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천연가스 배관 곡관부에서의 피그 동적 거동 해석

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Analysis of PIG Dynamics through Curved Section in Natural Gas Pipeline

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Summary

This paper presents simple models for flow and the PIG dynamics when it passes through a 90° curved section of pipeline. The simulation has been done with two different operational boundary conditions. The solution for non-linear hyperbolic partial equations for flow is given by using MOC. The Runge-Kuta method is used to solve the initial condition equation for flow and the PIG dynamics equation. The simulation results show that the proposed model and solution can be used for estimating the PIG dynamics when the pig runs in the pipeline including curved section.

Abstract – In this paper, dynamic modeling and its analysis for the PIG flow through 90° curved pipe with compressible and unsteady flow are studied. The PIG dynamics model is derived by using Lagrange equation under assumption that it passes through 3 different sections in the curved pipeline such that it moves into, inside and out of the curved section. The downstream and up stream flow dynamics including the curved sections are solved using MOC. The effectiveness of the derived mathematical models is estimated by simulation results for a low pressure natural gas pipeline including downward and upward curved sections. The simulation results show that the proposed model and solution can be used for estimating the PIG dynamics when we pig the pipeline including curved section.

Key words : Pipeline Inspection Gauge (PIG), Method Of Characteristic (MOC), Pipeline

I. Intrduction

Pipelines are the most common way and the safest method to transport oil and gas products. During operation, the walls of pipelines suffer a deterioration process and pipeline conditions get worse. Pipelines can be failed with time if they are not properly maintained. One part of a maintenance procedure of pipelines is pigging them regularly to prevent the increase of their wall roughness and the reduction of the internal diameter. The tool used for pigging is called Pipeline Inspection Gauge (PIG). There are different types of PIG and each type is designed for some different desired purposes. All of the PIGs are the most effective when they run at a near constant speed but will not be effective in case that they run at too high speed. The typical speeds for utility pigging are about 1-5m/s for on-stream liquids and 2-7m/s for onstream gas. Excessive and uncontrolled speed of a PIG can be very dangerous. So, prediction and control of the PIG velocity are very important when we operate a pigging process. Pigging of pipelines has become a standard procedure in gas and oil industry. One of the difficulties when we design a pigging operation is in fact that most of the available knowledge is based on experiment field. Hence, estimating the PIG dynamics often involves some guesswork and, consequently, a high degree of uncertainty^[7].

Results of research on the dynamics of the PIG in pipelines are scarcely found in the literature. Some works relating to this subject have been reported. J.M.M. Out^[9], 1993, used Lax-Wendroff scheme for the integration of gas equations with adaptation of finite difference grid. The grid has to be continuously updated with the PIG position and the fluid values at the new grid points are estimated by interpolation. Azevedo et al.^[7], 1996, simplified the solution with assumption of incompressible and steady state of flow. P.C.R. Lima^[6], 1999, solved the problem by using one-dimensional

semi-implicit finite difference scheme. At each time step, the nonlinear algebraic equations are solved using Newton's method. T.T. Nguyen et al. [1-3], 2000, treated the compressible, unsteady flow dynamic equations for flows in straight pipeline by using MOC and solved the PIG dynamic equation by using Runge-Kuta method.

The flow in the curved pipe is much more complex than the flow in straight pipe because of the centrifugally-induced secondary motions. Also the PIG dynamics in curved pipe are nonlinear. At this moment, there is no paper related to the dynamics of the PIG when it passes through the curved section of pipeline.

This paper deals with the PIG dynamics when it flows through a 90° curved section of pipeline with compressible and unsteady low pressure natural gas flow. The PIG dynamics model is obtained by using Lagrange equation under the condition that it passes through 3 different sections in the curved pipeline such that it moves into, inside and out of the curved section. The downstream and upstream flow dynamics including the curved sections are solved using MOC. The initial values of upstream and downstream are get from the analytical equation of general unsteady, compressible flow equations under assumption of steady state dynamics. The initial values of upstream and downstream flows and the PIG dynamics are solved using Runge-Kuta method. The effectiveness of the derived mathematical models is estimated through simulation results for a natural gas pipeline including downward and upward curved sections.

II. Modeling

The scheme of PIG flow in curved pipe can be described in Fig. 1.

