Pseudo-Orthogonal Space-Time Block Codes for MIMO-OFDM Systems over Frequency-Selective Channels

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Abstract

This paper proposes a new class of Space-Time Block Codes, which is manipulated from the existing transmit diversity schemes. We analyze the performance and the receiver complexity of the proposed scheme and confirm that the new diversity scheme can yield performance gain over other existing four-transmit antenna cases. By relaxing the diversity criterion on code designs, the proposed space-time code provides a full transmission rate for four-transmit antennas and makes it possible to approach the open-loop Shannon channel capacity. Outage capacity and simulation results are used to show that substantial improvements in performance while maintaining a simple linear processing receiver structure are obtained in frequency selective channels

1. Introduction

Recently, many researchers have studies using multiple antennas with space-time codes (STC) since a simple transmit diversity concept was introduced by Alamouti [1]. The STC techniques are used to improve the performance of multiple-input multiple-output (MIMO) systems. The potential gains of the STC/MIMO system are presented in [2,3,4,5,6,7,8,9]. A core idea is the space-time signal processing in which the time domain operation is complemented with the spatial dimension processing inherent in the use of spatially distributed multiple antennas. Mostly, space-time coding schemes have been developed assuming flat fading channels. As the increasing demand for higher bit rates leads to wideband communications, the wireless channels become frequency selective. It has been presented in [10] [11] that multicarrier modulation realized by orthogonal

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frequency division multiplexing (OFDM) is well suited for

such broadband applications. The OFDM modulation technique divides the total available bandwidth into a number of equally spaced frequency bands. By applying a proper cyclic prefix, the individual subchannels can be considered to show flat fading channel characteristics. Furthermore, OFDM can exploit frequency diversity by applying channel coding.

The construction of space-time coding schemes is to a large extent a trade-off among the following three goals: maximizing the error performance (i.e., diversity order and coding gain), maximizing the code rate and maintaining a simple decoding [5] [12]. For flat fading channels, optimizing the diversity order is the most critical point in designing STC. In contrast, for frequency selective channels where frequency diversity is available, the full diversity becomes a less important issue. Therefore, a better strategy is to loosen the full diversity condition and complement the loss of the diversity order by the channel frequency diversity exploited by OFDM-based systems so that we can concentrate on the full rate and maximize the coding gain instead. In this paper, we propose pseudo-orthogonal space-time block codes for MIMO-OFDM systems over frequency-selective channels. It will be shown that the proposed pseudo-orthogonal scheme provide additional coding advantage while maintaining a simple decoding algorithm.

The organization of the paper is as follows. In section II, we

construct a new class of space-time block codes (STBC) and derive a receiver algorithm. In section III, we analyze the performance of the new scheme. In section IV, we compute the outage capacity of the proposed STBC and compare it to other alternative schemes. In section V, the simulation results are presented comparing to other competing designs. Finally, the paper is terminated with conclusions in section VI.

2. A New Class of Space-Time Block Code

In this section, we introduce a new class of space time block code. We relax the definition of complex orthogonal designs in [2] to obtain the full rate STBC. Here we define a pseudo-orthogonal matrix as follows.

Definition 1. A pseudo-orthogonal (PO) design in variables $x_1, x_2, ..., x_n$ is an n by n matrix \mathbf{C} such that

- The entries of \mathbf{C} are $\pm x_1, \pm x_1^*, \pm x_2, \pm x_2^*, \dots, \pm x_n, \pm x_n^*$
 - $\mathbf{C}^H \mathbf{C} = \mathbf{D}$, where \mathbf{D} is a diagonal matrix with (i,i) th

diagonal element of the form $\left(l_1^i\left|x_1\right|^2+l_2^i\left|x_2\right|^2+\ldots+l_n^i\left|x_n\right|^2\right),$

with non-negative coefficients $l_1^i, l_2^i, \dots, l_n^i$ such that

$$l_1^i + l_2^i + \ldots + l_n^i = n$$

where H and * denote the complex-conjugate and transpose and the complex conjugate respectively. In contrast to the definition of orthogonal designs in [2], the pseudo-orthogonal schemes allow zero coefficients l_j^i such that \mathbf{D} is no longer an identity matrix.

