lactone ( 13 ) ( $200 \mathrm{mg}, 0.9 \mathrm{mmol}$ ) in THF ( 2 ml ) at $-78^{\circ} \mathrm{C}$ under nitrogen was added lithium diisopropylamide ( 1.0 M , $1.0 \mathrm{ml}, 1.0 \mathrm{mmol}$ ) in THF. The reaction mixture was stirred at $-78^{\circ} \mathrm{C}$ for 10 min and allowed to warm to $-45^{\circ} \mathrm{C}$ over 0.5 h . A mixture of diry HMPA ( $192 \mathrm{mg}, 1.1 \mathrm{mmol}$ ) and methyl iodide ( $890 \mathrm{mg}, 6.3 \mathrm{mmol}$ ) in THF ( 1 m ) was added dropwise to the enolate solution at $-45^{\circ} \mathrm{C}$ and the resulting solution was warmed to $-20^{\circ} \mathrm{C}$ for 0.5 h , and quenched with saturated $\mathrm{NH}_{4} \mathrm{Cl}$, dried ( $\mathrm{MgSO}_{4}$ ), and evaporated to dryness. The residue was subjected to silica gel column chromatography with hexane-ethyl acetate (3: 2) as an eluant to yield the methylated lactone ( 224 mg ) in $92 \%$ yield: NMR $\left(\mathrm{CDCl}_{3}\right) \delta 0.89$ (brt, $J=5 \mathrm{~Hz}, 3 \mathrm{H}$, $\mathrm{CH}_{3}$ ), 1.27 (br s, 19H, $\mathrm{CH}_{2}, \mathrm{CH}_{3}$ ), $1.45-2.10\left(\mathrm{~m}, 4 \mathrm{H}, \mathrm{CH}_{2}\right)$, 2.25-2.65 (m, 1H, $\mathrm{CHC}=0$ ), 4.00-4.40 (m, 1 H, OCH); IR $(\mathrm{NaCl}) 1735(\mathrm{C}=\mathrm{O}) \mathrm{cm}^{-1}$.
2-Methyl-2-hydroxymethyl-5-nonylpentanolide, isomalyngoll de (3). To a solution of the lactone (14)( $200 \mathrm{mg}, 0.8 \mathrm{mmol}$ ) in THF ( 3 ml ) at $-78^{\circ} \mathrm{C}$ under nitrogen was added lithium diisopropylamide ( $1.0 \mathrm{M}, 0.9 \mathrm{~m} /, 0.9 \mathrm{mmol}$ ) in THF. The reaction mixture was stirred at $-78^{\circ} \mathrm{C}$ for 0.5 h , warmed to $-20^{\circ} \mathrm{C}$, and treated with formaldehyde generated from paraformaldehyde ( 0.5 g ) at $180^{\circ} \mathrm{C}$. After all the paraformaldehyde was consumed, stirring was continued for an additional 0.5 h . The reaction mixture was quenched with oxalic acid and extracted with ethyl ether. The ether extracts were washed with brine, dried, and condensed under reduced pressure. The residue was subjected to silica get column chromatography with hexane-ethyl acetate (2:1) as an eluant to give isomalyngolide ( $135 \mathrm{mg}, 59 \%$ ) along with the starting material ( $54 \mathrm{mg}, 27 \%$ ): NMR ( $\mathrm{CDCl}_{3}$ ) $\delta 0.89$ (br t, J=5 Hz, $3 \mathrm{H}, \mathrm{CH}_{3}$ ), 1.27 (br $s, 19 \mathrm{H}, \mathrm{CH}_{2}, \mathrm{CH}_{3}$ ), $1.45-2.20\left(\mathrm{~m}, 4 \mathrm{H}, \mathrm{CH}_{2}\right), 2.95$ (br s, 1H, OH), 3.59 (br $s, 2 \mathrm{H}$, $\left.\mathrm{OCH}_{2}\right), 4.15-4.60(\mathrm{~m}, 1 \mathrm{H}, \quad \mathrm{CHC}=\mathrm{O}) ; \quad \mathrm{IR}(\mathrm{NaCl}) 3450$ $(\mathrm{OH}), 1720(\mathrm{C}=\mathrm{O}) \mathrm{cm}^{-1}$.

Anal. Calcd for $\mathrm{C}_{16} \mathrm{H}_{30} \mathrm{O}_{3}: \mathrm{C}, 71.07 ; \mathrm{H}, 11.18$. Found: C , 71.42; H, 11.43.

