The liberation of phosphine ligand during syntheses occurs probably due to the fact the volume of the ligand $I$ is too big to be accommodated by the small vanadium. It is worth noting that the size of the phosphine ligand exerts an influence on the geometry around the vanadium metal center. NMR studies of II and III $^{6.7}$ indicate the difference in the symmetries around the vanadium metal. Complex III, which has $\mathrm{PMe}_{3}$, shows four types of carbon atoms of the benzene ring on its ${ }^{13} \mathrm{C}$-NMR spectra and three types of hydrogen atoms on its ${ }^{1} \mathrm{H}-\mathrm{NMR}$ spectra, indicating that the two phenyl groups are in the same environment. Therefore the coordination sphere of vanadium in III can be described as a pseudotetrahedron. On the other hand, Complex II (a $\mathrm{PEt}_{3}$ ana$\log$ ) exhibits complicated NMR peak-splittings. ${ }^{13} \mathrm{C}-\mathrm{NMR}$ spectra of II exhibit twelve different carbon peaks of the phenyl groups and ${ }^{1} \mathrm{H}-\mathrm{NMR}$ spectra also indicate the existence of two different benzene rings. One carbon atom of the benzene ring even appears as a doublet ( $\delta 123.19$ ) with a coupling constant $J_{C \cdot P}=16.2 \mathrm{~Hz}$. Although at this time we cannot explain clearly why one carbon atom of the benzene ring on the tetrazene ligand backbone couples with the phosphorous atom, the results maybe imply that a larger phosphine ( $\mathrm{PEt}_{3}$ ) induces a more geometrically distorted tetrahedron. Reactivities and other chemistries of these complexes are under study.

Acknowledgement. This work is based on research sponsored by the Korea Science \& Engineering Foundation under grant KOSEF 913-0306-009-1.

