Pattern Spectrum Component Function and Warning Traffic Sign Recognition

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패턴 스펙트럼 성분 함수와 주의 교통 표지 인식

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ABSTRACT

In this paper, a pattern spectrum component function is introduced for an oriented shape analysis and its properties are discussed. It can represent directional information of shape more precisely than the conventional oriented pattern spectrum. An adaptive distance function between two pattern spectrum component functions is presented to recognize different shapes in noise. As a practical application, the pattern spectrum component function is applied to warning traffic sign recognitions utilizing the adaptive distance functions. Favorable results are obtained compared to the oriented pattern spectrum.

요 약

기존의 방향성 패턴 스펙트럼에 비하여 보다 정확하게 방향성 정보를 나타낼 수 있는 패턴 스펙트럼 성분 함수를 도입하고 그 성질을 분석하였다. 그리고 패턴 스펙트럼 성분 함수에 의하여 잡음성 형상을 식별하고차 적응 거리 함수를 제안하였다. 제안한 패턴 스펙트럼 성분 함수를 주의 교통 표지 식별에 실제 응용하여 적응 거리 함수에 의하여 평가한 본 결과 방향성 패턴 스펙트럼에 비하여 보다 만족할 만한 결과를 얻을 수 있었다.

I. Introduction

論文番號:96054-0209 接受日字:1996年 2月 9日 The shape representation and shape-size description are very important in image processing and computer vision [1]. Mathematical morphology provides an efficient approach to description and analysis of shapes [2-4]. In recent decade, many methods for shape analysis based on the mathematical morphology have been proposed [5-10], which can be classified into two categories shape structure enhancement and quantitative

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shape description. The pattern spectrum, also called a morphological shape-size histogram, is an important tool for shape representation in morphological image analysis [3, 6]. It is a quantitative description of shape, derived from the morphological size distribution (also called "granulometeries" in [2, 10]).

In recent researches, Goustias proposed a generalized form of pattern spectrum for multi-structuring elements [7], Shih a geometric spectrum based on the morphological skeleton transformation [11], Regazzoni a statistical pattern spectrum [12], and Zhou a high order pattern spectrum [13]. However, an oriented information of shape has not been respected in these researches because the employed structuring elements (SEs) such as octagon, square and rhombus are not adequate to linear directional shapes.

In this paper, the pattern spectrum component function is introduced to represent a directional information which is difficult to be described by the formal pattern spectrum. And its properties are discussed.

II. Pattern Spectrum and Oriented Pattern Spectrum

2.1 Pattern Spectrum

Let I be a compact continuous binary image, and let B be a continuous binary pattern, called the SE. Then, the basic morphological operations are represented as follows

dilation:
$$I \oplus B = \{a : \hat{B}_a \cap I \neq \emptyset\}$$
,
erosion: $I \ominus B = \{a : B_a \subseteq I\}$
opening: $I \circ B = (I \ominus B) \oplus B$,
closing: $I \bullet B = (I \oplus B) \ominus B$,

where $\hat{B} = \{-b; b \in B\}$ and B_a is the translated B by a. Then, the pattern spectrum of I with respect to B is

$$PS(I, B, r) = \begin{cases} -\frac{dA(I \circ rB)}{dr} , & r \ge 0 \\ -\frac{dA(I \bullet rB)}{dr} , & r < 0 \end{cases}$$
 (1)

where A(I) denotes the area of I and $rB = \{rb; b \in B\}$.

The pattern spectrum can describe the following informations of shape 1:

- 1. The lower size parts of the pattern spectrum represent boundary roughness in I relative to B.
- 2. The isolated impulses in the pattern spectrum illustrate long capes or bulky protruding parts in I.

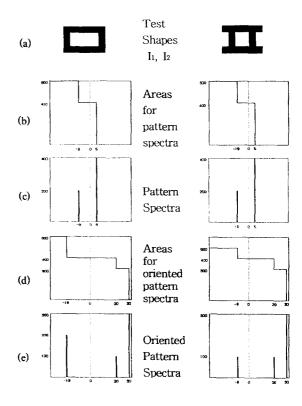


Fig. 1 Examples of pattern spectra and oriented pattern spectra. (a) Two test images Ii (i = 1, 2) similar to Korean consonants of \square and \square , with the same areas and widths of 400 and 5, respectively, (b) Area functions of Ii rB for $r \ge 0$ and Ii \bullet rB for r < 0, (c) Pattern spectra of PS(Ii, B, r), (d) Area functions of $\bigcup_{\sigma} (\text{Ii} \circ r L_{\sigma})$ for $r \ge 0$ and $\bigcap_{\sigma} (\text{Ii} \bullet r L_{\sigma})$ for r < 0, (d) Oriented pattern spectra of OPS(Ii, r),

given as follows [6]

- 3. PS(I, B, r)/A(I) represents the maximal degree that I contains the pattern rB.
- 4. The big impulses at negative r illustrate the existence of prominent intruding gulfs and holes in I.

