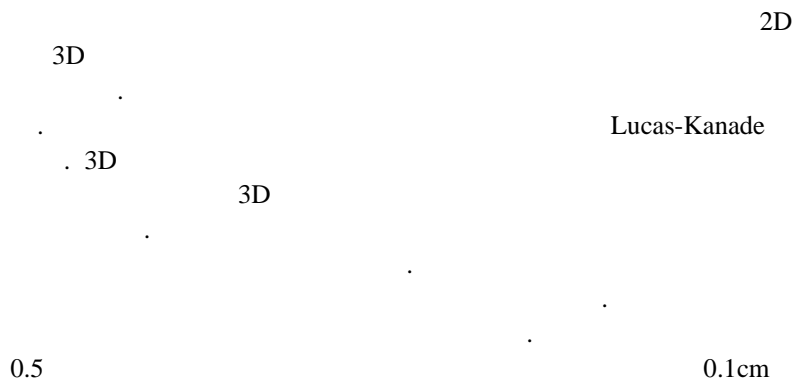


<sup>1, 2, 3, 4</sup>  
<sup>1 2 3, 4</sup>  
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## Fast Structure Recovery and Integration using Scaled Orthographic Factorization

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**Keywords** : Orthographic Factorization, 3D Structure Integration, Registration, Camera Pose Estimation

1.

가

2

3

3

가

가

3

[1].

3D

가 가

3D

가

가

가

3D

가

2

3

2.

2

3

(calibrated)

---

<sup>1</sup> (MOCIE)  
(IIT)

(uncalibrated) 가 [2].

Euclidean

$$x'_{fp} = x_{fp} - \frac{1}{N} \sum_{p=1}^N x_{fp}, \quad y'_{fp} = y_{fp} - \frac{1}{N} \sum_{p=1}^N y_{fp} \quad (2)$$

가 .

**W'** Singular Value Decomposition(SVD)

$$\mathbf{W}' = \mathbf{U} \mathbf{D} \mathbf{V}' \quad [7]. \quad \mathbf{U}$$

가 .  
가

**U'** , **D**

3×3 **D'** ,

**V**

**V'** .

**U** , **D** , **V**

**W'**

**U** , **D** ,

(orthographic factorization),

(scaled orthographic factorization),

(paraperspective factorization) [3][4].

**V**

(singular value)

가 ,  
가  
가

**R'** **S'** 가 3

$$\mathbf{R}' = \mathbf{U}' [\mathbf{D}']^{1/2}, \quad \mathbf{S}' = [\mathbf{D}']^{1/2} \mathbf{V}' \quad (3)$$

$$\mathbf{R}' = \mathbf{U}' [\mathbf{D}']^{1/2}, \quad \mathbf{S}' = [\mathbf{D}']^{1/2} \mathbf{V}' \quad (3)$$

**W'**=**R'S'**

**R'** 2F×3

**R**

**S'**

가 [5][6].

3×P

**S**

**R'** **S'**

(4)

**R** **S**

### 3.

[1].

$$\mathbf{W}' = \mathbf{R}' \mathbf{S}' = (\mathbf{R}' \mathbf{Q}) (\mathbf{Q}^{-1} \mathbf{S}') \quad (4)$$

$$\mathbf{R} = \mathbf{R}' \mathbf{Q}, \quad \mathbf{S} = \mathbf{Q}^{-1} \mathbf{S}'$$

### 3.2

가

가

$$c_x = \frac{1}{N} \sum_{p=1}^N x_{fp}, \quad c_y = \frac{1}{N} \sum_{p=1}^N y_{fp} \quad (5)$$

(5)

x, y

### 3.1

F

N

가

p

f

**R**

**R** (6)

$$\mathbf{R} = [\mathbf{i}_1 \cdots \mathbf{i}_N \mathbf{j}_1 \cdots \mathbf{j}_N] \quad (6)$$

(1)