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# Determination of Rate Constants in Competitive Consecutive (Series)Second-Order Reaction 

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The kinetics of the reactions of the type $A+B \xrightarrow{k_{1}} C+E$ and $B+C \xrightarrow{k_{2}} D+F$ has been analyzed and a method of obtaining approximate values of $k_{1}$ and $k_{2}$ for the cases where $k_{2}>k_{1}$ is proposed.

## Introduction

Several detailed numerical procedures have been given for the experimental determination of the individual rate stants $k_{1}$ and $k_{2}$ in the kinetic systems consisting of two comconpetitive consecutive (series) irreversible second-order
reactions.

$$
\begin{aligned}
& A+B \xrightarrow{k_{1}} C+E \\
& C+B \xrightarrow{k_{2}} D+F
\end{aligned}
$$

Frost and Schwemer ${ }^{1}$ developed a method for extracting
the values of $k_{1}$ and $k_{2}$ solely from a knowledge of the concentrations of $A$ or $B$ as a function of time, which applies to the case of equivalent initial concentrations (e. g., $B_{0}=$ $2 A_{0}$ ). McMillan ${ }^{2}$ developed a method of obtaining the ratio $K=k_{2} / k_{1}$ from a knowledge of the concentration pair of two components at a single time. They are useful mainly for the cases where $K$ is rather small,

In the present work, an approximation method of obtaining $k_{1}$ and $k_{2}$ that applies for the cases of large values of $K$ is proposed.

## Kinetic Expressions

The pertinent rate equations are

$$
\begin{align*}
& \frac{d A}{d t}=-k_{1} A B  \tag{1}\\
& \frac{d B}{d t}=-k_{1} A B-k_{2} B C=-k_{1} B(A+K C)  \tag{2}\\
& \frac{d C}{d t}=k_{1} A B-k_{2} B C \tag{3}
\end{align*}
$$

where A, B and C represent the molar concentrations of the corresponding chemical species. From the material balance conditions

$$
\begin{align*}
& A_{0}=A+D+C  \tag{4}\\
& 2 A+C-B=2 A_{0}-B_{0} \equiv 2 a \tag{5}
\end{align*}
$$

and the known solution ${ }^{3}$ in the form of implicit function of time

$$
\begin{equation*}
\frac{C}{A_{0}}=\frac{1}{K-1} z\left(1-z^{k-1}\right) \tag{6}
\end{equation*}
$$

where $z \equiv A / A_{0}$, the concentrations of $B$ and $D$ can be expressed in terms of $z$ as

$$
\begin{equation*}
\frac{D}{A_{0}}=1-\frac{K}{K-1} z+\frac{1}{K-1} z^{K} \tag{7}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{B}{A_{0}}=\frac{1}{K-1} z\left[(2 K-1)-z^{K-1}\right]-2 a / A_{0} \tag{8}
\end{equation*}
$$

In particular, for the case where $K=1$, the corresponding equations are given by

$$
\begin{align*}
& \frac{C}{A_{0}}=-z \ln z \\
& \frac{D}{A_{0}}=1-z+z \ln z  \tag{t}\\
& \frac{B}{A_{0}}=2 z-z \ln z-2 a / A_{0}
\end{align*}
$$

The term $(A+K C)$ appearing in Eq. (2) can also be expressed in terms of $z$ as

$$
\begin{align*}
A+K C & =\frac{2 K-1}{K-1} A-\frac{K A_{0}}{K-1} z^{K} \\
& =2 A+C-A_{0} z^{K}=B+2 a-A_{0} z^{K} \\
& =2 A_{0}-\left(B_{0}-B\right)-A_{0} z^{K}=(B+2 a)-A_{0} z^{K} \tag{9}
\end{align*}
$$

It is worth noting that the maximum value of $C$ occurs at

$$
\begin{equation*}
z_{\max }=\left(\frac{1}{K}\right)^{\frac{1}{K-1}} ; C_{\max }=A_{0} z_{\max }^{k} \tag{10}
\end{equation*}
$$

and the maximum value of $C$ is equal to $A_{0}\left(\frac{1}{K}\right)^{\frac{K}{X-1}}$.