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#### Abstract

yst., A32, 751 (1976). 6. Complex n. 'H-NMR ( $\left.\mathrm{C}_{6} \mathrm{D}_{6}, 500 \mathrm{MHz}\right): \delta 7.32\left(\mathrm{t}, 2 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5 r}\right.$ $J=7.4 \mathrm{~Hz}), 7.13\left(\mathrm{t}, 2 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5}, J=7.1 \mathrm{~Hz}\right), 7.06\left(\mathrm{~d}, 2 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5}\right.$, $J=7.23 \mathrm{~Hz}), 6.90\left(\mathrm{t}, 1 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5} J=7.1 \mathrm{~Hz}\right), 6.77\left(\mathrm{t}, 1 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5}\right.$, $J=7.1 \mathrm{~Hz}), 6.48\left(\mathrm{~d}, 2 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{51} J=7.23 \mathrm{~Hz}\right), 1.35(\mathrm{~m}, 6 \mathrm{H}$, $\left.\mathrm{PCH}_{2} \mathrm{CH}_{3}\right), 0.87\left(\mathrm{~m}, 9 \mathrm{H}, \mathrm{PCH}_{2} \mathrm{CH}_{3}\right) ;{ }^{33} \mathrm{C}-\mathrm{NMR}\left(\mathrm{C}_{6} \mathrm{D}_{5}, 500\right.$ MHz ): $\delta 153.78-114.42\left(\mathrm{C}_{6} \mathrm{H}_{5}\right), 18.98$ (td, $\mathrm{PCH}_{2} \mathrm{CH}_{3}, \quad J_{c \cdot \mathrm{H}}$ $\left.=128 . J_{C P}=63.2 \mathrm{~Hz}\right), 6.18\left(\mathrm{qd}, \mathrm{PCH}_{2} \mathrm{CH}_{3}, J_{C \cdot H}=128,{ }^{2} f_{C \cdot P}\right.$ $=4.2 \mathrm{~Hz}) ;{ }^{13} \mathrm{C}|\mathrm{H}| \mathrm{NMR}\left(\mathrm{C}_{6} \mathrm{D}_{56}, 500 \mathrm{MHz}\right): \delta 115.03,116.71$, 118.13, 129.13, 129.34, 147.31, 153.74 (s, $\mathrm{C}_{6} \mathrm{H}_{5}$ ), 123.19 ( d , $\mathrm{C}_{6} \mathrm{H}_{5}, J_{\mathrm{C} \cdot \mathrm{P}}=16.2 \mathrm{~Hz}$ ). MS (El): $412.27\left(\mathrm{M}^{+}-2,2\right), 379.49$ $\left(\mathrm{M}^{+}-\mathrm{Cl}, 11\right), 365.47\left(\mathrm{~V}\left(\mathrm{PEt}^{2}\right) \mathrm{N}_{3} \mathrm{Ph}_{2}, 8\right), 351.45\left(\mathrm{~V}_{\left(\mathrm{PEt}_{3}\right) \mathrm{N}_{2} \mathrm{Ph}}\right.$ $\left.{ }_{2}, 6\right), 337.41\left({ }^{2}\left(\mathrm{PEt}_{3}\right) \mathrm{ClN}_{4} \mathrm{Ph}, 5\right), 235.19\left(\mathrm{~V}\left(\mathrm{NHPh}_{2}, 33\right), 225\right.$. $17\left(\mathrm{VN}_{4}\left(\mathrm{PEt}_{3}\right), 67\right), 212.16\left(\mathrm{~N}_{4} \mathrm{H}_{2} \mathrm{Ph}_{2}, 24\right), 119.06\left(\mathrm{PhN}_{3}, 20\right)$, $105.09\left(\mathrm{PhN}_{2}, 18\right) 93.09\left(\mathrm{NH}_{2} \mathrm{Ph}, 100\right)$. 7. Complex III. ${ }^{1} \mathrm{H}-\mathrm{NMR}\left(\mathrm{C}_{6} \mathrm{D}_{6,} 500 \mathrm{MHz}\right): \delta 6.43$ (d, 4 H , $\left.\mathrm{C}_{6} \mathrm{H}_{5}, J=7.5 \mathrm{~Hz}\right), 6.78\left(\mathrm{t}, 4 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5}, J=7.5 \mathrm{~Hz}\right), 7.14(\mathrm{t}$, $\left.2 \mathrm{H}, \mathrm{C}_{6} \mathrm{H}_{5}, J=7.5 \mathrm{~Hz}\right), 0.925\left(\mathrm{~m}, 9 \mathrm{H}, \mathrm{CH}_{3}\right) ;{ }^{13} \mathrm{C}-\mathrm{NMR}\left(\mathrm{C}_{6} \mathrm{D}_{6}\right.$, $500 \mathrm{MHz}): \delta 129.37\left(\mathrm{dd}, \mathrm{C}_{6} \mathrm{H}_{5}, J_{\mathrm{c} \cdot \mathrm{H}}=156,3_{\mathrm{C} \cdot \mathrm{H}}=8.2 \mathrm{~Hz}\right)$, $118.23\left(\mathrm{dt}, \mathrm{C}_{6} \mathrm{H}_{5}, J_{\mathrm{C} \cdot \mathrm{H}}=160,{ }^{3} \mathrm{~J} \cdot \mathrm{H}=7.4 \mathrm{~Hz}\right), 114.97\left(\mathrm{dt}_{1} \mathrm{C}_{6} \mathrm{H}_{5}\right.$, $\left.J_{\mathrm{C} \cdot \mathrm{H}}=155,{ }^{3} \int_{\mathrm{C} \cdot \mathrm{H}}=6.4 \mathrm{~Hz}\right), 1.32\left(\mathrm{q}, \mathrm{CH}_{3}, J_{\mathrm{C} \cdot \mathrm{H}}=118 \mathrm{~Hz}\right) ;{ }^{13} \mathrm{C}$ (H) NMR ( $\mathrm{C}_{6} \mathrm{D}_{6,} 500 \mathrm{MHz}$ ): $147.16\left(\mathrm{~s}, \mathrm{C}_{6} \mathrm{H}_{5}\right), \delta 129.37$ (s, $\mathrm{C}_{6} \mathrm{H}_{5}$ ), $118.23\left(\mathrm{~s}, \mathrm{C}_{6} \mathrm{H}_{5}\right), 114.97\left(\mathrm{~s}, \mathrm{C}_{6} \mathrm{H}_{5}\right), 1.31\left(\mathrm{~s}, \mathrm{CH}_{3}\right)$. MS (EL): $372.22\left(\mathrm{M}^{+}, 4\right), 336.24\left(\mathrm{M}^{+} \mathrm{Cl}, 6\right), 32332$ (V(PMe) ${ }^{-}$ $\left.\mathrm{N}_{3} \mathrm{Ph}_{2}, 15\right), 296.19\left(\mathrm{M}^{+}-\mathrm{PMe}_{3}, 6\right), 212.11\left(\mathrm{~N}_{4} \mathrm{H}_{2} \mathrm{Ph}_{2}, 5\right), 105$. $08\left(\mathrm{PhN}_{2}, 35\right), 93.09\left(\mathrm{NH}_{2} \mathrm{Ph}, 100\right), 77.06(\mathrm{Ph}, 59)$.