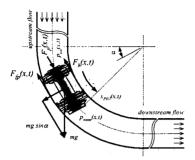


Fig.1. PIG flow in the bending pipeline.

1. Gas Flow Model

We assume as the following:

- i. the natural gas is ideal,
- ii. flow is one phase,
- iii. the pipeline diameter is constant,
- iv. the friction factor is a function of wall roughness and Reynolds number. Steady state values are used in transient calculations,
- v. the flow is quasi-steady heat flow.

The unsteady flow dynamic equations for flow in straight pipeline are given in the previous work^[1-3]. In this paper, we consider the flow in curved section. The flows in curved pipe are much more complex than those in the straight pipe because of the centrifugally-induced secondary motions. There are rich analytical literature related to the flow in curved pipe (Adler, 1934; Hasson, 1955; Barua,1963; Mori and Nakayama, 1965; Ito, 1975; Collin and Denis, 1975; VanDyke, 1978)^[10].

It is well known that the flows in curved pipe depend on the Dean number κ :

$$\kappa = 2\delta^{1/2} \operatorname{Re} = \left(\frac{d}{R_b}\right)^{1/2} \frac{2 du}{v} \tag{1}$$

The friction ratio between the curved pipe and the straight pipe with the same flow conditions is studied by Adler, 1934; Hasson,1955; Ito, 1975; and Van Dyke, $1978^{[10]}$. They suggested the approximate function for the friction ratio f_c / f_s which

is a function of Dean number. Among them, the model proposed by Hasson well fitted to the experiment data and the friction ratio is given as follows^[10]:

$$\frac{f_c}{f_c} = 0.0969 \ \kappa^{1/2} + 0.556 \tag{2}$$

Here we do not need to consider the behavior of the secondary flow. Our problem is to know the average flow values at each cross section in curved pipeline. Hence, in this paper we use the Hasson approximate function (2) to estimate the friction coefficient of the flow in the curved pipe. The friction coefficient in the straight pipe can be found in the references^[1-3,5,9,12].

Consider the control volume as shown in Fig. 2.

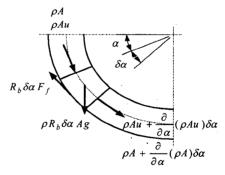


Fig. 2. Control volume for application of motion flow equation in curved pipe section.

When $\delta\alpha$ is small enough, the four basic flow equations such as continuity, momentum, state and energy equations can be derived as the following:

$$\frac{\partial \rho}{\partial t} + \frac{u}{R_h} \frac{\partial \rho}{\partial \alpha} + \frac{\rho}{R_h} \frac{\partial u}{\partial \alpha} = 0$$
 (3)

$$\frac{1}{R_h} \frac{\partial p}{\partial \alpha} + \frac{\rho u}{R_h} \frac{\partial u}{\partial \alpha} + \rho \frac{\partial u}{\partial t} + \frac{F_f}{A} - \rho g \cos \alpha = 0$$

(4)

$$\frac{p}{\rho} = (\gamma - 1)C_V T \tag{5}$$

$$\frac{\partial}{\partial t} \left[\rho \left(C_V T + \frac{u^2}{2} \right) \right] + \frac{1}{R_b} \frac{\partial}{\partial \alpha} \left[\rho \left(C_V T + \frac{u^2}{2} \right) u \right] + \frac{1}{R_b} \frac{\partial}{\partial \alpha} (p u) - \frac{q S}{A} = 0$$
 (6)

The mathematical description of the heat rate term, q in Eq. (6) depends on the problem assumptions. Because there is no heat producing in flow, q could be evaluated as a quasi-steady heat transfer from the surrounding environment to the gas:

$$q = C_C (T_{ext} - T)$$
 (7)
Let us define

$$s \equiv R_b \alpha \qquad 0 \le s \le R_b \pi / 2$$

After some rearrangement, the above equations can be rewritten as follows:

$$\frac{\partial \rho}{\partial t} + u \frac{\partial \rho}{\partial s} + \rho \frac{\partial u}{\partial s} = 0$$
(8)

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial s} + \frac{1}{\rho} \frac{\partial p}{\partial s} = -\frac{F_f}{\rho A} + g \cos \left(\frac{s}{R_b}\right)$$