For simplicity, we focus on the four transmit antenna case in this paper. The CDMA transmit diversity method introduced in [13] satisfies the pseudo-orthogonal code design conditions. We start from the Alamouti scheme [1] as a base matrix to build higher order matrices. Let us first define the code matrix \mathbf{X}_{ii} as

$$\mathbf{X}_{ij} = \begin{bmatrix} x_i & x_j \\ -x_j^* & x_i^* \end{bmatrix}. \tag{1}$$

Then, \mathbf{X}_{ii} is a well known Alamouti code matrix. We

extract some properties from the Alamouti matrix (1) and 2x2 Hadamard matrix in [14].

Then, the transmission matrix is given as

$$\mathbf{C} = \begin{bmatrix} \mathbf{X}_{12} & \mathbf{X}_{34} \\ -\mathbf{X}_{12} & \mathbf{X}_{34} \end{bmatrix} = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 \\ -x_2^* & x_1^* & -x_4^* & x_3^* \\ -x_1 & -x_2 & x_3 & x_4 \\ x_2^* & -x_1^* & -x_4^* & x_3^* \end{bmatrix}.$$
(2)

The code matrix (2) satisfies the pseudo-orthogonal code design conditions such that

$$\mathbf{C}^{\dagger}\mathbf{C} = \begin{bmatrix} d_1 & 0 & 0 & 0 \\ 0 & d_1 & 0 & 0 \\ 0 & 0 & d_2 & 0 \\ 0 & 0 & 0 & d_2 \end{bmatrix}$$

where

$$d_1 = 2(|x_1|^2 + |x_2|^2)$$
 and

 $d_2 = 2\left(\left|x_3\right|^2 + \left|x_4\right|^2\right). \text{ It is straightforward to check that}$ the minimum rank of the matrix $\mathbf{C}\left(x_{c1} - x_{e1}, x_{c2} - x_{e2}, x_{c3} - x_{e3}, x_{c4} - x_{e4}\right) \text{ as in [3] is}$ two. For simplicity, we assume the single receive antenna case. Let us define the received signal vector \mathbf{r} , the code matrix \mathbf{C} , and the noise vector \mathbf{n} . Then the received signals can be written as

$$\mathbf{r} = \begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \end{bmatrix} = \mathbf{C} \begin{bmatrix} h_1 \\ h_2 \\ h_3 \\ h_4 \end{bmatrix} + \mathbf{n}$$
 (3)

where we assume that \mathbf{n} is a vector of additive noise terms, which are independent and identically-distributed complex Gaussian with variance $\sigma_n^2=1$. The channel coefficient h_i is the path gain from the transmit antenna i to the receive antenna. The path gains are modeled as samples of independent complex Gaussian random variables with variance 0.5 per dimension. This choice models a Rayleigh fading environment.

By taking the complex-conjugate operation on the second and the fourth element of \mathbf{r} in (3), we obtain

$$\tilde{\mathbf{r}} = \mathbf{H}\mathbf{x} + \tilde{\mathbf{n}} \tag{4}$$

¹ Quasi-orthogonal and Semi-orthogonal are already defined for different class.

where
$$\tilde{\mathbf{n}} = \begin{bmatrix} n_1 & n_2^* & n_3 & n_4^* \end{bmatrix}^T$$
, $\mathbf{x} = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 \end{bmatrix}^T$ and $\tilde{\mathbf{r}} = \begin{bmatrix} r_1 & r_2^* & r_3 & r_4^* \end{bmatrix}^T$. Here \mathbf{H} is a channel matrix with space (in columns) and time (in rows) dimensions defined as

$$\mathbf{H} = \begin{bmatrix} h_1 & h_2 & h_3 & h_4 \\ h_2^* & -h_1^* & h_4^* & -h_3^* \\ -h_1 & -h_2 & h_3 & h_4 \\ -h_2^* & h_1^* & h_4^* & -h_3^* \end{bmatrix}.$$

This channel matrix inherently possesses a pseudo-orthogonal property such that

$$\mathbf{H}^{H}\mathbf{H} = \begin{bmatrix} \gamma_{1} & 0 & 0 & 0 \\ 0 & \gamma_{1} & 0 & 0 \\ 0 & 0 & \gamma_{2} & 0 \\ 0 & 0 & 0 & \gamma_{2} \end{bmatrix}$$
 (5)

where
$$\gamma_1=2\Big(\big|h_1\big|^2+\big|h_2\big|^2\Big)$$
 and $\gamma_2=2\Big(\big|h_3\big|^2+\big|h_4\big|^2\Big)$.