Thus, the larger the value of $K$, the closer the value of $z_{\text {max }}$ to unity; namely, if $K$ is large, the maximum of $C$ occurs at the initial stage of the reaction and the value of $K C$ is always comparable to A for $z \approx z_{\max }\left(K C_{\max }=A_{0}\left(\frac{1}{K}\right)^{\frac{1}{R-1}}=A_{0} z_{\text {max }}\right)$, although the value of $C_{\text {max }}$ itself is small (see Table 1 and Figure 1).

## Kinetic Equations for $\boldsymbol{B}$

Eq. (2) can be rewritten, by using Eq. (9), as

$$
\begin{align*}
-\frac{d B}{d t} & =k_{1}\left[1+\frac{K}{K-1}\left(1-z^{K-1}\right)\right] A B \\
& =k_{1} A_{0} B\left[\frac{2 K-1}{K-1} z-\frac{K}{K-1} z^{K}\right] \\
& =k_{1} B\left[(B+2 a)-A_{0} z^{K}\right] \tag{11}
\end{align*}
$$

which holds if $K \neq 1$. On the other hand, combination of Eq. (5) and (6) gives the relationship

$$
\begin{align*}
& z=\frac{K-1}{2 K-1} \cdot \frac{B+2 a}{A_{0}}+\frac{1}{2 K-1} z^{K} \\
& \quad\left(z=\frac{1}{2-\ln z} \cdot \frac{B+2 a}{A_{0}} \text { for } K=1\right) \tag{12}
\end{align*}
$$

which allows estimation of the magnitude of $z$ for a given experimental condition by successive approximation. For a sufficiently small value of $A_{0} z^{K}$ in comparison to $B+2 a$, Eq. (11) can be written approximately (exact when $K=\infty$ ) by

$$
\begin{equation*}
-\frac{d B}{d t} \fallingdotseq k_{1} B(B+2 a)=k_{1}\left[2 A_{0}-\left(B_{0}-B\right)\right] B \tag{13}
\end{equation*}
$$

whereas for the cases where $K=1 / 2$

$$
-\frac{d B}{d t}=1 / 2 k_{1} B(B+2 a)
$$

and

$$
z^{1 / 2}=\frac{B+2 a}{2 A_{0}}
$$

hold exactly. The error in the approximation Eq. (13) is determined by the relative magnitude of $A_{0} z^{K}$ in comparison to $B+2 a$, which is, in turn, related to $z$ by Eq. (12). If the ratio $B_{0} / A_{0}$ is not too small, Eq. (13) should lead to a sufficiently accurate result as long as $K$ is fairly large. The solutions of the above-given rate equations are

$$
\begin{equation*}
\ln \frac{B}{B+2 a}-\ln \frac{B_{0}}{B_{0}+2 a} \doteqdot-2 a k_{1} t(K \neq 1, K \neq 1 / 2) \tag{14}
\end{equation*}
$$

and

$$
\ln \frac{B}{B+2 a}-\ln \frac{B_{0}}{B_{0}+2 a}=-a k_{1} t(K=1 / 2)
$$

respectively. In particular, for equivalent mixtures ( $2 A_{0}=$ $B_{0}$ ), the solutions are in the forms

$$
\begin{equation*}
\frac{1}{\mathcal{B}}-\frac{1}{B_{0}} \doteqdot k_{1} t(K \neq 1, K \neq 1 / 2) \tag{15}
\end{equation*}
$$

and

$$
\frac{1}{B}-\frac{1}{B_{0}}=1 / 2 k_{1} t(K=1 / 2)
$$

respectively. Eq. (15') has been reported in the literature. ${ }^{1}$ Eq. (14) can be used for estimation of the value of $k_{1}$ from kinetic experiments without too strenuous restriction
on the mixing ratio of the reactants. The $\ln [B /(B+2 a] v s$. $t$ plot will approach a straight line as the contribution of the term $A_{0} z^{K}$ diminishes. From the slope of the straight line portion, the value of $k_{1}$ can be obtained, and the result should be more accurate than that obtained by the previously reported mothod ${ }^{1}$ which relies on overlapping of the experimental Powell plot on the families of calculated ones.

