A Posture Control for Two Wheeled Mobile Robots

Hyun-Sik Shim and Yoon-Gyeoung Sung

Abstract: In this paper, a posture control for nonholonomic mobile robots is proposed with an empirical basis. In order to obtain fast and consecutive motions in realistic applications, the motion requirements of a mobile robot are defined. Under the assumption of a velocity controller designed with the selection guidance of control parameters, the algorithm of posture control is presented and experimentally demonstrated for practicality and effectiveness.

Keywords: nonholonomic mobile robot, posture control, soccer robot

I. Introduction

It has been a topic to design the wheeled mobile robot controller due to the control redundancy that an ordinary mobile robot possesses only two degrees of freedom for motion control, while its posture is described by three degrees of freedom. For the entire system dynamics, the kinematic relation is nonlinearly coupled. Moreover, the mobile robot is described by a non-holonomic system with its unintegrable constraint equation. Hence, a variety of approaches have been proposed including various techniques of automatic control [1], [2].

Kanayama et al. [3] presented the use of reference and current postures for vehicle control, the use of a local error coordinate system, and a PI control algorithm for linear and rotational velocities. A novel control algorithm for determining the robot's linear and rotational velocities based on Lyapunov theory is described in [4]. The algorithm has a convergence problem so that if the reference linear velocity is zero, convergence cannot be achieved. Thus, it cannot be applied to the parking problem. Shim and Kim [5] suggested a stable tracking control method for a non-holonomic vehicle to resolve the convergence problem. Aicardi et al. [6] presented a control algorithm which uses polar coordinates and its stability was proven with the Laypunov stability theory. For convenient analysis and motion control design, the algorithms [4], [5], [6] were reported with numerical simulations. Recently, Yang and Kim [7] presented an algorithm with sliding mode control with the inclusion of robot dynamics. Those algorithms were evaluated under constraint conditions in practical illustrations.

For the experiment, most of the algorithms were sluggish due to the limitations of motor output, velocity controller performance, etc. A controller in this paper is presented with an empirical motivation by taking the robot kinematics at the controller design stage as simple as possible. Contrary to the former control design approaches with a mathematical basis, the control algorithm is designed by focusing on the given specifications of the robot's desired trajectory and physical limitations. The stability of the proposed controller is verified with the Lyapunov stability theory in the reference [8]. With the worst case of scenario, the effectiveness and robustness of the posture control are demonstrated through experiments.

Manuscript received: Jan. 22, 2000., Accepted: June 23, 2000. Hyun-Sik Shim: LG Traffic Information System Yoon-Gyeoung Sung: School of Mechanical Eng., Yeungnam University The remainder of the paper is organized as follows. In Section 2, the notations used and the kinematic model are defined. In Section 3, a control law for motion control is designed. In Section 4, experimental results illustrate the effectiveness of the scheme. Lastly, the conclusion is given.

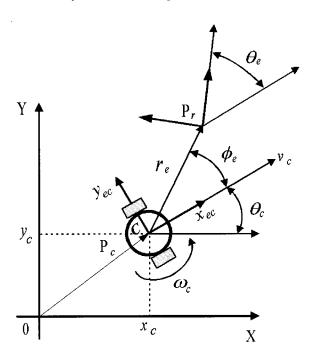


Fig. 1. Coordinate system of the mobile robot (subscript "c" refers to the "current state").

II. Kinematics of the mobile robot

A mobile robot is on a 2-D plane in a global cartesian coordinate. There are global coordinates X-Y and local coordinates x-y attached to the center of the robot body as shown in Figure 1. The robot has three degrees of freedom in its relative positioning which is represented by the *posture*,

$$\mathbf{p} = \begin{pmatrix} x \\ y \\ \theta \end{pmatrix} \tag{1}$$

where, the heading direction θ is taken counterclockwise from the X-axis to the x-axis. The angle θ indicates the orientation of the robot or the wheels. The set $(x \ y)$ represents the robot

position. In Figure 1, the vector $(x_c \ y_c \ \theta_c)^T$ corresponds to the current posture of the robot.

The robot's motion is controlled by its *linear velocity* v and angular velocity ω , which are functions of time. The robot kinematics are defined by the Jacobian matrix $J(\theta)$,

$$\dot{\mathbf{p}} = \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} = J(\theta)\mathbf{q} = \begin{pmatrix} \cos\theta & 0 \\ \sin\theta & 0 \\ 0 & 1 \end{pmatrix} \mathbf{q}$$
 (2)

where, $\mathbf{q} = (v \ \omega)^T$.