We are now ready to begin linear processing at the receiver using the vector channel model in (4). We will assume that the realization of \mathbf{H} is known to the receiver, but not to the transmitter. The MIMO channel can be decomposed into parallel channels by applying the channel matched filter \mathbf{H}^H , and this results in

$$\hat{\mathbf{r}} = \mathbf{H}^H \tilde{\mathbf{r}} = \mathbf{D} \mathbf{x} + \hat{\mathbf{n}} \tag{6}$$

where \mathbf{D} is a diagonal matrix $\mathbf{D} = \operatorname{diag}(\gamma_1, \gamma_1, \gamma_2, \gamma_2)$ and

$$\hat{\mathbf{n}} = \mathbf{H}^H \tilde{\mathbf{n}}$$
.

The estimated signal $\hat{\mathbf{X}}$ can then be obtained as

$$\widehat{\mathbf{x}} = \mathbf{D}^{-1}\widehat{\mathbf{r}} = \mathbf{x} + \mathbf{D}^{-1}\widehat{\mathbf{n}}$$
.

Computing the noise autocorrelation matrix yields

$$\mathbf{R}_{nn} = E \left[\left(\mathbf{D}^{-1} \hat{\mathbf{n}} \right) \left(\mathbf{D}^{-1} \hat{\mathbf{n}} \right)^{H} \right]$$
$$= E \left[\mathbf{D}^{-1} \mathbf{H}^{H} \tilde{\mathbf{n}} \tilde{\mathbf{n}}^{H} \mathbf{H} \mathbf{D}^{-1} \right]$$
$$= \mathbf{D}^{-1}.$$

The diversity gains corresponding to recovering (x_1,x_2) and (x_3,x_4) are γ_1 and γ_2 , respectively. Thus the diversity gain reduces from $\left(\left|h_1\right|^2+\left|h_2\right|^2+\left|h_3\right|^2+\left|h_4\right|^2\right)$

, to
$$2\left(\left|h_1\right|^2+\left|h_2\right|^2\right)$$
 or $2\left(\left|h_3\right|^2+\left|h_4\right|^2\right)$ compared to the

full diversity scheme. Note that the proposed scheme achieves the full rate at the expense of the reduced transmit diversity. We will later observe that in spite of the partial transmit diversity, the proposed scheme outperforms the full diversity designs for frequency selective channels.

It has been shown [2] that transmission using orthogonal designs provides a full diversity and a simplified decoding algorithm and also that for more than two transmit antennas there exists no complex orthogonal code which achieves the full diversity and the full rate at the same time. Therefore, for a system employing more than two transmit antennas, either the diversity order or the transmission rate should be sacrificed. In order to achieve the full rate, the proposed pseudo-orthogonal codes do not fully satisfy the complex orthogonal code design conditions in [2]. Nonetheless, we maintain an orthogonality property so that the proposed code can still employ a very simple maximum-likelihood decoding algorithm at the cost of the partial diversity order.

Suppose a set S consisting of all possible symbol vectors \mathbf{X} . Then the size of S is equal to M^4 , where M represents the number of constellation points. The ML detection for the transmitted symbol vector in (4) can be obtained as

$$\widehat{\mathbf{x}} = \arg\min_{\widehat{\mathbf{x}} \in S} \| \widetilde{\mathbf{r}} - \mathbf{H} \widehat{\mathbf{x}} \|^2.$$
 (7)

Using the fact that \mathbf{H} is pseudo-orthogonal as shown in (5), the ML solution yields

$$\widehat{\mathbf{x}} = \arg\min_{\widehat{\mathbf{x}} \in S} (\widetilde{\mathbf{r}} - \mathbf{H}\widehat{\mathbf{x}})^{H} (\widetilde{\mathbf{r}} - \mathbf{H}\widehat{\mathbf{x}})$$

$$= \arg\min_{\widehat{\mathbf{x}} \in S} (\widetilde{\mathbf{r}} - \mathbf{H}\widehat{\mathbf{x}})^{H} (\mathbf{H}^{H}\mathbf{H}) (\widetilde{\mathbf{r}} - \mathbf{H}\widehat{\mathbf{x}})$$

$$= \arg\min_{\widehat{\mathbf{x}} \in S} \|\mathbf{H}^{H} (\widetilde{\mathbf{r}} - \mathbf{H}\widehat{\mathbf{x}})\|^{2}$$

$$= \arg\min_{\widehat{\mathbf{x}} \in S} \|\mathbf{H}^{H}\widetilde{\mathbf{r}} - \mathbf{D}\widehat{\mathbf{x}}\|^{2}.$$
(8)

Thus the ML decoding rule in (7) is reduced to a simple decorrelating expression in (8).