(9)

$$\frac{\partial p}{\partial t} + u \frac{\partial p}{\partial s} + \gamma p \frac{\partial u}{\partial s} = \frac{\gamma - 1}{A} \left\{ \left[F_f - A \rho g \cos \left(\frac{s}{R_b} \right) \right] u + q S \right\}$$
(10)

Using MOC^[8,12] to transform the nonlinear hyperbolic partial differential equations (8)-(10) to the ordinary differential

equations which can be integrated by finite differences in the form, we can obtain the following equations:

$$\frac{du}{dt} + \frac{c}{\rho p} \frac{dp}{dt} = E_1 \quad \text{along} \quad \frac{ds}{dt} = u + c$$
(11)

$$\frac{du}{dt} - \frac{c}{\rho p} \frac{dp}{dt} = E_2 \text{ along } \frac{ds}{dt} = u - c$$
(12)

$$\frac{dp}{dt} - c^2 \frac{d\rho}{dt} = E_3 \text{ along } \frac{ds}{dt} = u$$
(13)

where

$$E_1 = \frac{\gamma - 1}{c} \frac{q}{\rho m} + \left(\frac{F_f}{\rho A} - g \cos \alpha \right) \left(\frac{\gamma - 1}{c} u - 1 \right)$$

(14)

$$E_2 = -\frac{\gamma - 1}{c} \frac{q}{\rho m} - \left(\frac{F_f}{\rho A} - g \cos \alpha \right) \left(\frac{\gamma - 1}{c} u + 1 \right)$$

(15)

$$E_3 = (\gamma - 1)\frac{q}{m} + \left(\frac{F_f}{\rho A} - g\cos\alpha\right)(\gamma - 1)u\rho$$

(16)
$$m = A/S$$
, $c = (\gamma p/\rho)^{1/2}$

The initial values of flow are given from steady state condition of flow. The governing steady flow equations can be derived from the analytical equations (8)-(10):

$$\rho u = const$$
(17)

$$\frac{dp}{ds} = -\frac{F_f}{A} + \rho g \cos\left(\frac{s}{R_h}\right) +$$

$$\frac{u}{u^2 - c^2} \left[\gamma \frac{F_f u}{A} - \gamma \rho g \cos \left(\frac{s}{R_b} \right) u + (\gamma - 1) \frac{q}{m} \right]$$
(18)
$$\frac{du}{ds} = -\frac{1}{\rho (u^2 - c^2)} \times \left[\gamma \frac{F_f u}{A} - \gamma \rho g \cos \left(\frac{s}{R_b} \right) u + (\gamma - 1) \frac{q}{m} \right]$$

(19)

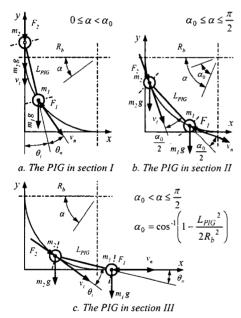


Fig. 3. The scheme of PIG flow in downward curved pipe.

2. PIG Dynamics Model

Dynamic equation for PIG flow in straight pipeline can be found in references^[1-3,9]. In this paper we deal with the PIG moving in 90° curved section of pipeline. The PIG contacts pipe's wall through its front and tail cups. To model the PIG motion in curved pipe, we consider that the mass of the PIG is concentrated at its end parts as shown in Fig. 3. Hence, the mass of the PIG becomes 2 particle masses located at its nose and tail.

The PIG moves through curved pipe in three different sections: moving into, moving inside and moving out of the curved section as shown in the above figure. To derive its dynamic equation, we use Lagrange method[11]. Let us consider the system of 2 particles whose positions are given by Cartesian coordinates (x_i, y_i) , (i=1,2). The system is one degree of freedom and α is chosen to be generalized coordinate. Lagrange equation is in the form:

$$\frac{d}{dt}\left(\frac{\partial K}{\partial \dot{\alpha}}\right) - \frac{\partial K}{\partial \alpha} + \frac{\partial P}{\partial \alpha} = F \tag{20}$$

where K, P and F are kinetic energy, potential energy and generalized force, respectively:

$$K = \frac{1}{2} m_1 \left(\dot{x}_1^2 + \dot{y}_1^2 \right) + \frac{1}{2} m_2 \left(\dot{x}_2^2 + \dot{y}_2^2 \right)$$
(21)

$$P = m_1 g y_1 + m_2 g y_2 (22)$$

$$F = F_1^x \frac{\partial x_1}{\partial \alpha} + F_1^y \frac{\partial y_1}{\partial \alpha} + F_2^x \frac{\partial x_2}{\partial \alpha} + F_2^y \frac{\partial y_2}{\partial \alpha}$$