## Synthesis of Prostaglandins II $^{\mathbf{1}}$. Convenient Synthesis of Misoprostol

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Recived July 30, 1992

It is well known that naturally occurring prostaglandins of E-series exhibit powerful gastric antisecretory activity and cytoprotection. ${ }^{2}$ However, their numerous side effects, rapid metabolism, and chemical instability limit their application as a therapeutic agent for the treatment of peptic ulcer disease. Misoprostol 1, the 15 -deoxy-16-hydroxy-16-methylprostaglandin $E_{1}$ is a potent anti-ulcer agent which reduced the critical drawbacks of the natural prostaglandins. ${ }^{3}$ Since its development, a number of synthetic methods for 1 have been reported. In most cases, the synthetic routes to 1 involve, for the introduction of $\omega$-side chain, a 1.4-conjugate addition of an appropriate 16-hydroxy-16-methyl vinyl copper species to the cyclopentenone ring which already has the $\alpha$-side chain. ${ }^{4}$ Here we describe a new efficient synthetic approach to I .

Since the highly efficient method to construct the upper side chain had been available, ${ }^{5}$ our attention was focused upon the introduction of the lower side chain bearing trans-



Scheme 1

(a) DHP/PPTS, $\mathrm{CH}_{2} \mathrm{Cl}_{2}$; (b) DIBAH, $\mathrm{PhCH}_{3}$; (c) $n$ - $\mathrm{BuLi}, \mathrm{PhP}^{+} \mathrm{CH}_{2}$ $\left(\mathrm{CH}_{2}\right)_{3} \mathrm{CH}_{2} \mathrm{OH}, \mathrm{Br}^{-}$; (d) TBSCl, Imidazole, DMF; (e) $\mathrm{H}_{2}, 5 \% \mathrm{Pd} / \mathrm{C}$, $5 \% \mathrm{AcOH}$ in EtOH ; (f) Collins reagent, $\mathrm{CH}_{2} \mathrm{Cl}_{2}$; (g) $n$-BuLi, 8, $\mathrm{Ph}_{3} \mathrm{P}^{+} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{C}\left(\mathrm{CH}_{3}\right)(\mathrm{OH}) \mathrm{CH}_{2}\left(\mathrm{CH}_{2}\right)_{2} \mathrm{CH}_{3} \mathrm{I}^{-}$; (h) TBAF, THP; (i) PDC, DMF; $\mathrm{CH}_{2} \mathrm{~N}_{2}, \mathrm{Et} 2 \mathrm{O}$; (j) $\mathrm{AcOH} / \mathrm{H}_{2} \mathrm{O} /$ THF (20: $10: 3$ ); (k) $n$-BuLi, $\left.\mathrm{PhSO}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{C}_{2} \mathrm{CH}_{3}\right)\left(\mathrm{OTHP}^{2}\right) \mathrm{CH}_{2}\left(\mathrm{CH}_{2}\right)_{2} \mathrm{CH}_{3}$; then $\mathrm{Ac}_{2} \mathrm{O}$; (I) $5 \%-\mathrm{Na}(\mathrm{Hg}) / \mathrm{Na}_{2} \mathrm{HPO}_{4}, \mathrm{MeOH}$

Scheme 2
homoallylic alcohol unit. As outlined in Scheme 1, a key feature of our approach to 1 involves the trans-stereoselective Wittig coupling of the optically active aldehyde 2 , with $\gamma$ oxide ylide 3.
Although non-stabilized phosphonium ylides react with aldehydes to afford largely cis olefin, $\gamma$-oxido ylides exhibit unexpectedly high trans stereoselectivity by intramolecular base ( $\beta$ - or $\gamma$-alkoxide) ${ }^{6}$ or intermolecular base induced (Schlosser method) ${ }^{7}$ equilibration of a Wittig intermediate. Accordingly, we anticipated that misoprostol could be synthesized efficiently by employing trans-stereoselective Wittig coupling strategy.

As shown in Scheme 2, aldehyde 2 was prepared as follows. Protection of Corey lactone benzyl ether 5 as its THP ether, followed by DIBAH reduction delivered the lactol 4 in $94 \%$ yield. Subsequent construction of $\alpha$-side chain was
carried out by the Wittig reaction of the lactol 4 , with the ylide derived from (5-hydroxypentyl)triphenylphosphonium bromide and $n$-BuLi to afford the diol 6, in $74 \%$ yield. The diol 6 was converted into the aldehyde 2 by a three step sequence; protection of the diol 6 as di-f-butyldimethylsilyl ethers (TBS), concomitant hydrogenolysis and debenzylation by treatment with $\mathrm{H}_{2}$ in the presence of $5 \% \mathrm{Pd} / \mathrm{C}$, and $\mathrm{Col}-$ lins oxidation of the corresponding alcohol. With the aldehyde 2 in hand, the next step is the installation of $\omega$-side chain by the trans-selective Wittig coupling of the aldehyde 2 with the $\gamma$-oxido ylide 3, generated by treatment of (3-hy-droxy-3-methyl)heptyltriphenylphosphonium iodide 8 with $n$ BuLi.