However, in most applications of the pattern spectrum, the typical binary area shapes, such as circle, square, and rhombus, are chosen as the SEs. Fig.1(a), (b) and (c) show examples of pattern spectrum using a 3×3 square SE, where we have used two shapes of Korean consonant styles such as \square and \square with the same width of 5 within 20×30 rectangle. We see that they have the same pattern spectra and thus it is impossible to discern between them.

2.2 Oriented Pattern Spectrum

To enable the pattern spectrum to extract directional informations of shape, Maragos proposed an oriented pattern spectrum, denoted OPS(I, r), as follows [6].

$$OPS(I, r) = \begin{cases} -\frac{dA(\bigcup_{\theta} (I \circ rL_{\theta}))}{dr}, & r \geq 0 \\ -\frac{dA(\bigcap_{\theta} (I \bullet rL_{\theta}))}{dr}, & r < 0 \end{cases}$$
 (2)

where L_{θ} denotes an unit-length line segment SE passing through the origin and forming an angle θ with the horizontal $(0 \le \theta \le 2\pi)$.

Fig. 1(d) and (e) show the results of oriented pattern spectra corresponding to Fig. 1(a), where we have used four directional line segment SEs:0°{(0, 0)-(1, 0)}, 45°{(0, 0)-(1, 1)}, 90°{(0, 0)-(0, 1)}, 135°{(0, 0)-(-1, 1)}. The result indicates that two shapes consist of line segments of the same lengths of 20 and 30, and that they have rectangular holes of 20×10 and 10×10 , respectively. But it does not inform about any oriented angle. The union and intersection operations over θ in Eq. (2) give rise to lose each directional information.

III. Pattern Spectrum Component Function

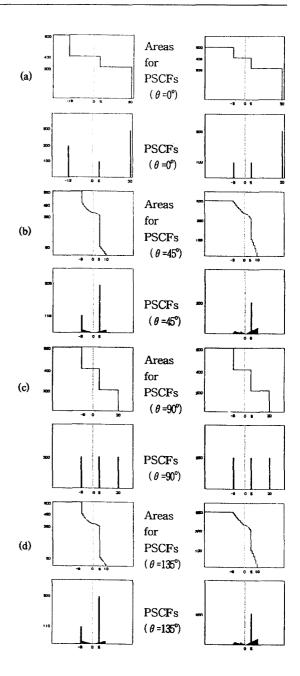


Fig. 2 PSCFs for θ = 0°, 45°, 90°, 135° of Fig. 1(a). (a) The upper left and right graphs represent area functions of Ii ∘ rL_θ for r ≥ 0 and Ii • rL_θ for r < 0 when θ = 0°, corresponding to □ and □ of Fig. 1(a), respectively, and the lower are their PSCFs. In this manner, the area functions and PSCFs for θ = 45°, 90°, and 135° are depicted in (b), (c), and (d), respectively.</p>

To alleviate the problem of losing directional informations, we adopt a new approach to keeping θ in Eq. (2) alive. We define a function, called a pattern spectrum component function (PSCF), denoted PSC (I, θ , r), as

$$PSC(I, \theta, r) = \begin{cases} -\frac{-dA(I \circ rL_{\theta})}{dr}, & r \ge 0\\ -\frac{-dA(I \bullet rL_{\theta})}{dr}, & r < 0 \end{cases}$$
(3)

which can be also considered as a special type of pattern spectrum by adopting a line segment SE L_{θ} instead of area SE B in Eq. (1).

Fig. 2 shows the results of PSCFs using the same four L_{θ} 's $(\theta = 0^{\circ}, 45^{\circ}, 90^{\circ}, 135^{\circ})$ as used in the oriented pattern spectrum in Fig. 1(d). We see that the four PSCFs are much different with θ and that the PSCFs of two shapes π and π are distinguishable for the cases of $\theta = 0^{\circ}$, 45° and 135° except for $\theta = 90^{\circ}$.

3.1 Properties of PSCF

1. Non-negative.

Each element of PSCF is positive:

 $PSC(I, \theta, r) \ge 0$ for $\forall r$ and $\forall \theta$.