Let us define \mathbf{h}_i as the i th column vector in \mathbf{H} . Then the decision metric for detecting x_1 or x_2 is obtained from (8) as

$$\left|\mathbf{h}_{i}^{H}\tilde{\mathbf{r}}-\gamma_{1}x_{i}\right|^{2}$$
,

And similarly the metric for detecting x_3 or x_4 is

$$\left|\mathbf{h}_{j}^{H}\tilde{\mathbf{r}}-\gamma_{2}x_{j}\right|^{2}.$$

It is also straightforward to see that the decision rule can be extended to multiple receive antenna. The decoding scheme for the pseudo-orthogonal design is as simple as the one established for the complex orthogonal designs in [2]. Also soft output for the transmitted symbol is readily available. These soft decisions are fed to the outer channel code (e.g., convolutional codes) to yield better performance.

3. Code Design Criteria

We analyze the proposed STBC in terms of the performance criteria presented in [3]. The design criteria for space-time codes are fully formulated through the codeword difference matrix \mathbf{B}_{ce} , which is defined as $\mathbf{B}_{ce} = \mathbf{C}_c - \mathbf{C}_e$. Here \mathbf{C}_c is the transmitted code matrix and \mathbf{C}_e is the erroneously detected matrix. The probability of transmitting the codeword $\mathbf{c} = (c_1(1), \dots, c_1(l), \dots$

 $,c_{n}(l),\ldots,c_{l}(1)\big)$ and deciding erroneously in favor of a different codeword

$$\mathbf{e} = (e_1(1), \dots, e_n(1), \dots, e_1(l), \dots, e_n(l))$$
 is given by [3]

$$P(\mathbf{c} \to \mathbf{e} | h_{ij}, i = 1, 2, ..., n, j = 1, 2, ..., m)$$

$$\leq \exp\left(-\left(\frac{E_s}{4N_o}\right)\sum_{j=1}^{m}\sum_{k=1}^{l}\left|\sum_{i=1}^{n}h_{ij}\left(c_i(k)-e_i(k)\right)\right|^2\right)$$

where n, m and l represent the number of transmitters, receivers, and the packet, respectively. Under the assumption of Rayleigh fading channels, the above error probability bound can be rewritten after some algebra as

$$P(\mathbf{c} \to \mathbf{e}) \le \left(\prod_{i=1}^{r} \lambda_{i}\right)^{-m} \left(\frac{E_{s}}{4N_{o}}\right)^{-rm} \tag{9}$$

where r denotes the rank of matrix $\mathbf{A} = \mathbf{B}_{ce}^{\dagger} \mathbf{B}_{ce}$ and λ_i denotes nonzero eigenvalues of \mathbf{A} . Thus a diversity advantage of rm and a coding advantage of $(\lambda_1 \lambda_2 \dots \lambda_r)^{1/r}$ are achieved. Since the matrix \mathbf{B}_{ce} has an equivalent property with the matrix \mathbf{A} in the sense of rank and determinant, we proceed to investigate the matrix

 \mathbf{B}_{ce} to minimize the pairwise error probability (PEP), which determines the performance at high signal-to-noise ratios.

Concentrating on the four transmit antenna systems, we compare with other complex orthogonal designs. Let us define P and O as the pseudo-orthogonal designs and the orthogonal designs, respectively. Then the diversity order is

$$\begin{aligned} \min_{c \neq e} \operatorname{rank} \left[P_{ce}^{H} P_{ce} \right] &= \min_{c \neq e} \operatorname{rank} \left[\sum_{k=1}^{2} 2 \left| x_{ck} - x_{ek} \right|^{2} \begin{bmatrix} \mathbf{I}_{2} & 0 \\ 0 & 0 \end{bmatrix} \right] \\ &+ \sum_{k=3}^{4} 2 \left| x_{ck} - x_{ek} \right|^{2} \begin{bmatrix} 0 & 0 \\ 0 & \mathbf{I}_{2} \end{bmatrix} \right] &= 2. \end{aligned}$$

It is now clear that the diversity of the pseudo-orthogonal designs is 2 while the diversity of orthogonal designs is 4.