As mobile robot postures in control implementation, there are two postures such as the *reference* $\mathbf{p}_r = (x_r \ y_r \ \theta_r)^T$ which is the target posture and the *current posture* $\mathbf{p}_c = (x_c \ y_c \ \theta_c)^T$ which is the true posture at the current moment. By transforming the position of the robot in cartesian coordinates into polar coordinates, the posture error is expressed as

$$\begin{pmatrix} x_{ec} \\ y_{ec} \\ \theta_{ec} \end{pmatrix} = \begin{pmatrix} \cos \theta_c & \sin \theta_c & 0 \\ -\sin \theta_c & \cos \theta_c & 0 \\ 0 & 0 & 1 \end{pmatrix} (\mathbf{p}_r - \mathbf{p}_c) = \begin{pmatrix} r_e \cos \phi_e \\ r_e \sin \phi_e \\ \theta_e \end{pmatrix}$$
(3)

where, $r_e > 0$ is the distance error, $\theta_e = \theta_r - \theta_c$ is the orientation error with respect to \mathbf{p}_c , and ϕ_e is the angle measured from the robot's principle axis to the distance error vector r_e . The posture velocity error [6] in polar coordinates is expressed as

$$\begin{cases} \dot{r}_e = -v_c \cos \phi_e \\ \dot{\phi}_e = -\omega_c + v_c \frac{\sin \phi_e}{r_e} \\ \dot{\theta}_e = -\omega_c \end{cases}$$
(4)

III. Posture control

For the control based on robot kinematics, a control structure is composed of a velocity controller and a posture controller as shown in Fig. 2. If a reference posture is given, the controllers command the mobile robot to engage in the reference posture. The posture controller let the robot chase the reference posture through a velocity command q_m . The velocity controller then makes the robot follow the command q_m . However, in the velocity controller, the dynamic model of the mobile robot is needed. Moreover, computational burden follows in implementing this scheme. Considering these issues, a posture controller is presented under the assumption that the velocity controller is designed using a control scheme such as adaptive control [9], variable structure control [10], or nonlinear feedback control [11]. In this paper, if the velocity controller designed is under such as friction, unknown disturbances or motor saturation, it could assume that a command velocity becomes the robot's velocity: $\mathbf{q}_m = \mathbf{q}_c$.

A. Motion Requirements

The motion specifications based on the posture velocity error in Eq.(4), to follow a trajectory or a velocity command, are given as follows:

- (1) If the traveling distance to the reference posture is large, then move fast. Reduce speed as it comes closer.
 - (2) It should take the arriving time to arrive at a final posture.

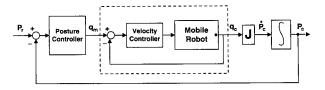


Fig. 2. Control diagram with posture controller.

- (3) If the angle error ϕ_e is large, the robot's linear velocity should be reduced so that the robot will have a traveling distance.
- (4) If the reference posture is far, it needs to reduce the distance error first.
- (5) The robot should meet the reference posture immediately.

These specifications require the posture controller to generate the best trajectory with a posture error. The posture controller is designed using the vector $(r_e \ \phi_e \ \theta_e)^T$ and the velocity command to the robot is generated based on the above specifications.

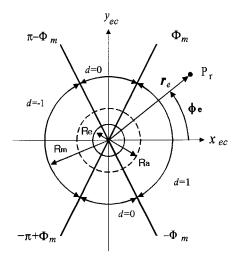


Fig. 3. Control parameter assignment to the robot's location.

For the first and second specifications, a linear velocity controller with $v_m = k_r r_e$ is considered. This equation is similar to the equation proposed by Aicardi *et al.* [6]. When the distance is very large, the velocity command will be very high and the robot velocity will be saturated. Instead of r_e , a new variable r_e' is introduced to take care of such a situation:

$$r_e^{'} = \left\{ egin{array}{ll} rac{\pi}{2}, & r_e \geq R_m \\ rac{\pi r_e}{2R_m}, & ext{otherwise.} \end{array}
ight.$$

A 'sine' relation instead of a linear one is employed so that the velocity becomes higher even with a smaller r_e :

$$v_m = k_r \sin r_e^{'}$$
.

