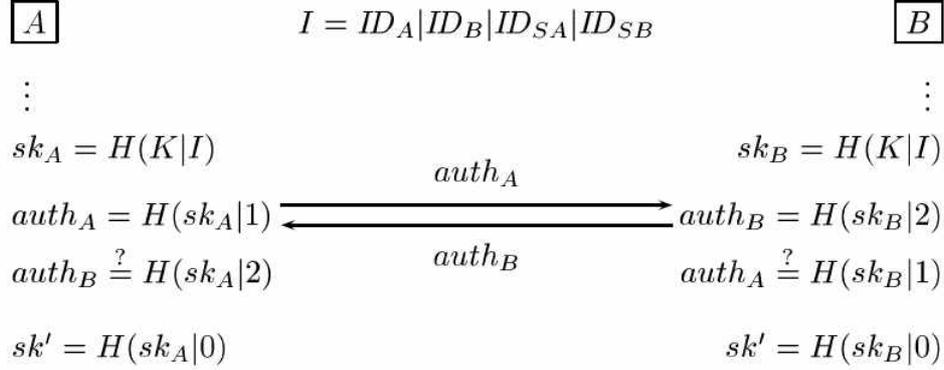
In this section we present a new four-party password authenticated key distribution protocol PAKD in which the session key is created by two servers and securely transmitted to these two clients. In describing the PAKD protocol, we will omit 'mod  $p$ ' from expressions for notational simplicity. The PAKD protocol is outlined in Fig. 3 and a more detailed description is as follows:

### 4.1 Description of PAKD Protocol

**Step 1.** Two clients  $A$  and  $B$  first need to inform each other of their respective authentication server. To this end,  $A$  sends to  $B$  the message  $\langle ID_A, ID_{SA}, ID_B \rangle$  and  $B$  sends to  $A$  the message  $\langle ID_B, ID_{SB}, ID_A \rangle$ .

**Step 2.** The clients request the assistance of their respective server in establishing a session key between them. Client  $A$  (resp.  $B$ ) does this by sending the message  $\langle ID_A, ID_B, ID_{SB} \rangle$  (resp.  $\langle ID_B, ID_A, ID_{SA} \rangle$ ) to the server  $SA$  (resp.  $SB$ ).

**Step 3.** Server  $SA$  chooses a random number  $s \in R_{Z_p^*}$ , computes  $r_{SA} = g^s$  and  $c_{SA} = \varepsilon_{PW_A}(r_{SA})$ , and sends the ciphertext  $c_{SA}$  to  $A$ . Similarly, server  $SB$  chooses a



The final session key :  
 $sk' = H(sk_A|0) = H(sk_B|0)$

<Fig. 2> Adding Explicit Authentication

random number  $t \in RZ_p^*$ , computes  $r_{SB} = g^t$  and  $c_{SB} = \varepsilon_{PW_B}(r_{SB})$ , and sends the ciphertext  $c_{SB}$  to  $B$ .

**Step 4.** After receiving  $c_{SA}$ , client  $A$  recovers  $r_{SA}$  by decrypting  $c_{SA}$  i. e.,  $r_{SA} = D_{PW_A}(c_{SA})$ , and chooses a random number  $a \in RZ_p^*$ . Given  $r_{SA}$  and  $a$ , client  $A$  computes the one time key  $k_A$  to be shared with the server  $SA$  as

$$k_A = g^{as} = (r_{SA})^a.$$

Additionally,  $A$  computes  $r_A = g^a$  and  $u_A = H(ID_A|ID_B|ID_{SA}|ID_{SB}/k_A)$ . Then  $A$  sends the message  $\langle r_A, u_A \rangle$  to the server  $SA$ .