(23)

where m_i is the mass of the particle i; (x_i, y_i) is coordinate of the particle i; F_i^x , F_i^y is the force acting on the particle i in the direction of x and y coordinates (i=1,2). Using equations (20)-(23), after some calculations, we can get the dynamic equations of the PIG when it passes through each curved section I, II and III as shown in Fig. 3, respectively:

$$\ddot{\alpha} + \frac{m_2 Y Y_{\alpha}}{m_1 R_b^2 + m_2 Y^2} \dot{\alpha}^2 = \frac{m_1 g R_b \cos \alpha + m_2 g Y - F_1 R_b + F_2 Y}{m_1 R_b^2 + m_2 Y^2}$$
(24)

$$\ddot{\alpha} = \frac{m_1 g \cos \alpha + m_2 g \cos (\alpha - \alpha_0) - F_1 + F_2}{(m_1 + m_2) R_b}$$

$$(25)$$

$$\ddot{\alpha} + \frac{m_1 T T_{\alpha}}{m_1 T^2 + m_2 R_b^2} \dot{\alpha}^2 = \frac{m_2 g \cos \alpha - F_1 T + F_2 R_b}{m_1 T^2 + m_2 R_b^2}$$

$$(26)$$

where
$$X = \sqrt{L_{PIG}^2 - R_b^2 (1 - \cos \alpha)^2}$$

$$Y = R_b \cos \alpha + \frac{R_b^2}{X} \left(\sin \alpha - \frac{1}{2} \sin 2\alpha \right)$$

$$Y_\alpha = \frac{\partial Y}{\partial \alpha}$$

$$Z = \sqrt{L_{PIG}^2 - R_b^2 (1 - \sin \alpha)^2}$$

$$T = R_b \sin \alpha + \frac{R_b^2}{Z} \left(\cos \alpha - \frac{1}{2} \sin 2\alpha \right)$$

$$T_\alpha = \frac{\partial T}{\partial \alpha}$$

The forces acting on the PIG include gravity force of the PIG, the different pressure across its body and friction force. Generalized forces acting on the PIG in each section are given in the following:

In section I:

$$F_{1} = -m_{1}g\cos\alpha + \left(p_{n}A + \frac{1}{2}F_{fp}\right)\cos\theta_{n}$$

$$F_{2} = m_{2}g + \left(p_{t}A - \frac{1}{2}F_{fp}\right)\cos\theta_{t}$$

$$\theta_{t} = \sin^{-1}\left(\frac{R_{b}(1 - \cos\alpha)}{L_{PIG}}\right),$$

$$\theta_{n} = \alpha - \theta_{t}$$

In section II:

$$F_1 = -m_1 g \cos \alpha + \left(p_n A + \frac{1}{2} F_{fp} \right) \cos \frac{\alpha_0}{2}$$

$$F_2 = m_2 g \cos (\alpha - \alpha_0) + \left(p_r A - \frac{1}{2} F_{fp} \right) \cos \frac{\alpha_0}{2}$$

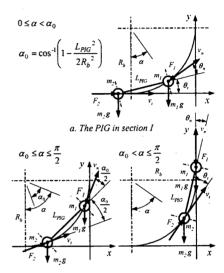
In section III:

$$F_1 = \left(p_n A + \frac{1}{2} F_{fp}\right) \cos \theta_n$$

$$F_2 = m_2 g \cos \alpha + \left(p_t A - \frac{1}{2} F_{fp} \right) \cos \theta_t$$

$$\theta_n = \sin^{-1} \left(\frac{R_b (1 - \sin \alpha)}{L_{PIG}} \right),$$

$$\theta_t = \frac{\pi}{2} - (\alpha + \theta_n)$$



b. The PIG in section II c. The PIG in section III

Fig. 4. The scheme of PIG flow in upward curved pipe.