For the third specification, the angle error ϕ_e is used in controlling the linear velocity. To apply an inverse proportional relationship for ϕ_e , the following equation is employed:

$$v_m = k_r \sin r_e' \cos \phi_e.$$

The following variables are defined for limitations:

$$d = \left\{ \begin{array}{ll} 1, & -\Phi_m \leq \phi_e \leq \Phi_m \\ -1, & \phi_e < -\pi + \Phi_m \text{ or } \phi_e > \pi - \Phi_m \\ 0, & \text{otherwise,} \end{array} \right.$$

$$\phi_e^{'} = \left\{ \begin{array}{ll} \phi_e - \pi, & \phi_e > \frac{\pi}{2} \\ \phi_e + \pi, & \phi_e < -\frac{\pi}{2} \\ \phi_e, & \text{otherwise,} \end{array} \right.$$

$$\theta_e^{'} = \left\{ egin{array}{ll} heta_e - \pi, & heta_e > rac{\pi}{2} \ heta_e + \pi, & heta_e < -rac{\pi}{2} \ heta_e, & ext{otherwise} \end{array}
ight.$$

where, Φ_m is an arbitrary constant between 0 and $\frac{\pi}{2}$. By introducing d, ϕ_e' and θ_e' , it is possible to make the robot move in the back and forth directions because the front and rear sides of a mobile robot are not distinguishable. Thus, the linear velocity controller law with a new parameter diagram in Fig. 3 is proposed as

$$v_m = k_r d \sin r_e^{'} \cos \phi_e^{'} \tag{5}$$

where, k_r is a positive constant with the unit of velocity and d refers to the direction of the robot so that the robot moves in a forward direction with d=1 and in a backward direction with d=-1. Since there is no difference between the front and rear sides of a mobile robot, only the regions $r_e \geq 0, -\frac{\pi}{2} \leq \phi_e \leq \frac{\pi}{2}$ and $-\frac{\pi}{2} \leq \theta_e \leq \frac{\pi}{2}$ are considered. For each of the distance errors r_e and angle errors ϕ_e , four regions are classified as in Fig. 4.

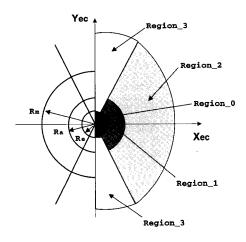


Fig. 4. Four classifications to r_e and ϕ_e . Region_0 $(r_e \leq R_e)$, Region_1 $(-\Phi_m \leq \phi_e \leq \Phi_m \text{ and } R_e \leq r_e \leq R_a)$, Region_2 $(-\Phi_m \leq \phi_e \leq \Phi_m \text{ and } r_e \geq R_a)$ and Region_3 $(\Phi_m < \phi_e \leq \frac{\pi}{2}, -\frac{\pi}{2} \leq \phi_e < -\Phi_m \text{ and } r_e > R_e)$.

In order to regulate the angle and orientation errors, the angular velocity is uniquely employed in this paper. Based on the design concept above, a relation equation could be expressed as

$$\omega_{m} = k_{\theta} (\sin \phi_{e}^{'} + \sin \theta_{e}^{'})$$

where k_{θ} is a positive constant with the unit of angular velocity. When the reference posture is at a distance, the angle error ϕ_e should be considered more to meet the fourth specification. As the robot is approaching the reference posture, the orientation

error θ_e will be the important factor to meet the 4th specification. Therefore, the angular velocity control law is deliberately proposed as

$$\omega_{m} = k_{\theta}(\epsilon \sin \phi_{e}^{'} + (1 - \epsilon) \sin \theta_{e}^{'})$$
 (6)

where, a variable ϵ is defined as

$$\epsilon = \begin{cases} 0 & r_e \le R_e \\ 0.5 - \alpha Sgn(\sin\theta'_e)Sgn(\sin\theta'_e + \sin\phi'_e) \\ R_e < r_e < R_a \\ 1 & \text{otherwise} \end{cases}$$

where, $0 < R_e \le R_a \le R_m$, $0 < \alpha < 0.5$ and, the function Sgn(x) is 1 if x is positive and is -1 otherwise.

The control parameters for the proposed control law are k_r , k_θ , R_m , R_e , R_a and Φ_m . Various trajectories can be generated according to their values. However, the trajectories do not differ as much from each other as those in [4], [5], [6]. This is possible because the control laws for v_m and ω_m are designed based on the design specifications.

 k_r and k_θ are the variables limited by the maximum velocity of the robot. To the contrary, the values of k_r and k_θ should be higher to meet the 2nd specification. To tackle this problem, the robot's linear velocity v and angular velocity ω should be limited within the shadow areas as shown in Fig. 5, as a robot's wheel velocity is limited by its maximum velocity V_{max} . That is, the robot should be controlled by the values within this area. If a high linear velocity v_m is given, the applied angular velocity ω_c should be limited to a smaller value than the control command ω_m in the calculation. Therefore, k_r and k_θ must be limited to

$$k_r + Lk_\theta \le V_{max} \tag{7}$$

where, L is the radius of the robot body.