Meanwhile, client  $B$ , having received  $c_{SB}$ , computes  $r_{SB} = D_{PW_B}(c_{SB})$  and chooses a random number  $b \in RZ_p^*$ . From  $r_{SB}$  and  $b$ ,  $B$  computes the one time key  $k_B$  to be shared with  $SB$  as

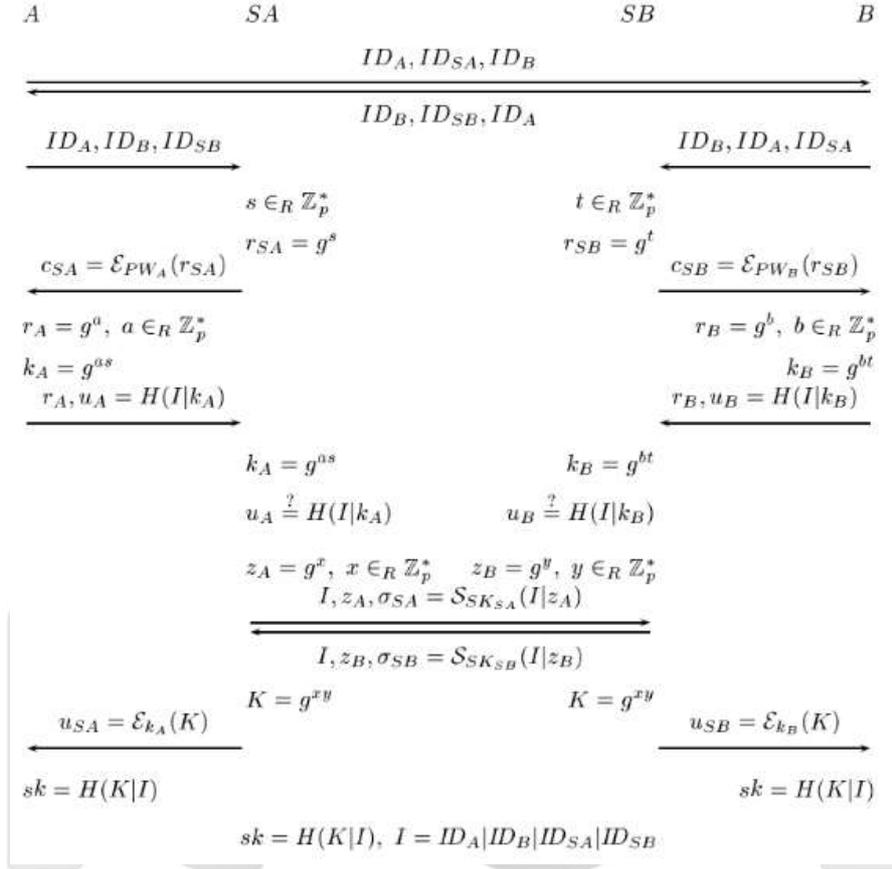
$$k_B = g^{bs} = (r_{SB})^b.$$

$B$  also computes  $r_B = g^b$  and  $u_B = H(ID_A|ID_B|ID_{SA}|ID_{SB}/k_B)$  and then sends  $\langle r_B, u_B \rangle$  to  $SB$ .

**Step 5.** Upon receiving  $\langle r_A, u_A \rangle$ , server  $SA$  first computes the one time key  $k_A = g^{as}$  shared with  $A$  and then verifies that  $u_A$  from  $A$  equals the hash value  $H(ID_A|ID_B|ID_{SA}|ID_{SB}/k_A)$ . If the verification fails,  $SA$  stops executing the protocol; otherwise,  $SA$  believes that client  $A$  is genuine.  $SA$  chooses a random number  $x \in RZ_p^*$ , computes  $z_A = g^x$ , and then sends the message  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, z_A, \sigma_{SA} \rangle$  to the server  $SB$ , where  $\sigma_{SA}$  is the signature on  $ID_A|ID_B|ID_{SA}|ID_{SB}/z_A$  generated by the signing algorithm  $S$  using the private key  $SK_{SA}$  namely,

$$\sigma_{SA} = S_{SK_{SA}}(ID_A|ID_B|ID_{SA}|ID_{SB}/z_A).$$

Similarly, after receiving  $\langle r_B, u_B \rangle$ , server  $SB$  computes the one time key  $k_B = g^{bs}$  shared with  $B$  and