We recognize here that the multiplicative term 2 in diagonal terms makes a coding advantage in terms of the determinant criteria for the pseudo-orthogonal codes. The evaluations of the determinant criteria for $\,P\,$ and $\,O\,$ then yield

$$\min_{c \neq e} \det \left[O_{ce}^{H} O_{ce} \right] = \min_{c \neq e} \left[\sum_{k=1}^{4} \left| x_{ck} - x_{ek} \right|^{2} \right]^{4}$$
$$= \left| x_{ck} - x_{ek} \right|^{8} \quad \text{for } k = 1, \dots, 4$$

and

$$\min_{c \neq e} \det \left[P_{ce}^{H} P_{ce} \right] = \min_{c \neq e} 4 \left[\sum_{k=1}^{2} \left| x_{ck} - x_{ek} \right|^{2} \right]^{2}$$

$$\otimes \left[\sum_{k=3}^{4} \left| x_{ck} - x_{ek} \right|^{2} \right]^{2}$$

$$= 4 \left| x_{ck} - x_{ek} \right|^{4} \quad \text{for } k = 1, \dots, 4$$

where \otimes denotes product between nonzero values and leave out the zero values.

The minimum value of $\left(\det\left[\mathbf{C}_{ce}^H\mathbf{C}_{ce}\right]\right)^{1/r}$ determines the coding advantage in (9). Therefore, the coding gain of the orthogonal design O is $\left|x_{ck}-x_{ek}\right|^2$ whereas the coding gain of the pseudo-orthogonal design P is $2\left|x_{ck}-x_{ek}\right|^2$. Consequently, the pseudo-orthogonal designs have a 3dB coding gain over the orthogonal design.

4. Channel Capacity

In this section, we analyze the channel capacity for the proposed scheme and compare with other alternatives. We require that the total transmitted power is held constant independently of the number of transmit antennas. Components of \mathbf{X} are assumed to be independent and identically distributed. Then we have

$$E\left[\mathbf{x}\mathbf{x}^H\right] = \frac{\rho}{N}\mathbf{I}_N$$

where ρ is the SNR at the receiver and \mathbf{I}_N denotes the identity matrix of order N .

The capacity of systems with N transmit antennas is given by [4]

$$C_N = \log_2\left(1 + \frac{\rho}{N} \sum_{i=1}^N \left| h_i \right|^2\right) \text{b/s/Hz}.$$
(10)

Note that the capacity $\,C_N\,$ approaches the Gaussian capacity $\log_2(1+\rho)\,$ as $\,N\,$ becomes larger [15]. In practice, the

random variable $\frac{1}{N} \sum_{i=1}^{N} \left| h_i \right|^2$ is already close to 1 when

N is as small as 4 [3]. This motivates us to explore a compromise between the full rate and full diversity.

The Alamouti scheme [1] achieves the open-loop capacity of (10) with $\ N=2$

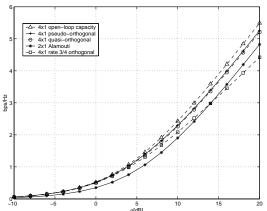


Figure 1. Outage capacities compared to other alternative schemes

$$C_{Al} = \log_2 \left(1 + \frac{\rho(|h_1|^2 + |h_2|^2)}{2} \right).$$

We can calculate the channel capacity of the pseudo-orthogonal scheme using the vector channel model (6). The capacity is then given by

$$C_{PO} = \log_2 \det \left(1 + \frac{\rho}{4} \mathbf{D} \right).$$

Since **D** is a diagonal matrix, it follows

$$C_{PO} = \frac{1}{2}\log_{2}\left(1 + \frac{\rho(|h_{1}|^{2} + |h_{2}|^{2})}{2}\right) + \frac{1}{2}\log_{2}\left(1 + \frac{\rho(|h_{3}|^{2} + |h_{4}|^{2})}{2}\right).$$

We now investigate the outage capacity to illustrate the impact on the systems. The ${\cal E}$ outage capacity b is defined as [15]

$$C_{\varepsilon}^{out}(b) = [b : \max b \text{ such that } P(b) \le \varepsilon]$$

where P(b) denotes the probability that the data rate b can not be supported. The outage capacity is calculated by Monte-Carlo simulations and provides additional insight into the performance characteristics of different designs [17]. The 10% outage capacities of the different schemes are plotted in Figure 1. The channel capacities for the quasi-orthogonal codes and orthogonal codes are obtained from [17]. For comparison purposes, this figure includes the system with two transmit antennas and one receive antenna as a reference. No other alternatives outperform the pseudo-orthogonal design except for 4x1 open-loop capacity, which is merely a theoretical case. We emphasize that the pseudo-orthogonal design employs much simpler decoding algorithm than any other alternatives for four transmit antennas.