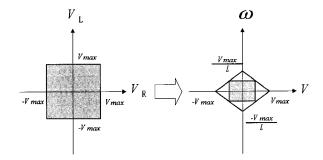


Fig. 5. Usable velocity area of wheel and robot velocities.

 R_m is a deceleration factor for linear velocity. If it is large, the velocity is reduced even when the robot is too far away. A high value reduces slippage and makes it more stable than a smaller R_m . It will, however, take more time to reach the target point.

 Φ_m should be decided because it is related to the trajectory. If it is close to $\Phi_m=0^\circ$, the robot motion will be "turning" or "going straight". However, if it is close to $\Phi_m=90^\circ$, the traveling distance will be large. Therefore, Φ_m is an important factor which is related to the allowable error range (maximum R_e).

 R_a is the radius of the circular area where the control law has all three error terms. It can generate similar trajectories with smaller differences according to Φ_m . If it has a small value, the trajectory is close to a straight line and the orientation error is reduced at the reference posture. If it has a large value, the trajectory is smooth and it may take a longer time to get to the target point.

 R_e takes an allowable value based on the system performance and its maximum value depends on Φ_m . If a small value is used for the same, the arriving time will be much longer.

In the implementation of the motion control, there are several control parameters such as k_r , k_θ , R_m , R_e , R_a , and Φ_m so that the motion trajectory depends on the parameters. In Figs. 6 and 7, the variation of the motion trajectory are shown according to the parameters R_a and Φ_m .

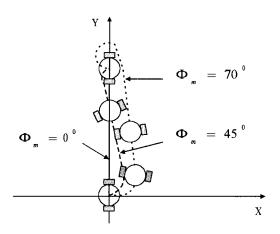


Fig. 6. Schematic trajectory variation to Φ_m .

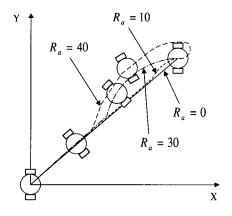


Fig. 7. Schematic trajectory variation to R_a .

IV. Experimental evaluation

1. Experimental evaluation

In order to illustrate the effectiveness and practicality of the proposed method with a PID (Proportional Integral Derivative) velocity controller as a worst case of scenario, the posture control law is implemented with a mobile robot, sized $7.5cm \times 7.5cm \times 7.5cm$, designed for robot soccer games [12], [13]. The soccer robot employed has no body frame, but has 2 PCBs with surface mounting devices. The robot has an 80C196KC microprocessor running at 20MHz, and two wheels

driven by two DC motors with two LM629 motion controllers. The LM629 chip is used as a velocity controller which receives only a reference velocity as the input signal and implicitly generates the required torque according to the reference velocity via the L298 driver chip. The maximum speed of the robot is about 125 cm/sec.

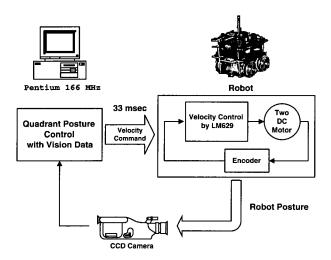


Fig. 8. Control block diagram of a vision based mobile robot.

The sampling time of the posture control is 33 msec which is depending on the vision processing time. The sampling time of the velocity controller is 410 μsec . The command velocities (v,ω) from the posture controller are utilized to get the right and left wheel velocities (V_R,V_L) as

$$V_R = v + L\omega$$

$$V_L = v - L\omega$$

where, L is the radius of the robot body. The host computer transmits the wheel velocities to the motion controller of the robot. However, accurate motion information is not provided to the robot system because the command velocity of the motor is updated by 1cm/sec and the locating accuracy of the vision system is limited to $1~cm \sim 2~cm$. Therefore, the proposed algorithm will be demonstrated under a nonideal situation with the built-in PID velocity controller on the LM629.