<Fig. 3> Four-party password authentication key distribution protocol

verifies that  $u_B$  from  $B$  equals  $H(ID_A|ID_B|ID_{SA}|ID_{SB}|k_B)$ . If the verification fails,  $SB$  aborts the protocol; otherwise,  $SB$  believes client  $B$  as authentic. Then  $SB$  chooses a random number  $y \in_R \mathbb{Z}_p^*$ , computes  $z_B = g^y$  and sends the message  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, z_B, \sigma_{SB} \rangle$  to  $SA$ , where  $\sigma_{SB}$  is the signature on  $ID_A|ID_B|ID_{SA}|ID_{SB}|z_B$  generated by  $S$  using the private key  $SK_{SB}$ , namely,

$$\sigma_{SB} = \mathcal{S}_{SK_{SB}}(ID_A|ID_B|ID_{SA}|ID_{SB}|z_B).$$

**Step 6.** After receiving  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, z_B, \sigma_{SB} \rangle$ ,  $SA$  first verifies the signature  $\sigma_{SB}$  using the

public key  $PK_{SB}$ .  $SA$  halts immediately if the verification fails. Otherwise,  $SA$  computes

$$K = g^{xy} = (z_B)^x$$

$$u_{SA} = \mathcal{E}_{k_A}(K)$$

and sends  $\langle u_{SA} \rangle$  to client  $A$ .

The server  $SB$ , upon receiving  $\langle ID_A, ID_B, ID_{SA}, ID_{SB}, z_A, \sigma_{SA} \rangle$ , verifies the signature  $\sigma_{SA}$  and if correct, computes

$$K = g^{xy} = (z_A)^y$$

$$u_{SB} = \mathcal{E}_{k_B}(K)$$

and sends  $\langle u_{SB} \rangle$  to client B.

**Step 7.** Upon receiving  $\langle u_{SB} \rangle$ , client  $A$  recovers  $K$  by decrypting  $u_{SA}$  i. e.,  $K = D_{k_A}(u_{SA})$ .

Similarly, after receiving  $\langle u_{SA} \rangle$ , client  $B$  recovers  $K$  by decrypting  $u_{SB}$  i. e.,  $K = D_{k_B}(u_{SB})$ . Finally, the clients compute their session key  $sk$  as

$$sk = H(K/ID_A/ID_B/ID_{SA}/ID_{SB}).$$

## 4.2 Security Analysis on PAKD Protocol

In this preliminary version of the paper, we only provide a heuristic security analysis of the proposed protocol, considering a variety of attacks and security properties; a rigorous proof of security in a formal communication model will be given in the full version of this paper.

### 4.2.1 Off-line Password Guessing Attack.

In the proposed protocol, the only information related to passwords is  $c_{SA} = \varepsilon_{PW_A}(g^s)$  and  $c_{SB} = \varepsilon_{PW_B}(g^t)$ , but because  $s$  and  $t$  are chosen randomly, these values does not help the attacker to verify directly the correctness of the guessed passwords. Thus, off-line password guessing attacks would be unsuccessful against the proposed protocol.

### 4.2.2 Undetectable On-Line Password Guessing Attack.

At the highest level of security threat to password authenticated key exchange protocols are undetectable on-line password guessing attacks [8] where an attacker tries to check the correctness of a guessed password in an on-line transaction with the server, i. e., in a fake execution of the protocol; if his guess fails, he starts a new transaction with the server using

another guessed password. Indeed, the possibility of an undetectable on-line password guessing attack in the three-or-more-party setting represents a qualitative difference from the two-party setting where such attack is not a concern. However, this attack is meaningful only when the server is unable to distinguish an honest request from a malicious one, since a failed guess should not be detected and logged by the server.

In our protocol, the server is the first who issues a challenge and the client is the first who replies with an answer to some challenge. It is mainly due to this ordering that the protocol is secure against undetectable on-line password guessing attacks. Suppose that an attacker  $A'$ , posing as  $A$ , decrypts  $c_{SA}$  by guessing a password, computes  $r_{A'}$ ,  $k_{A'}$  and  $u_{A'} = H(ID_A/ID_B/ID_{SA}/ID_{SB}/k_{A'})$  by choosing his own random  $a'$ , and sends the fake message  $\langle r_{A'}, u_{A'} \rangle$  to server  $SA$ . Then, the server  $SA$ , upon receiving  $r_{A'}$  and  $u_{A'}$  from  $A'$ , should be easily able to detect a failed guess since the protocol specification mandates  $SA$  to check the correctness of  $u_A$ . Note that the attacker cannot send a correct  $u_A$  without knowing a correct  $k_A$  which in turn only can be computed if the guessed password is correct. Hence, the proposed protocol can resist undetectable on-line password guessing attacks.