5. Simulation Results

In this section, we present the simulation results for the four-transmit antenna systems. The system parameters are summarized in Table I. The binary convolutional code polynomials

(133, 171) in octal notation are used throughout the simulation.

3bps/Hz	2bps/Hz
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Rate 3/4 Orthogonal	64QAM R _c =2/3	16QAM R _c =2/3
Quasi-orthogonal	16QAM R _c =3/4	16QAM R _c =1/2
Pseudo-orthogonal	16QAM R _c =3/4	16QAM R _c =1/2

Table I. System Parameters

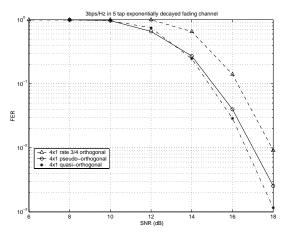


Figure 2. Performance comparison to other alternative schemes

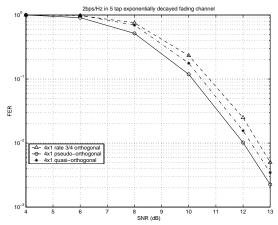


Figure 3. Performance comparison to other alternative schemes

The spectral efficiencies of 2bps/Hz and 3bps/Hz are assumed. We use a typical indoor channel model with a 5 tap power delay profile having exponentially decayed fading

characteristics where each ray is assumed to be independently Rayleigh fading. The OFDM modulation defined in the 802.11a standard with 64 point FFT are used. One OFDM symbol duration is 4 μ s including the 0.8 μ s guard interval. This specification is designed to handle the root mean square (RMS) delay spread up to 250ns. The 5 tap multipath channel used in the simulations accounts for approximately the RMS spread of 100 ns. The length of the frame is assumed to consist of four OFDM symbol. It has been shown [18] that a rotation of constellation results in a performance improvement for the quasi-orthogonal codes. A optimal rotation of constellation obtained in [18] is used for the quasi-orthogonal codes. For the rate 3/4 orthogonal codes, we have used the code matrix in [19].

First, Figure 2 shows the comparison between different schemes with 3 bps/Hz in a 4 by 1 system. It is observed from the plot that the proposed scheme exhibits about a 1dB gain over the orthogonal designs and performs as good as quasi-orthogonal codes at 1% FER. Considering the receiver complexities, the pseudo-orthogonal codes with a simple decoding algorithm are much more attractive than the quasi-orthogonal codes which require the more complex decoder structure. It is also interesting that there is no distinctive slope change among different schemes in Figure 2. This is due to the fact that the frequency selective channel contains some level of

frequency diversity inherent in the channel with OFDM.

The performance of OFDM-based systems can be further improved by applying lower rate channel coding exploiting additional frequency diversity. The frequency selective channels have more dramatic effect on the performance of pseudo-orthogonal codes. The frequency diversity can complement the partial transmit diversity of the pseudo-orthogonal codes. Figure 3 shows that the performance gain of the pseudo-orthogonal codes over the other schemes increases as lower channel coding rate is adopted.

The simulation results justify our code design that we can benefit from a reasonable compromise between a full rate and a full diversity. They also confirm that the coding gain shown in section III enhances the performance in the frequency selective channels, where a coding gain plays more important role than a diversity gain. Consequently, the simulation results show that a better performance is possible when more frequency diversity exists in the channel.

6. Conclusion

In this paper, a new class of space-time block codes has been presented and evaluated for frequency selective channels. We have shown that the proposed scheme has a simple decoding structure and outperforms the existing other orthogonal designs for four transmit antenna systems. Furthermore, the computer simulation demonstrates that we need to consider the channel characteristics and take a compromise between the full rate and the full diversity. We have used the design criteria to justify the improvement of the performance for the pseudo-orthogonal. The proposed scheme can be generalized to the systems with larger number of transmit antennas.

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