2. Energy identity.

The sum of PSCF of a shape at any direction θ equals to the total area of the shape:

$$\int_0^\infty PSC(I, \theta, r) dr = A(I) \text{ for } \forall \theta.$$

3. Translation invariance.

The PSCF is translation invariant on I:

 $PSC(I_d, \theta, r) = PSC(I, \theta, r)$ for $d \in \mathbb{R}^2$

4. Rotation properties.

① PSC(Rot(I,
$$\alpha$$
), θ , r) = PS(I, $\theta + \alpha$, r),

where Rot(I, α) expresses the counterclockwise rotated I by an angle α .

5. Periodicity.

The PSCF is a periodic function with respect to θ with a period of π :

$$PSC(I, \pi + \theta, r) = PSC(I, \theta, r).$$

6. Symmetries.

- ① If I is symmetric on the direction α , its PSCF is symmetric on the direction α , too.
- ② If I is symmetric with J on the direction α , then

$$PSC(J, \theta, r) = PSC(I, 2\alpha - \theta, r).$$

7. Additivity.

For a mutually exclusive set, i.e., if $I = I_1 \cup I_2$ $\cup ... \cup I_N$ and $I_i \cap I_j = \Phi$ for $i \neq j$, then

$$PSC(I, \theta, r) = \sum_{n} PSC(I_n, \theta, r) \text{ for } r \ge 0.$$

3.2 PSCF of Discrete Binary Image

Let X be a finite-extent discrete binary image. Then, its PSCF at discrete θ can be similarly obtained from Eq. (3) by exchanging the differential area and the real number r by the difference of cardinality and an integer n, respectively, as

$$PSC(X, \theta, n) = \begin{cases} Card(X \circ nL_{\theta} \setminus X \circ (n+1)L_{\theta}), & n \ge 0 \\ Card(X \bullet (-n)L_{\theta} \setminus X \bullet (-1-n)L_{\theta}), & n < 0 \end{cases}$$
(4)

where Card(X) denotes the cardinality (the total number of elements) of X, \setminus set difference, and nL_{θ} the origin set $\{o\}$ dilated by L_{θ} n times, i.e.,

$$nL_{\theta} = (\cdots ((\{o\} \oplus L_{\theta}) \oplus L_{\theta}) \cdots) \oplus L_{\theta}$$
. Note that $0L_{\theta} = \{o\}$.

The PSCF of X at any angle θ is, similarly as stated in rotation property, equal to that of Rot(X, θ) at zero angle. We can thus rewrite Eq. (4) as follows.

$$PSC(X,\;\theta,\;n) = \begin{cases} Card(Rot(X,\;\theta)\circ nL_0\backslash Rot(X,\;\theta) \\ & \circ (n+1)\,L_0), \qquad n \geq 0 \\ \\ Card(Rot(X,\;\theta)\bullet (-n)\,L_0\backslash Rot(X,\;\theta) \\ & \bullet (-1-n-L_0), \qquad n \leq 0 \end{cases}$$

3.3 Adaptive Distance Function

For comparison of two PSCFs, we adopt a distance function based on mean square error as

$$D(X, Y) = \sqrt{\sum_{\theta} w(\theta) \sum_{n} (PSC(X, \theta, n) - PSC(Y, \theta, n))^{2}}$$
(5)

where $w(\theta)$ is a positive weighting factor with $\sum_{\theta} w(\theta)$ = 1. As the distance is smaller, the shape X resembles Y more closely.

In consideration of noisy shapes, we develop an adaptive algorithm to be robust to scale changes modifying Eq. (5) as follows

Adaptive Distance Function

For each
$$\theta$$
, do:
{ for each n, compute

$$T = \min_{m}^{min} \{(PSC(X, \theta, n) - PSC(Y, \theta, m))^2;$$

$$\leq |m - n| \leq N_1\};$$

$$d(\theta) = d(\theta) + T;$$

$$mark PSC(Y, \theta, m') \text{ as visited,}$$

$$which corresponds to T.$$
for each m' not visited, compute

$$d(\theta) = d(\theta) + \min_{k}^{min} \{(PSC(Y, \theta, m') - PSC(X, \theta, k))^2;$$

$$|m' - k| \leq N_1\};$$
Finally, adaptive distance

$$D_a(X, Y) = \sqrt{\sum_{\theta} w(\theta) d(\theta)}$$
(6)

Note that the search interval N_1 in the adaptive distance function is assumed to be very small positive integer, for example, $N_1 = 1$ or 2, and that this adaptive distance function is not commutative, i.e., $D_a(X, Y) \neq D_a(Y, X)$.