### 4.2.3 Insider Attack.

Suppose one client, say  $A$ , tries to learn the password of the other client  $B$  during execution of the protocol. Of course,  $A$  should not be able to have this ability through a protocol run and this is still an important security concern to be addressed. As mentioned earlier in this section, the only information related to the  $B$ 's password is  $c_{SB} = \varepsilon_{PW_B}(r_{SB})$ , where

$r_{SB}$  is computed as  $r_{SB} = g^t$  and  $t$  is a random value chosen by the server  $SB$ . The actual value  $r_{SB}$  itself is never included in any message sent in the protocol and  $t$  is a secret information only known to  $SB$ . This means that the malicious insider  $A$  has no advantage over outside attackers in learning  $B$ 's password. In other words,  $A$ 's privileged information —  $PW_A$ ,  $r_{SA}$  and  $k_A$  — gives  $A$  no help in learning  $B$ 's password. Therefore, our protocol is also secure against insider attacks.

#### 4.2.4 Implicit Key Authentication.

Given  $Z_A = g^x$  and  $Z_B = g^y$ , the secret value  $K = g^{xy}$  cannot be computed, since no polynomial algorithm has been found to solve the computational Diffie-Hellman problem. Thus, if the random numbers  $x$  and  $y$  are unknown, then the session key  $sk$  cannot be computed since  $H$  is a one-way hash function. Hence, the secrecy of the session key is guaranteed based on the computational Diffie-Hellman assumption in the random oracle model [4].

#### 4.2.5 Perfect Forward Secrecy.

The proposed protocol also achieves perfect forward secrecy [7] since the long-term information of the protocol participants is used for implicit key authentication only, and not for hiding the session key. Even if an attacker obtains the clients' passwords and the servers' signing private keys, he cannot get any of secret values  $K = g^{xy}$  computed in previous sessions since  $x$  and  $y$  chosen respectively by  $SA$  (resp.  $SB$ ) are unknown. Because the session key in this protocol is computed as  $sk = H(K/ID_A/ID_B/ID_{SA}/ID_{SB})$ , he cannot compute it without knowing the secret value  $K$ . Hence, our protocol provides perfect forward secrecy.

Table 1. Comparison of security properties between PAKA and PKAD

Security Property	PAKA	PAKD
Off-line password guessing attack	satisfy	satisfy
Undetectable on-line password guessing attack	satisfy	satisfy
Insider attack	satisfy	satisfy
Perfect forward secrecy	satisfy	satisfy
Known key security	satisfy	satisfy
Implicit key authentication	satisfy	satisfy

#### 4.2.6 Known Key Security.

In our protocol, the session keys generated in different sessions are independent since the ephemeral secret exponents  $x$  and  $y$  are chosen independently at random from session to session. Thus, the proposed protocol still achieves its goal in the face of an attacker who has learned some other session keys.

## V. Conclusion

We considered the problem of password authenticated key exchange in the inter domain distributed computing environment, where the authentication server of one client is different from that of another client, hence four parties — two clients and two servers — involved in key exchange. The work of Yeh and Sun [20] is probably the first and only one that deals with the problem. But, the protocols by Yeh and Sun exhibit an undesirable feature that each client needs not only to remember a password shared with the server but also to store and manage the server's public key. In some sense, this disadvantage obviates the reason for considering password authenticated protocols in the first place; it is difficult for humans to securely manage long

cryptographic keys. The contribution of this paper was to propose the four-party password authenticated key exchange protocol that requires each client only to remember a password shared with its authentication server. We, in this preliminary version of the paper, showed heuristically that the proposed protocol achieves all the intended security goals against a variety of attacks. We leave a rigorous security proof for the protocol in a formal communication model as a future work.

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