As $K$ tends to zero ( $k_{2}=0$ ), Eq, (14) can not be used, since the rate equation will not contain $C\left(A_{0}-A=B_{0}-B\right)$. The solution for such cases is given by the well-known equation

$$
\begin{equation*}
\ln \frac{B_{0}\left[A_{0}-\left(B_{0}-B\right)\right]}{A_{0}\left[B_{0}-\left(B_{0}-B\right)\right]}=\left(A_{0}-B_{0}\right) k_{1} t \tag{16}
\end{equation*}
$$

which can be rewritten in a simitar form as Eq. (14):

$$
\ln \frac{2 B}{2 a-B_{0}+2 B}-\ln \frac{B_{0}}{2 a+B_{0}}=\left(a-B_{0} / 2\right) k_{1} t
$$

or

$$
\begin{aligned}
\ln \frac{B}{B+A_{0}-B_{0}}-\ln \frac{B_{0}}{B_{0}+2 a} & =\ln \frac{B}{B+A_{0}-B_{0}}-\ln \frac{B_{0}}{2 A_{0}} \\
& =\left(A_{0}-B_{0}\right) k_{1} t,
\end{aligned}
$$

which indicates that the treatment of the system as a simple second-order reaction would give approximately twice the value of $k_{1} ; \mathrm{it}$ is obvious since consumption of $B$ will be a half for $k_{2}=0$.

On the other hand, for the other extreme case where $k_{1} \ll k_{2}$ (or $k_{2}=\infty$ ) hence $2\left(A_{0}-A\right)=B_{0}-B$ and $C \rightarrow 0$ (but $K C$ is finite) hold, the rate equation is given by

$$
\ln \frac{B}{B+2 a}-\ln \frac{2 B_{0}}{B_{0}+2 a}=-2 a k_{1} t
$$

which differs from Eq. (14) only by an additional term $\ln 2$ in the left-hand side. Thus, Eq. (14) is essentially the rate equation for

$$
A+2 B \xrightarrow{2 k_{1}} D+F
$$

which would represent the system at stationary state $\frac{d C}{d t}=0$ or $C=0$. Benson's Figure 1 and Table $I^{3}$ indicate that the steady state condition cannot be reached when a large excess of A is used in the reactions with large value of $K$; however, in such cases, the magnitude of $C$ becomes negligibly small after a certain length of initial period in view of Eq. (10).

Furthermore, it should be noted that, when $A$ is used in large excess, $B+2 a \doteqdot 2 A_{0}$ in Eq. (13) and $A_{0}-B_{0}+B \fallingdotseq A_{0}$ in Eq. (16); thus, the time dependence of $B$ is dominated by the term $\ln B$ (psedo-first order in $B$ ) so that both Eq. (14) and ( $16^{\prime}$ ) will give straight lines with the slopes in about $1: 2$ ratio. Therefore, apparent fit of Eq. (16) in the experiment where a large excess of A is used should not be taken as evidence of $K \ll 1$. An example is illustrated in Figure 1.

When the term $A_{0} z^{K}$ is not negligible as in the case where $K<1$ or $A_{0} \gg B_{y}$, the rate equation

$$
\begin{align*}
-\frac{d B}{d t} & =k_{1} K\left[(B+2 a)-\frac{2 K-1}{K} A\right] B \\
& =k_{1} K\left[2\left(A_{0}-A\right)-\left(B_{0}-B\right)+\frac{A}{K}\right] B
\end{align*}
$$



Figure 1. Plots of the kinetic data for $\mathrm{N}_{2} \mathrm{H}_{4}-\mathrm{Br}_{2}$ reaction at $20^{\circ} \mathrm{C}:\left[\mathrm{N}_{2} \mathrm{H}_{4}\right]_{0}=20.1 \times 10^{-5} \mathrm{M} .\left[\mathrm{Br}_{2}\right]_{0}=3.37 \times 10^{-5} \mathrm{M}$.

TABLE 1: The Value of $z$ for which the Concentration of $C$ is Maximum

| $K$ | $z_{\max }=\frac{K C_{\max }}{A_{0}}$ | $z_{\max }^{x}=\frac{C_{\max }}{A_{0}}$ | K | $z_{\max }=\frac{K C_{\max }}{A_{0}}$ | $z_{\operatorname{arx}}^{x}=\frac{C_{\operatorname{axax}}}{A_{0}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.01 | 0.0095 | 0.955 | 2 | 0.50 | 0.25 |
| 0.1 | 0.0774 | 0.774 | 5 | 0.699 | 0.134 |
| 0.5 | 0.25 | 0.50 | 10 | 0.774 | 0.077 |
| 1.0 | 1/e | 0.367 | 20 | 0.854 | 0.043 |
|  |  |  | 40 | 0.923 | 0.018 |
|  |  |  | 100 | 0.955 | 0.010 |
|  |  |  | 200 | 0.974 | 0.005 |
|  |  |  | 500 | 0.988 | 0.002 |