We can use the adaptive distance function for the pattern spectrum PS() in Eq. (1) and the oriented spectrum OPS() in Eq. (2) by exchanging the differential area and the real number r for the difference of cardinality and an integer n, respectively. Of course, in the adaptive distance function, it requires only one repetition process with respect to θ , since θ is not

variable but fixed.

IV. Experimental Results

To test performances of shape recognitions using the pattern spectrum PS() in Eq. (1), the oriented spectrum OPS() in Eq. (2), and pattern spectrum component function PSC() in Eq. (3), simulations are carried out for recognition of 22 symbols in the Korean warning traffic signs on road.

Fig. 3 shows 22 reference symbols (Xi's) and filtered noisy symbols (Yi's), which are first corrupted by 10% salt and pepper noise and then filtered by morphological open-close operation using 3×3 square SE.

With the reference symbols and noisy symbols in Fig. 3, respectively denoted by Xi and Yi, we have computed adaptive distances $D_a(Y_i, X_j)$ in Eq. (6) (i, j = 1, 2, ..., 22).

Table 1 shows adaptive distances $D_a(Y_i, X_j \text{ in Eq.}$ (6) using pattern spectrum component functions in Eq. (3) with $\theta = 0^{\circ}$, 45° , 90° , and 135° . Here we consider Y_i as X_k when the k-th element is the smallest, which is marked by underline, among all elements of the i-th row. In Table 1, there are four symbols mistaken by others: Y_5 as X_8 , Y_{16} as X_{15} , Y_{17} as X_{15} , and Y_{21} as X_{20} . We can interpret these errors by rotation invariant property of pattern spectrum component functions as noted in section 3.1 since X_5 and X_{21} are rotated X_4 and X_{20} by an angle 1800, respectively, and both X_{16} and X_{17} are in some degree similar to X_{15} in directional pattern spectrum components of $\theta = 45^{\circ}$, 90° , and 135° .

Similarly Table 2 and 3 show adaptive distances using oriented pattern spectra in Eq. (2) with $\theta = 0^{\circ}$, 45° , 90° , and 135° , and using pattern spectra in Eq. (1) with 3×3 square SE, respectively. There are, in Table 2 and 3, nine and sixteen symbols mistaken by others, respectively.

With these failure rates of recognitions, the proposed pattern spectrum component function shows the best performance, while the pattern spectrum is the

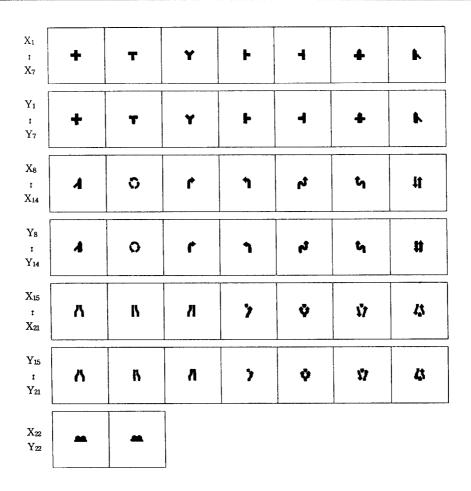


Fig. 3 Reference symbols (X_i) and their filtered noisy symbols (Y_i) for $i = 1 \sim 22$.

worst.

In fact two shapes rotated by an angle 180°, each spectrum results in the same result. But as we see in Table 1, 2, and 3, it is not so. This tells us that the above three algorithms are not much robust to noise. This may be improved by normalizing T by n in adaptive distance function since it can reduce the noisy effect for long capes or long holes.

V. Conclusions

In this paper, the PSCF is introduced and its properties are discussed. The PSCF can represent oriented

informations of the shape, and is more suitable to describe the shape of object than both the oriented pattern spectrum and the pattern spectrum. And with the proposed adaptive distance function, the PSCF can recognize 18 warning symbols among 22 in noise. The PSCF may be very attractive to analysis of the other traffic signs, especially, indicatory signs, since all of them consist of directional shapes. However rotated symbols such as \leftarrow and \rightarrow , \vdash and \dashv , etc., and some symbols of equal directional components such as \leftarrow and \rightarrow , \rightarrow and \rightarrow , etc., can not be made a distinction between them.