**i**<sub>1</sub> **j**<sub>1</sub>, **i**<sub>N</sub> **j**<sub>N</sub>

$$\{(x_{fp}, y_{fp}) \mid f = 1, \dots, F, p = 1, \dots, N\} \quad (1)$$

2F×N **W**

$$\mathbf{W} = [\mathbf{X}^T \mid \mathbf{Y}^T]^T$$

가 (normalize)

z-

**X**

x

x-

y-

F×N

**Y**

y

F×N

$$\mathbf{W}' = [\mathbf{X}' \mid \mathbf{Y}']$$

**X'**

**Y'**

(orientation)가

$$\mathbf{X}' = [x'_{fp}], \quad \mathbf{Y}' = [y'_{fp}]$$

x'\_{fp}

y'\_{fp}

(2)

z, x, y

$$Mq=0$$

M

3

SVD

q

(8)

$$Mq = 0$$

4. 3

$$M = \left[ \begin{array}{ccc|c} \mathbf{p}_j^T & \mathbf{0}_3^T & \mathbf{0}_3^T & \\ \mathbf{0}_3^T & \mathbf{p}_j^T & \mathbf{0}_3^T & \\ \mathbf{0}_3^T & \mathbf{0}_3^T & \mathbf{p}_j^T & \end{array} \middle| \mathbf{I}_{3 \times 3} \middle| -\mathbf{p}_i \right] \quad (9)$$

[8].

(9)  $\mathbf{p}_i, \mathbf{p}_j, \mathbf{q}$

$$\mathbf{p}_i = [x_i \ y_i \ z_i]^T, \mathbf{p}_j = [x_j \ y_j \ z_j]^T$$

$$\mathbf{q} = [r_{11}, \dots, r_{33}, t_1, t_2, t_3, 1]^T$$

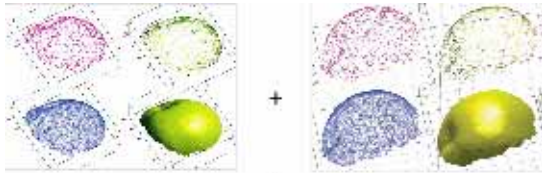
$\mathbf{D}_i$   $\mathbf{D}_j$ 가 가  $\mathbf{D}_i$   
 $\mathbf{D}_j$   
 1 3

13x1  $\mathbf{q}$  12

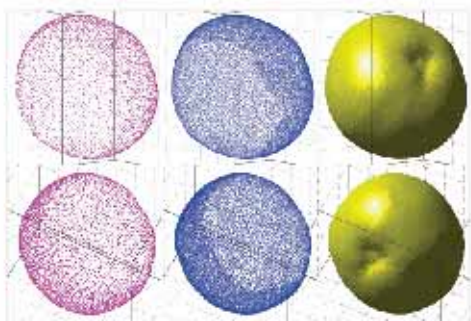
$\mathbf{q}$

5

5



$$Aq = 0, A = \begin{bmatrix} M_1 \\ \vdots \\ M_5 \end{bmatrix} \quad (10)$$



(10)  $M_i$  (9) 15x13  
 $A$  3  $Q$

T

(7)

5.

5.1

3

1.

T

$$\mathbf{X}_i = \mathbf{T}_{ij} \mathbf{X}_j \quad (7)$$

32

가

$$\mathbf{X}_i = \begin{bmatrix} x_i \\ y_i \\ z_i \\ 1 \end{bmatrix}, \mathbf{X}_j = \begin{bmatrix} x_j \\ y_j \\ z_j \\ 1 \end{bmatrix}, \mathbf{T}_{ij} = \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

(7)



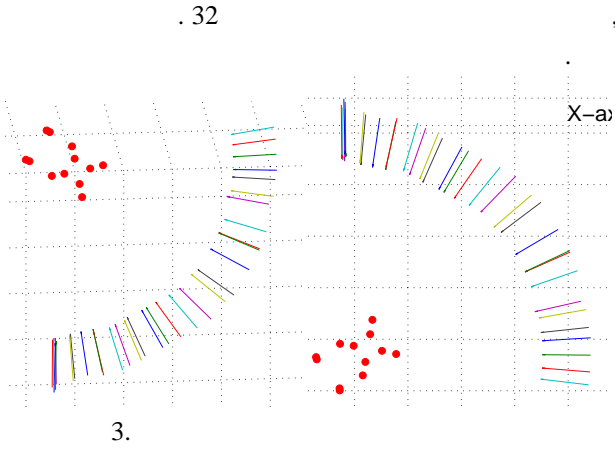
2.

$$\begin{bmatrix} r_{11}x_j + r_{12}y_j + r_{13}z_j + t_1 - x_i \\ r_{21}x_j + r_{22}y_j + r_{23}z_j + t_2 - y_i \\ r_{31}x_j + r_{32}y_j + r_{33}z_j + t_3 - z_i \\ 0 \end{bmatrix} = \mathbf{0}_4 \quad (8)$$