The scheme for deriving the PIG dynamics when it moves in upward curved pipe is given in Fig. 4.

In the case of upward curved section, by the same way, we have the dynamic equations of the PIG as follows:

In section I:

$$F_{1} = m_{1}g \sin \alpha + \left(p_{n}A + \frac{1}{2}F_{fp}\right)\cos \theta_{n}$$

$$F_{2} = \left(p_{t}A - \frac{1}{2}F_{fp}\right)\cos \theta_{t}$$

$$\theta_{t} = \sin^{-1}\left(\frac{R_{b}(1 - \cos \alpha)}{L_{PIG}}\right), \ \theta_{n} = \alpha - \theta_{t}$$

$$\ddot{\alpha} + \frac{m_{2}YY_{\alpha}}{m_{1}R_{b}^{2} + m_{2}Y^{2}}\dot{\alpha}^{2} = \frac{-m_{1}gR_{b}\sin \alpha - F_{1}R_{b} + F_{2}Y}{m_{1}R_{b}^{2} + m_{2}Y^{2}}$$

(27)

In section II:

$$F_1 \approx m_1 g \sin \alpha + \left(p_n A + \frac{1}{2} F_{fp} \right) \cos \frac{\alpha_0}{2}$$

$$F_2 \approx -m_2 g \sin(\alpha - \alpha_0) + \left(p_1 A - \frac{1}{2} F_{fp} \right) \cos \frac{\alpha_0}{2}$$

$$\ddot{\alpha} = \frac{-m_1 g \sin \alpha - m_2 g \sin(\alpha - \alpha_0) - F_1 + F_2}{(m_1 + m_2) R_2}$$

(28)

In section III:

$$F_{1} = m_{1}g + \left(p_{n}A + \frac{1}{2}F_{fp}\right)\cos\theta_{n}$$

$$F_{2} = -m_{2}g\sin\alpha + \left(p_{t}A - \frac{1}{2}F_{fp}\right)\cos\theta_{t}$$

$$\theta_{n} = \sin^{-1}\left(\frac{R_{b}(1 - \sin\alpha)}{L_{PlG}}\right),$$

$$\theta_{t} = \frac{\pi}{2} - (\alpha + \theta_{n})$$

$$\ddot{\alpha} + \frac{m_{1}TT_{\alpha}}{m_{1}T^{2} + m_{2}R_{b}^{2}}\dot{\alpha}^{2} = \frac{-m_{1}gT - m_{2}gR_{b}\sin\alpha - F_{1}T + F_{2}R_{b}}{m_{1}T^{2} + m_{2}R_{b}^{2}}$$

$$(29)$$

III. Simulation and Results

The computational scheme for solving the PIG dynamics together with upstream and down stream flow dynamics by using MOC were presented in the previous work^[1-3]. Eqs. (17)-(19) are solved using Runge-Kuta method to get the initial values of upstream and downstream flows in pipeline. Also the PIG dynamic equations are solved using Runge-Kuta method.

The simulation is done with a low pressure natural gas pipeline including start riser, downward curved, upward curved and end raiser sections. This type of pipeline is used when we transport gas from buoy to tank as shown in the Fig. 5. The scheme of pipeline using in the simulation is given in Fig. 6.

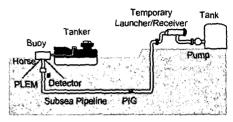


Fig. 5. The U-shaped pipeline used to transport gas.

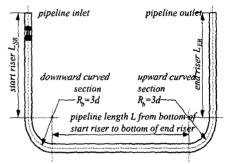


Fig. 6. Scheme of pipeline using in the simulation.

We choose the sampling time $\Delta t = 0.001s$ and the sampling distance $\Delta x = 0.5785 \, m$. And two following boundary conditions of interest are used: (1) constant flow rate at pipeline inlet $u_0(t) = u_0$ and constant pressure at pipeline outlet $p_L(t) = p_L$; (2) constant pressure at pipeline inlet $p_0(t) = p_0$ and constant flow rate at pipeline outlet $u_1(t) = u_1$.

The numerical values using in this simulation are given in the Table. 1.