246 524 387 534 540 190 266 226

282

0

0

0

х

0

Reference Symbols Xi ($i = 1, 2, \cdots, 22$) Υi failure 22 8 9 10 11 12 13 14 15 17 18 19 5 6 16 118 162 264 300 307 318 291 295 374 356 354 395 399 680 608 690 741 288 362 424 406 n 453 249 169 273 337 345 324 285 311 356 258 261 303 298 591 574 673 658 295 344 356 429 387 0 343 342 149 377 387 387 355 373 366 321 323 342 342 657 539 644 711 267 305 406 406 392 0 269 224 318 146 154 448 256 257 392 328 335 421 436 679 592 680 751 299 366 431 442 439 0 309 267 324 311 317 397 301 287 382 383 389 435 445 695 617 704 768 362 419 456 477 х 368 375 368 476 483 <u>101</u> 274 286 425 424 421 426 431 733 643 721 789 440 454 498 555 n 90 265 411 413 427 394 394 714 615 704 762 452 506 492 541 450 420 437 484 491 324 463 0 7 | 434 411 395 479 486 353 308 <u>138</u> 441 431 423 385 403 732 609 698 778 444 502 506 527 451 0 8 415 378 335 415 424 450 391 411 124 305 297 300 322 595 390 491 629 312 315 262 293 0 9 353 271 245 238 248 455 363 382 370 145 178 257 244 480 533 646 543 221 296 312 394 0 10 348 270 275 235 241 483 307 315 372 288 <u>217</u> 338 321 538 598 690 644 301 352 382 430 0 11 386 309 281 392 399 448 389 384 350 251 264 <u>177</u> 198 513 444 571 580 269 337 246 322 n 12 404 319 298 398 406 476 400 416 353 242 270 196 183 518 435 559 584 274 319 284 325 0 13 555 469 550 412 413 700 644 659 607 388 377 376 362 175 636 727 357 444 520 381 490 0 546 467 422 492 500 604 541 540 340 314 307 264 258 486 <u>189</u> 370 458 305 322 249 232 x 15 16 613 591 504 625 632 644 588 594 376 362 343 345 299 306 178 181 327 481 454 383 289 х

656 523 544 419 421 694 639 659 531 384 394 407 391 288 <u>186</u> 206 223 374 475 406 316

|413 364 313 395 400 509 448 438 377 354 345 388 378 556 458 553 611 284 <u>153</u> 326 354

500 371 402 424 430 586 478 477 334 254 282 242 262 439 312 454 468 231 318 <u>146</u> 157

| 477 362 367 399 406 527 449 452 326 249 242 228 235 463 317 446 503 250 286 <u>129</u> 183 541

458 462 390 528 536 428 471 473 463 438 444 449 462 763 581 709 770 458 411 557 549 176

Table 1. D_a(X_i, X_j) using the pattern spectrum component functions.

Table 2. D_a(X_i, X_i) using the oriented pattern spectra.

307 256 234 327 337 429 374 388 293 198 246 227

18

19

Yi	F	Reference Symbols Xi (i = 1, 2, ···, 22)														failure							
11	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	Tantac
1	61	50	236	193	207	_48	110	116	335	155	153	226	225	61	298	150	143	221	533	257	286	208	x
2	80				245		75					187			291						289	204	x
3	316	313				313														334			x
4	1000					228								232							278	195	0
5	239													238						324		306	x
6	49			227				134					252	57						270		204	0
7	128					122								129							271	232	0
8		201				201								_						290		283	0
9					295									273						222		246	0
10	1													209						282		116	0
11	1					178								170		89				245		132	0
12	1																			284		305	X
13	1																				251	293	0
14	92				253																278	166	0
15																				324			1 -
16						210														268		_	
17	1					187				66	_			160						270			1 -
18	1																			136			
19											Г									433			1
20														247						_58			0
21														253						128			.1
22	102	157	2/0	176	186	156	213	211	321	6/	70	253	257	156	193	142	98	202	413	272	277	129	x

Yi	ŀ	Refer	ence	Syn	nbols	Xi	(i	= 1,	2,		. , 22	2)		-									failuma
	1.	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	failure
1	777	303	377	544	553	648	730	738	847	327	331	518	528	637	10+	11+	603	435	315	645	833	798	x
2	851	191	<u>131</u>	594	604	844	482	489	836	281	325	644	660	781	10+	11+	746	369	333	713	807	854	x
3	908	283	<u>164</u>	633	644	850	493	505	567	226	214	605	639	799	683	740	763	198	350	505	442	809	0
4												884											
5												959											1
6												909											_
7												10+											
8												10+											1
9									*****			218											1 -
10												224											
11												565											
12												422						-					_
13	1											342											x
14												307											L
15												185											
16												103											
17												_93											ř.
18												438											L
19												263											t .
20												326								-			
21												278											
122	114+	1()+	10+	12+	12+	342	11+	11+	10+	10+	-999	11+	11+	13+	12+	12+	12+	989	11+	11+	11+	674	x

Table 3. $D_a(X_i, X_j)$ using the pattern spectra. The symbol +denotes a number of two ciphers, so that for example, 13 + is greater than 1300.

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