3

. 12

3



3 3 1 4 12

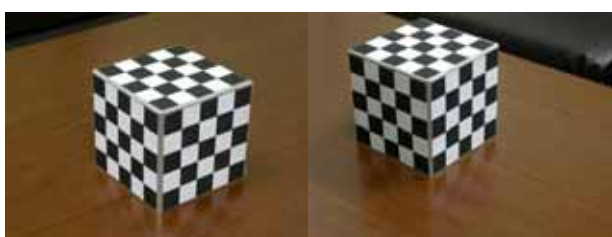
cm  
가  
1 d1 d4  
0.3cm 가  
1 3 3

( :cm)

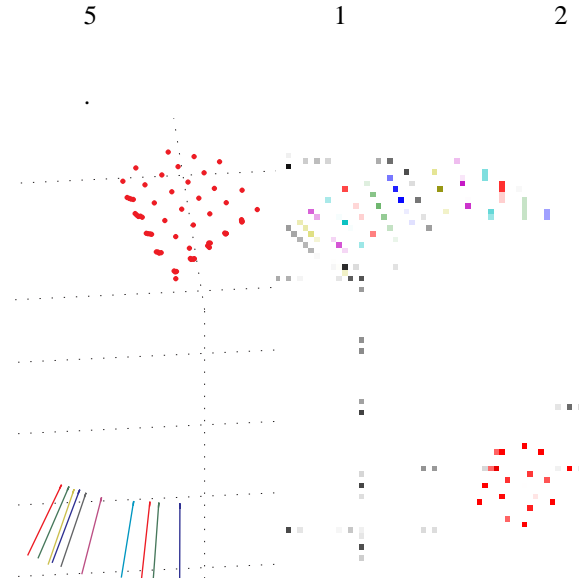
	d1	d2	d3	d4
inner square	0.2225	0.1199	-0.3137	-0.0287
outer square	0.0212	0.0270	-0.0735	0.0253
points	-0.1167	0.0846	-0.0274	0.0596

5.2

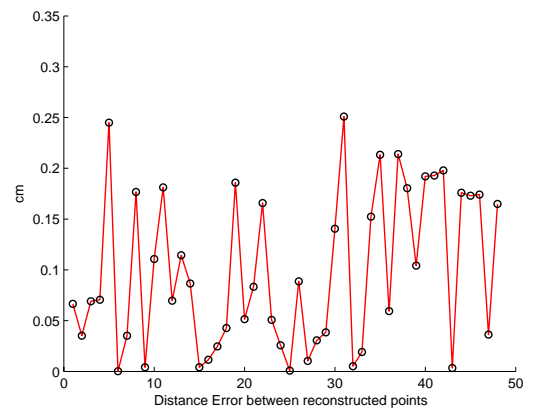
3 3  
2 7 3 10 14  
61 61 43 4



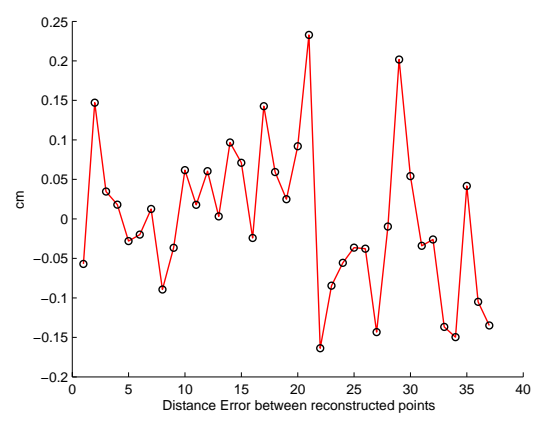
4.



5.



6. 1 3



7. 2 3

6 1

48

0.25cm  
0.0986cm

가  
7 6  
2  
37  
0.0742cm  
가  
6

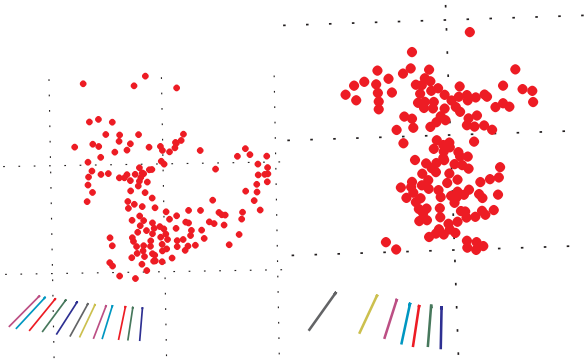
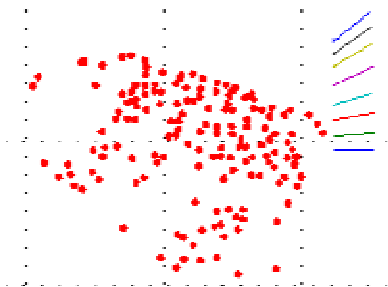
5.3 (sheep)

가 3  
8



8. ( 3)

9



9. ( ), (

), ( )

7 , 8 , 12  
143 ,  
155 , 146

5.4

2. ( : )

	0.5000	0.5000	0.5150	0.5150
	0.7820	0.8280	0.7500	0.9380

0.5

가

6.