In this paper, R_e is chosen as $2\ cm$ due to the locating accuracy of the vision information. This is a suitable choice because it is more than the maximum error of $1.607\ cm$ when $\Phi_m=70^\circ$. The reference posture is given as $(100,50,0^\circ)$. Fig. 9 shows the robot trajectories according to the values of R_a . The smaller R_a is, the faster the robot can move to its reference posture. It is shown that the orientation error is largely reduced when the robot is close to the reference posture. Fig. 10 shows the robot trajectories according to R_m . There is little difference between the two trajectories since it works only when the robot is close to the reference posture. However, it takes $3.465\ sec$ for $R_m=10$ and $6.1\ sec$ for $R_m=50$ to get the reference posture so that it is faster when R_m is small.

Fig. 11 shows the robot trajectories for various values of k_r . k_r refers to the maximum linear velocity of the robot with unit cm/sec. If the maximum velocity is high, the robot will quickly arrive at the reference posture. However, if the maximum ve-

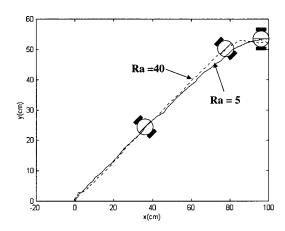


Fig. 9. Robot trajectories to the values of R_a ($k_r=60,\,\Phi_m=70^\circ,\,R_m=20,\,k_\theta=10,\,p_r=(112,72,0^\circ)$).

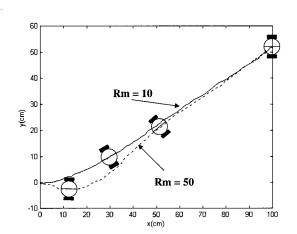


Fig. 10. Robot trajectories to the values of R_m ($k_r=60$, $\Phi_m=70^\circ$, $R_a=10$, $k_\theta=10$).

locity is very high, the trajectories could not achieve the design specifications.

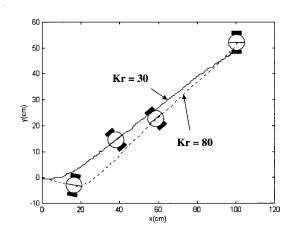


Fig. 11. Robot trajectories to the values of k_r ($R_a=10, \Phi_m=70^\circ, R_m=20, k_\theta=10$).

In Fig. 12, the robot trajectories are shown through the

7 via-points determined in advance as a more general robot motion control. the Via-points are located at $(60,47,0^{\circ})$, $(115,70,45^{\circ})$, $(120,48,0^{\circ})$, $(113,17,-45^{\circ})$, $(66,13,0^{\circ})$, $(13,20,0^{\circ})$, and $(16,80,90^{\circ})$ from 'Start' to 'Via 6'. The posture control could generate a smooth motion trajectory in both a continuous reference posture and a discrete reference posture.

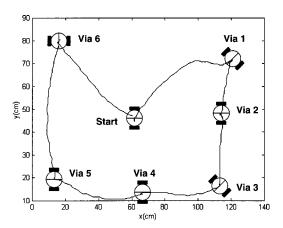


Fig. 12. Consecutive robot trajectory through 7 via-points ($k_r=60~R_a=10, \Phi_m=70^\circ, R_m=20, k_\theta=10$).

V. Conclusion

In this paper, a posture control is proposed with empirical motivation. The control law was derived based on the given design specifications for the desired trajectory. In the experiment, no matter how the velocity controller may be constructed, an ideal controller will not be readily designed because velocity and acceleration limits exist resulting from limitations on the motor specifications. Thus, the control algorithm was proposed and experimentally demonstrated for effectiveness and applicability under the worst case scenario. The proposed algorithm was successfully employed and has shown excellent performance for the international robot soccer game MiroSot'98 for a vision based soccer robot system held in France.

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Hyun-Sik Shim

Received his B.S., M.S., and Ph.D. degrees in Electrical Engineering, Korea Advanced Institute of Science and Technology, 1991, 1993, 1998, respectively. He is working for LG Traffic Information System. His research interests are mobile robots, intelligent traffic control.

He is a member of IEEE, KITE, and ICASE.



Yoon-Gyeoung Sung

Received his B.S., M.S., and Ph.D. degrees in Mechanical Engineering, Yeungnam University in 1982, Yonsei University in 1985, University of Alabama in 1997, respectively. He had worked for Korea Atomic Energy Institute. Since 2000, He is in School of Mechanical En-

gineering, Yeungnam University as a professor. His research interests are robotics, smart structural control, multibody dynamics, nonlinear control, and machine vision. He is a member of ASME, KSME, and ICASE.