Table. 1. Numerical values for simulation.

Parameters	Values	Units	Parameters	Values	Units
L	12	m	ν	1.45e-5	m²/s
LSR	12	m	R	518.30	J/kgK
LER	12	m	γ	1.40	
L_{PlG}	1.1	m	M	750	kg
d	0.7366	m	C_C	2	W/m²s
x_{PIG}^{0}	1.1	m	v_{PIG}^0	4	m/s

k	0.0450	mm	F_{fp}	0.33	bar
<i>p</i> ₀	8	bar	p_L	7.65	bar
Qo	1.16	m³/s	Q_L	1.16	m³/s
ρ_0	5.44	kg/m³	ρ_L	5.20	kg/m³
Text	15	⁰ C	T	15	⁰ С

Figure 7 shows the different pressure acting on the PIG. It varies with different operational boundary conditions.

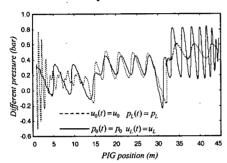


Fig. 7. Different pressure acting on the PIG.

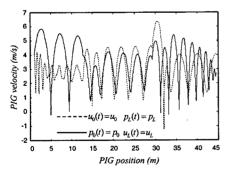


Fig. 8. PIG velocity vs. PIG position.

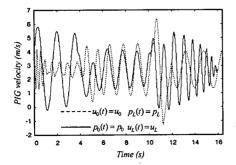


Fig. 9. PIG velocity vs. time.

Figure 8 shows the PIG velocity at each its position. In both cases, the maximum velocities seem to be the same but in case of the second boundary condition, the PIG arrives its trap barrel with lower velocity. Fig. 9 shows the PIG velocity vs. time when it moves in the pipeline. The PIG velocity oscillates in the different manners in different parts of the pipeline.

IV. Conclusion

This paper presents simple models for flow and the PIG dynamics when it passes through a 90° curved section of pipeline. The simulation has been done with two different operational boundary conditions. The solution for non-linear hyperbolic partial equations for flow is given by using MOC. The Runge-Kuta method is used to solve the initial condition equation for flow and the PIG dynamics equation. The simulation results show that the proposed model and solution can be used for estimating the PIG dynamics when the pig runs in the pipeline including curved section.

Acknowledgment

This paper is a part of study results of "Modeling and Control of PIG Flow in Natural Gas Pipeline" which is studied by Korea Gas Corporation support. We gratefully acknowledge the contributions and suggestions of related persons.

Nomenclatures

A	pipe cross section	$[m^2]$
c	wave speed	[m/s]
C_C	convection heat transfer coeffic	cient
		$[m^2]$
d	internal diameter of pipeline	[m]
f_c	friction coefficient in curved p	ipeline
f_s	friction coefficient in straight p	ipeline
F_b	braking force	[<i>N</i>]
F_f	friction force per unit pipe leng	gth
,		[N/m]
F_{c}	friction force between the PIG	and[N]

	pipe wall	
F_p	force due to different pressure	[<i>N</i>]
•	acting on the PIG	
g	gravity acceleration	$[m/s^2]$
\boldsymbol{k}	pipe wall roughness	[m]
L	length of pipeline	[m]
L_{SR}	length of start riser	[m]
L_{ER}	length of end riser	[m]
L_{PIG}	length of the PIG	[m]
m	hydraulic mean radius of pipe	[m]
M	mass of the PIG	[kg]
p	flow pressure	$[N/m^2]$
q	compound rate of heat inflow	$[W/m^2]$
-	per unit area of pipe's wall	
R	gas constant $[J/kgK]$	
R_b	bending radius of curved section	on [m]
S	perimeter of pipe	[<i>m</i>]
S	distance from inlet of curved s	ection
		[m]
T	flow temperature	$[{}^{\bar{o}}C]$
T_{ext}	seabed temperature	$[{}^{0}C]$
u	flow velocity	[m/s]
	Crooks:	

Greeks:

- y the ratio of specific heat
- κ Dean number
- ν kinetic viscosity of flow $[m^2/s]$
- o flow density $[kg/m^3]$

Subscripts

- n, t denote the points at the nose and tail of the PIG
- o, L denote the points at inlet and outlet of pipeline

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