6.1

3 가 4  
3 가

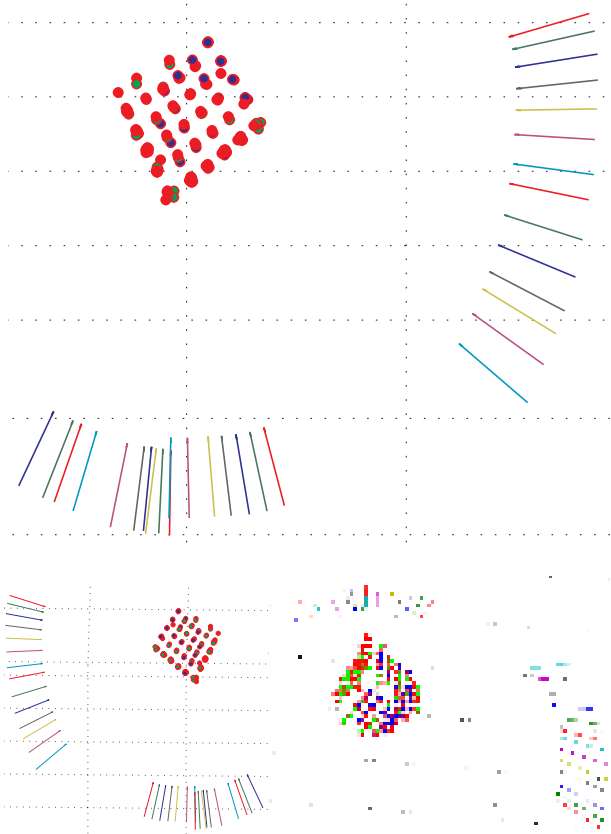
10

가

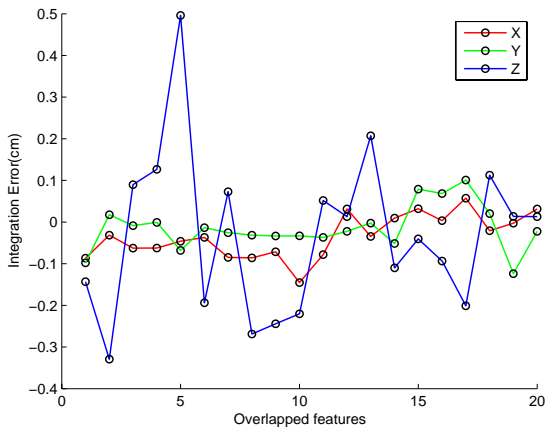
11

10

가 0.1cm x- y- z  
0.5cm 가 가

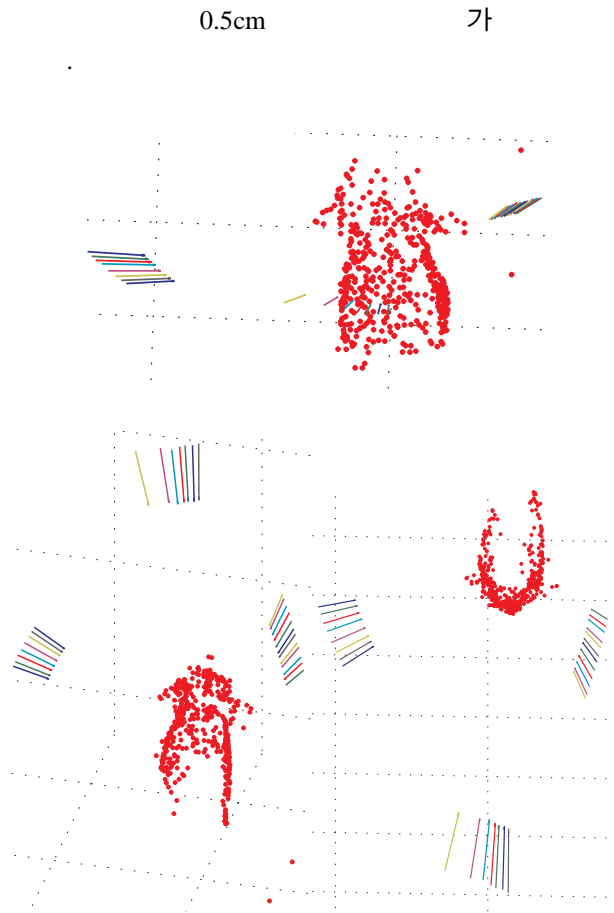


10.