better information. Since the large excess of the reactant A presumes

$$
C=2\left(A_{0}-A\right)-\left(B_{0}-B\right) \ll A_{0} \fallingdotseq A
$$

Eq. (11') leads to a pseudo-firstorder rate equation

$$
-\frac{d B}{d t} \fallingdotseq k_{1} A_{0} B
$$

provided $\mathrm{C}=2\left(A_{0}-A\right)-\left(B_{0}-B\right) \ll \frac{A}{K}$ holds. Thus, if the kinetics deviates from first order in $B$ and simple secondorder kinetics treatment gives gradually varying rate constant in an experiment with a large excess of $A$, one can presume that $A / K$ is not much larger than $C$. In Figure 1 of McMillan's work ${ }^{2}, z$ is plotted against $C / A_{0}$ for various values of $K$ from which the condition for negligible contribution of $C$ can be found. As a matter of fact, from Eq. (6), it can be shown that the maximum value of $C$ satisfies

$$
\frac{K C_{\max }}{A_{0}}=\left(\frac{1}{K}\right)^{\frac{1}{R-1}}=z_{\max }
$$

so that $K C$ can be neglected throughout the course of reaction
in comparison to $A$ only for $K<0.1$ if $A_{0} \gg \boldsymbol{B}_{0}$, as shown in Table 1. Thus, if the term $K C$ can be neglected, the rate equation is represented by

$$
-\frac{d B}{d t} \doteqdot k_{1} A B
$$

which corresponds to $k_{2}=0$, whence Eq. (16) should give a constant rate constant. Otherwise, it is better to carry out experiment under the condition of $2 A_{0} \simeq B_{0}$ so that the magnitude of $z$ decreases rapidly and hence Eq. (14) or (15) can be used, which are valid when $A_{0} z^{K} \ll B+2 a$ and $a>0$ hold.

Finally, rearrangement of Eq . (14) gives

$$
\begin{equation*}
B=\frac{B_{0}}{1+\frac{B_{0}}{2 a}\left(1-e^{2 a k_{1} t}\right)} \cdot e^{-2 k k_{1} t} \tag{17}
\end{equation*}
$$

which predicts the exponential decrease of $B$ for the final stage where $a k_{1} t \ll 1$.

For the cases where $K$ is not sufficiently large to make the term $A_{0} z^{K}$ negligible, Frost and Schwemer's method ${ }^{2}$ may be the only resort.

## Kinetic Eaqations for $\boldsymbol{A}$

From the material balance equation (5), $B$ can be expressed in terms of $z$ as

$$
\begin{equation*}
B=A_{0}\left[2 z+\frac{1}{K-1^{z}}\left(1-z^{K-1}\right)\right]-2 a \tag{5'}
\end{equation*}
$$

which gives the rate equation for $A$

$$
\begin{align*}
-\frac{d A}{d t} & =k_{1} A B=k_{1} A_{0}{ }^{2} z\left[\frac{2 K-1}{K-1} z-\frac{1}{\mathrm{~K}-1} \imath^{K}-\frac{2 a}{A_{0}}\right] \\
& =-A_{0} \frac{d z}{d t} \tag{18}
\end{align*}
$$

or

$$
\begin{gather*}
\ln \frac{A}{A-\frac{K-1}{2 K-1} \cdot 2 a}-\ln \left[1-\frac{K-1}{2 K-1} \cdot 2 a\right] \\
\fallingdotseq-k_{1} A_{0} \frac{2 K-1}{K-1} t \tag{19}
\end{gather*}
$$

if $z^{K} \ll(2 K-1) z$ and $a \neq 0$ hold.
In particular, if $2 K-1 \doteqdot 2(K-1)$, Eq. (19) can be approximated by

$$
\begin{equation*}
\ln \frac{A}{A-a}-\ln \frac{B_{0}}{2 A_{0}} \fallingdotseq-2 k_{1} A_{0} t \tag{19'}
\end{equation*}
$$

Furthermore, if $a=0$ and $z^{K} \ll(2 K-1) z$, Eq. (18) is integrated to

$$
\frac{1}{A}-\frac{1}{A_{0}} \doteqdot k_{1} \cdot \frac{2 K-1}{K-1} t
$$

or

$$
\frac{A_{0}}{A} \doteq 1+k_{1} A_{0} \frac{2 K-1}{K-1} t
$$

The rate equation (19) is valid as long as $K$ is large and $z^{K} \ll(2 K-1) z$ holds. If $k_{1}$ is determined from Eq.(14), Eqs. (19') and (19) provide an estimation procedure for $K$.