Reaction of (3-hydroxy-3-methyl)heptyltriphenylphosphonium iodide ( $8,80 \mathrm{mg}, 0.15 \mathrm{mmol}$ ) with $n-\mathrm{BuLi}(0.336 \mathrm{mmol})$ in THF ( 1 m ) at room temperature for 30 min afforded the deep red $\gamma$-oxido ylide solution. The solution was cooled to $-78^{\circ} \mathrm{C}$ and treated with a solution of aldehyde ( 2,43 $\mathrm{mg}, 0.077 \mathrm{mmol}$ ) in THF ( 0.4 ml ) at that temperature. The mixture was allowed to warm to room temperature over 1 h. The mixture was poured into ice-water and extracted with ether. The ether solution was dried and purified by flash column chromatography (EtOAc/hexane $=1: 3$ ) to afford 9 ( $33 \mathrm{mg}, 64 \%$ ) exclusively. ${ }^{1} \mathrm{H}-\mathrm{NMR}\left(200 \mathrm{MHz} \mathrm{CDCl}_{3}\right.$ ); 85.45 ( $\mathrm{m}, 1 \mathrm{H}, \mathrm{C}_{14}$ ), 5.36 (dd, $J=14.8 \mathrm{~Hz}, 8.9 \mathrm{~Hz}, 1 \mathrm{H}, \mathrm{C}_{13}$ ), 4.51 and 4.69 (two br. s, 1H, -OTHP) 4.05 (m, 1H), 3.82 (m, 2H, -OTHP), 3.54 (t, $J=6.6 \mathrm{~Hz}, 2 \mathrm{H}, \mathrm{C}_{1}$ ), $3.39(\mathrm{~m}, 1 \mathrm{H}), 0.84(\mathrm{~s}$, 21 H ), 0.00 ( $\mathrm{s}, 12 \mathrm{H}$ ). IR (neat); 3459, 2930, 2857, 1466, 1253, $1100 \mathrm{~cm}^{-1}$.

The stereochemistry of the double bond was confirmed as trans by the coupling constant ( 14.8 Hz ) in the ${ }^{1} \mathrm{H}-\mathrm{NMR}$ spectrum. From this point of view, it should be noted that the presence of the hydroxy group in phosphonium salt 8 is critical for the trans-selective Wittig reaction, wherein deprotonation/equlibriation of the intermediate betaine is effected by the basic alkoxide. ${ }^{6.7}$

16-Hydroxy group of 9 was protected as THP ethers to give 10. The trans stereochemistry of double bond in $\mathbf{1 0}$ was again proved by unambiguous synthesis of 11, and then 10 (overall $42 \%$ from the aldehyde 2 ) employing Julia olefin$a^{2}{ }^{8}$ as shown in Scheme 2.

Deprotection of the silyl ether and subsequent oxidation of the diol 6 with pyridinium dichromate (PDC) followed by methylation with diazomethane gave the 9-keto-ester. Finally, the THP groups were removed by treatment with acetic acid in aqueous THF to afford misoprostol 1. The spectral data of misoprostol, thus obtained, were in complete agreement with those reported earlier. ${ }^{\text {d.c }}$

In summary, we have developed a new synthetic route to misoprostol using a trans-stereoselective Wittig reaction as a key step. The whole synthesis comprises 11 steps from Corey lactone benzyl ether and proceeds in $\sim 13 \%$ overall yield. This synthetic route may also provide substantial flexibility for the synthesis of $\mathbf{1 5}$-deoxy-16-hydroxy prostaglandin analogues.

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## Mixed Amplitude and Phase Grating Effect in Forced Rayleigh Scattering

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Received August 8, 1992

Although the forced Rayleigh scattering (FRS) has recently emerged as a powerful tool for the study of mass diffusion in various media, ${ }^{1-9}$ there still remain some aspects of the technique which seem to deserve further attention. The technique utilizes the diffraction from a transient concentration fringe pattern created by a photo-reaction of appropriate photoprobe. In order for the concentration fringe to diffract the light, the product of the photo-reaction (shifted state) should possess a different optical properties from the unshifted state either in absorptivity (amplitude grating) or in refractive index (phase grating). ${ }^{10-12}$ If the transient sinusoidal concentration fringe decays by the Fickian diffusion process, the diffracted optical filed decays exponentially following the functional form, $E_{d}=A \exp (-t / t)$.