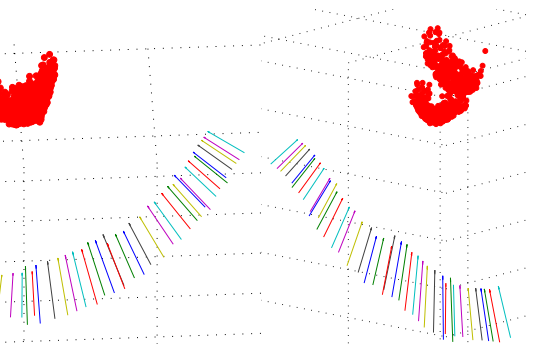
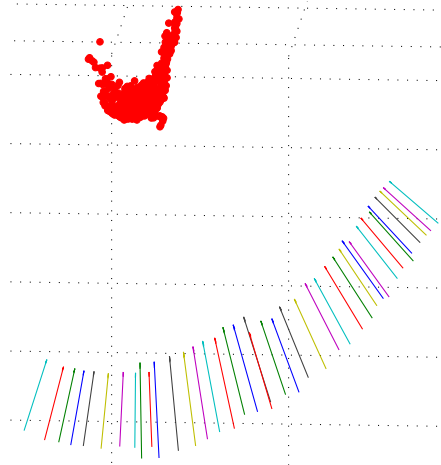


11.

6.2



12.



13.

12

3

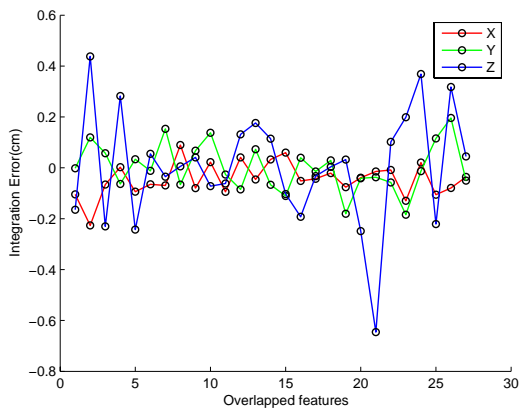
13

3

14

13

가 가



14.

7.

3

2D

3

5

가

가

가

가

가

## Reference

- [1] Christoph Bregler, Aaron Hertzmann, Henning Biermann, "Recovering Non-Rigid 3D Shape from Image Streams," Proc. of IEEE Conference on Computer Vision and Pattern Recognition, Hilton Head, South Carolina, pp. 190-696, June 2000.
- [2] Mei Han, Takeo Kanade. "Creating 3D Models with Uncalibrated Cameras," WACV, p. 178, Fifth IEEE Workshop on Applications of Computer Vision, 2000.
- [3] Carlo Tomasi, Takeo Kanade, "Shape and Motion from Image Streams: a Factorization Method," Technical Report CMU-CS-91-172, Carnegie Mellon University, Pittsburgh, PA, September 1991.
- [4] Conrad J. Poelman and Takeo Kanade, "A Paraperspective Factorization Method for Shape and Motion Recovery," Technical Report CMU-CS-93-219, Pittsburgh PA, December 1993.
- [5] L. Matthies, T. Kanade, R. Szeliski, "Kalman filter-based algorithms for estimating depth from image sequences," International Journal of Computer Vision, Vol. 3(3), pp. 209-236, September 1989.
- [6] C. Tomasi, T. Kanade, "Shape and Motion without depth," In Proceedings of the DARAPA Image Understanding Workshop, pp. 258-270, Pittsburgh, September 1990.
- [7] G.H. Golub, C. Reinisch, "Singular Value Decomposition and Least Squares Solutions," In Handbook for Automatic Computation, Vol. 2, pp. 134-151, 1971.
- [8] Andrew Johnson, Sing Bing Kang, "Registration and Integration of Textures 3-D Data," Proceedings of 3DIM'97, pp. 234-241, 1997.