## Estimation of the Value of $K$

Svirbely ${ }^{4}$ has suggested that the value of $K$ can be obtained from a measured pair ( $C, A$ ) of experimental concentrations with the aid of Eq. (6). For fast reactions, the concentration pair after completion of reaction are easier to determine. Since, at the end of the reaction $B=0, \mathrm{Eq}$. (12) can be written for $K \neq 1$ as

$$
z=\frac{K-1}{2 K-1} \cdot \frac{2 a}{A_{0}}+\frac{1}{2 K-1} z^{K}
$$

if $A$ is used in excess. If $x^{K}$ can be neglected in comparison to (K-1) $\frac{2 a}{A_{0}}$, one can approximate Eq. (6) and (7) by

$$
\begin{align*}
\frac{C}{A_{0}} & =\frac{1}{2 K-1} \cdot \frac{1}{A_{0}}\left[2 a-2 A_{0} z^{K}\right] \\
& \fallingdotseq \frac{1}{K-1} \frac{A}{A_{0}}\left(=\frac{2 a}{(2 K-1) A_{0}} \text { for } B=0\right)
\end{align*}
$$

and

$$
\begin{align*}
\frac{D}{A_{0}} & =\frac{1}{2 K-1} \cdot \frac{1}{A_{0}}\left[K B_{0}-A_{0}+\frac{2 K-1}{K-1} z^{K}\right] \\
& \fallingdotseq 1-\frac{K}{2 K-1} \cdot \frac{2 a}{A_{0}}(\text { for } B=0)
\end{align*}
$$

Eq. ( $6^{\prime \prime}$ ) indicates that neglect of the $z^{K}$ term implies the approximation

$$
C \fallingdotseq \frac{1}{K-1} A \fallingdotseq \frac{1}{2 K-1} \cdot(B+2 a)
$$

Thus, after the reaction is complete, the concentrations of the products satisfy the following relationships:

$$
\begin{equation*}
\frac{C}{B_{0}} \div \frac{1}{2 K-1} \cdot \frac{2 a}{B_{0}} \tag{20}
\end{equation*}
$$

and

$$
\begin{align*}
& \frac{D}{B_{0}} \doteqdot \frac{1}{2 K-1}\left(K-\frac{A_{0}}{B_{0}}\right)  \tag{21}\\
& \frac{D}{C}=\frac{(K-1)-K z-z^{K}}{z-z^{K}} \fallingdotseq(2 K-1) \frac{A_{0}}{2 a} \\
& -K=\frac{K B_{0}-A_{0}}{2 a}=\frac{\frac{B_{0}}{A_{0}} K-1}{2-\frac{B_{0}}{A_{0}}} \tag{22}
\end{align*}
$$

provided $z^{K-1}<1$ can be assumed, from which the value of $K$ can be estimated. The proper choice of the value $-\frac{2 a}{A_{0}}$ should enable to satisfy the necessary condition for the above-given approximation (see Table 2). If $A$ can be determined accurately at the end of reaction, trial and error method to fit the Eq. ( $12^{\prime}$ ) will give an estimate of the value of $K$, but the procedure may be rather cumbersome.

TABLE 2: Product ratio D/C for Various Slituations

| $B_{0} / A_{0}$ |  |  |  |  |  |  |  |  | 5 | 10 | 20 | 50 | 100 | 200 | 1000 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.5 | 13.0 | 28.0 | 58.0 | 148 | 312 | - | - |  |  |  |  |  |  |  |  |
| 0.5 | 4.33 | 2.67 | 6.0 | 16.0 | 32.7 | 49.3 | 66.0 |  |  |  |  |  |  |  |  |
| 0.2 | - | $0.55_{5}$ | 1.66 | 5.00 | 10.6 | 16.1 | 21.7 |  |  |  |  |  |  |  |  |
| 0.1 | - | - | $0.52_{5}$ | 2.10 | 4.71 | 7.37 | 10.0 |  |  |  |  |  |  |  |  |
| 0.01 | - | - | - | - | - | 0.503 | 45 |  |  |  |  |  |  |  |  |