However, deviations from the single exponential type decay of diffracted signal have often been observed and the deviation is ascribed to the difference in the decay time constants of a pair of complementary gratings which consist of excess optically shifted and unshifted state of the photoprobe. ${ }^{5,6,9,12,13}$ Under this circumstance, the time-varying diffracted intensity has been analyzed by the following model function.

$$
\begin{equation*}
I_{d}(t)=\left[A_{1} \exp \left(-t / \tau_{1}\right)-A_{2} \exp \left(-t / \tau_{2}\right)\right]^{2}+B \tag{1}
\end{equation*}
$$

where $\tau_{1}$ and $\tau_{2}$ are the respective decay time constants of two complementary gratings, $B$ is the baseline, and $A_{1}$ and $A_{2}$ represent the amplitude of optical fields diffracted from each complementary grating. The negative sign arises from the fact that two gratings are $180^{\circ}$ out of phase, but it is only valid for either pure phase (contrast in refractive index) or amplitude (contrast in absorptivity) grating. ${ }^{1122}$ Otherwise, it is necessary to include one more parameter, i.e., the phase difference between two diffracted optical fields from each grating in order to describe the FRS decay profile. ${ }^{3,911: 12}$ The amplitude and phase grating contribution to the diffraction was well demonstrated previously in the other type of transient optical grating experiment, ${ }^{10}$ however, the mixed grating effect exhibits itself in a somewhat different fashion in FRS.

For an unslanted grating, the coupled-wave theory gives the diffracted optical field, $E_{d}$ from a weak diffraction grating. ${ }^{3.10,11}$

$$
\begin{equation*}
E_{d} \propto[-i(\Delta n)+(\Delta k)] \tag{2}
\end{equation*}
$$

where $\Delta n$ and $\Delta k$ are the gratings peak-null differences in real and imaginary part of complex refractive index, respectively. Eq. (2) shows that a pure amplitude grating ( $\Delta n=0$ ) introduces no phase shift while light diffracted from a pure phase grating ( $\Delta k=0$ ) is shifted by $-\pi / 2$. For an arbitrary grating in the weak grating limit, the phase shift is given by

$$
\begin{equation*}
\varphi=\sin ^{-1}\left(-\Delta n /\left[(\Delta n)^{2}+(\Delta k)^{2}\right]^{1 / 2}\right) \tag{3}
\end{equation*}
$$

This phase information is lost in the detection of diffracted light from a single grating by a square-law detector such as a photomultiplier. However, the phase shift leads to a distinct departure from a simple exponential decay when the complementary grating effect is visible. For a mixed amplitude and phase grating, Eq. (1) should be written as

$$
\begin{aligned}
I_{d}(t)= & \left|E_{d}(t)\right|^{2} \\
= & {\left[A_{1} \exp \left(-t / \tau_{1}\right)+A_{2} \exp \left(-t / \tau_{2}\right) \exp (i \Delta \varphi)\right] \times } \\
& {\left[A_{1} \exp \left(-t / \tau_{1}\right)+A_{2} \exp \left(-t / \tau_{2}\right) \exp (-i \Delta \varphi)\right]+B(4}
\end{aligned}
$$

where $\Delta \varphi$ is the phase difference between the diffracted optical fields from two complementary gratings, i.e. $\Delta \varphi=\pi+\left(\varphi_{1}\right.$ $-\varphi_{2}$ ). The analysis according to Eq. (4) is not trivial and thus it seems advantageous to choose a photoprobe exhibiting either a pure amplitude or phase grating behavior at the reading beam wavelength. In this case, $\Delta \varphi=\pi$, which reduces Eq. (4) to Eq. (1).

So far the phase effect due to the mixed grating has not been considered for the analysis of FRS decay profiles. This is likely due to one of the following reasons; (1) the both shifted and unshifted state of the photoprobes do not show a significant absorption at the wavelength of reading beam so that most of the experiments have been carried out at near pure phase grating limit, e.g., use of $\mathrm{He} / \mathrm{Ne}$ laser reading beam for most of azobenzene derivatives which absorb negligibly at 632.8 nm wavelength; (2) the decay time constants of complementary gratings (i.e., diffusivities of the shifted and the unshifted states) are the same; (3) the shape of decay profiles is such that it is hard to recognize the existent phase effect. If the effect (3) is operational, analysis of the signal by Eq. (2) could lead to an erroneous result.

As can be seen from the simulation results in Figure 1.