## Application of the Theory to Experimental Results

The kinetic data ${ }^{5}$ for hydrazine-bromine reaction in 7.2 M $\mathrm{H}_{2} \mathrm{SO}_{4}$ are plotted in Figure 1. Simple second-order treatment by Eq. (16) gives gradually decreasing value of $k_{1}$ starting from $97 \mathrm{M}^{-1} \mathrm{sec}^{-1}$ at 7.5 sec to 88 at 82.5 sec . However both Eqs. (14) and (16') give fairly good straight lines that are dominated by $\ln B$. The straight line portion of the competitive cousecutive second-order plot of Eq. (14) gives $42 M^{-1} \mathrm{sec}^{-1}$, whereas the plot of Eq. (16') gives $86 M^{-1} \mathrm{sec}^{-1}$. The fact that the deviation of initial stage is rather small and diminishes rather rapidly can be attributed to a large value of $K$ so that the magnitude of the term $A_{0} z^{K}$ becomes negligible at an early stage of the reaction. Since the point corresponding to $z=0.98$ lies on the straight line, the vlaue of K is inferred to be greater than $10 .^{2}$ Unfortunately, a small
portion of $B$ (mainly $\mathrm{N}_{2} \mathrm{H}_{2}$ in the present example) is consumed by some side reaction so that estimation of the value of $K$ from stoichiometry may not give results of desirable accuracy, in the present example.

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# Temperature Dependence of Self-Diffusion of THO in Copolymer Hydrogel Membrane as a Function of Gel Compositions 

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#### Abstract

The self-diffusion experiment of THO was performed across a series of copolymer hydrogel membranes at different temperatures. Copolymer hydrogel membranes were prepared by copolymerizing 2 -hydroxyethyl methacrylate (HEMA)and 2-aminoethyl methacrylate (AEMA) in the presence of the solvent and the crosslinker, ethylene glycol dimethacrylate (EGDMA). By changing the crosslinker content and the ratio of HEMA and AEMA monomer, two series of copolymer hydrogel membranes were synthesized. The tagging material was THO and efflux of THO was counted on a Liquid Scintillation Counter. The experimental data show that the permeability decreases as the amount of EGDMA and the mole fraction of HEMA increase, and the permeability is proportional to the temperature. The partition coefficient shows a parallel trend with permeability. Using the relationship between viscosity and diffusivity, the viscosity of water within the membrane was obtained. According to the result, the viscosity of water within the membrane has the same value with those of supercooling water. And we obtained the activation energy of THO for transport in the membrane by using Arrhenius plotting.


## Introduction

The properties of poly(2-hydroxyethyl methacrylate) (HEMA) hydrogel membrane were investigated by many authors. It is the reason that poly(HEMA) have attracted considerable attentions for medical applications because of their low chemical reactivity, high strength, and high permeability, and have been introduced as important biocompatible materials. ${ }^{1-6}$ The experiments for the transport phenomena have been performed by many authors and given many informations about it. Spacek et al. ${ }^{7}$ showed that the diffusion coefficient strongly depends on the structure of the hydrogel membrane investigated. Chen ${ }^{8}$ found that water swelling was changed by the crosslinker content in the dehydrated poly (HEMA) hydrogels. Recently, Kim ef al. ${ }^{9}$ measured the permeability of THO through fully swollen poly (HEMA) hydrogel membrane with varying the cros-
slinker content. They found that diffusion coefficients decrease as the crosslinker contents increase. Refojo et al. ${ }^{3}$ measured the swelling contents in hydrogels at the temperature is varied. They found that the minimum in the amount of water in hydrogel is found in the neighborhood of $60^{\circ} \mathrm{C}$ and the amount of water in the hydrogel increases up to the freezing and boiling temperature, and the minimum found in the curve in the HEMA hydrogel is independent of the temperature at which the polymerization was carried out. Wisniewski ${ }^{10}$ measured the temperature effects of permeation of THO across poly (HEMA) membrane. According to the temperature dependence of diffusion coefficient, they performed the Arrhenius plots and found the activation energy of THO for transport through poly (HEMA) membrane.
In this paper, we measured the permeability and partition coefficient of THO in the copolymer hydrogel membranes with varying the ratio of HEMA and AEMA monomer and

