

### Active High pass filter with Notch Characteristic using Uniformly Distirbuted RC Line

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**Abstract:** This paper describes the high pass filter with notch charecteristics. The proposed circuits configuration consists of two uniformly distributed RC line (herein after is called URC) and two gain amplifiers ( $K_1$  and  $K_2$ ). With the appropriate  $K_1$  and  $K_2$ , the circuit has a steeper slope of magnitude response at pass band steeper than using a single gain amplifier.

**Keywords:** High Pass Filter , URC

#### 1. INTRODUCTION

The uniformly distributed RC line with a single amplifier have been published in many case [1], [2], [3], [4]. Herein, the paper proposed an active high pass filters using two lumped URC and two amplifiers. The lumped URC ( $R_1C_1$ ) behavior as a high pass filter in conjunction with amplifier  $K_1$  and active notch filter circuits with amplifier  $K_2$  respectively.

#### 2. UNIFORMLY DISTRIBUTED RC LINE (URC)

A crossed sectional structure of the URC is illustrated in Fig. (a) The circuit symbol of Fig. 1(a) is illustrated in Fig. 1(b)

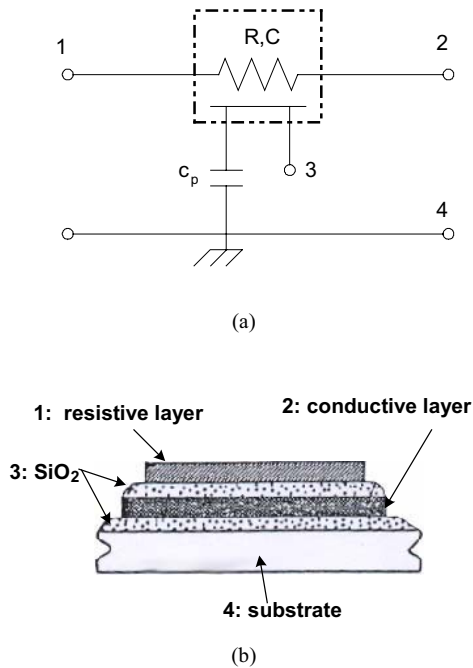


Fig. 1(a) A distributed RC line and (b) It’s symbol

The 3-ports floating admittance parameters matrix  $[Y_{ij}]$  of the URC in Fig. 1(a) is given as follows:

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = X \begin{bmatrix} Y & -1 & -(Y-1) \\ -1 & Y & -(Y-1) \\ -(Y-1) & -(Y-1) & 2(Y-1) \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} \quad (1)$$

Where  $X = \frac{P}{R \sinh P}$  and  $Y = \cosh P$ ,

$P = \sqrt{sRC}$ ,  $R$  and  $C$  are the values of total resistance and capacitance of the URC respectively.  $s$  is the complex angular frequency variable.

#### 3. HPF USING URC

##### 3.1 HPF WITH NOTCH CHARACTERISTICS

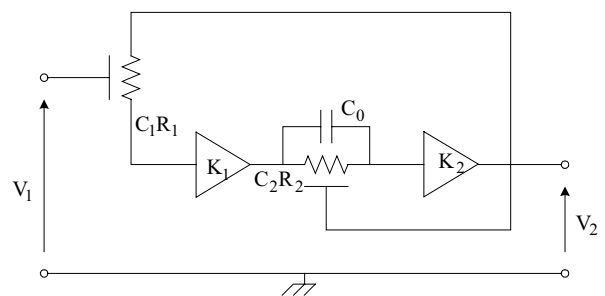


Fig. 2 Active distributed RC HPF.

The proposed active distributed RC HPF circuit is shown in Fig. 2. The voltage transfer function  $T(p) = V_2/V_1$  of the circuit is given as follow:

$$\frac{V_2}{V_1} = \frac{-(Y_1 - 1)(sC_0 + X_2)K_1K_2}{(sC_0 + X_2)K_1K_2 - Y_1\{-X_2(Y_1 - 1)K_2 + (sC_0 + X_2)Y_2\}} \quad (2)$$

Where

$$\left. \begin{aligned} Y_1 &= \cosh P_1, & Y_2 &= \cosh P_2, \\ X_1 &= \frac{P_1}{R_1 \sinh P_1}, & X_2 &= \frac{P_2}{R_2 \sinh P_2}, \\ P_1 &= \sqrt{sR_1 C_1}, & P_2 &= \sqrt{sR_2 C_2}, \\ \frac{P_2}{sC_0 R_2} &= \frac{1}{P_2} \cdot \beta, & \beta &= \frac{C_2}{C_0} \end{aligned} \right\} \quad (3)$$

$K_1, K_2$  are positive gain amplifier.

Eq. (2) is reduced to the following expression:

$$\frac{V_2}{V_1} = \frac{-(\cosh P_1 - 1)(P_2 \sinh P_2 + \beta)K_1 K_2}{(P_2 \sinh P_2 + \beta)K_1 K_2 + \cosh P_1 \{\chi - \beta K_2 - P_2 \sinh P_2\}} \quad (4)$$

Where  $\chi = \beta \cosh P_2 (K_2 - 1)$

### 3.2 Frequency response

Frequency response of Eq. (4) for the values of  $K_1, K_2$  are plotted in Fig. 3(a), 3(b). The frequency response are favorable for HPF.

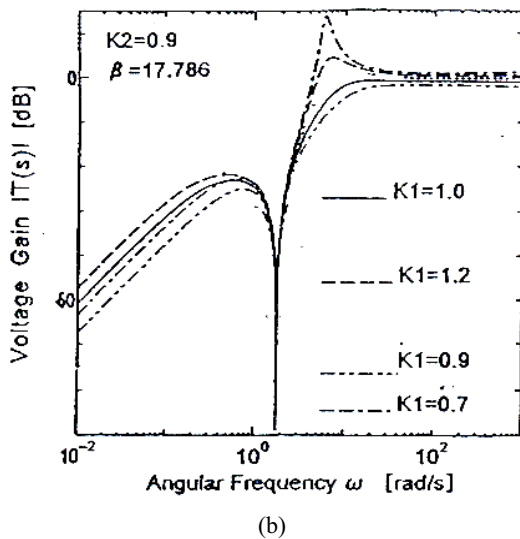
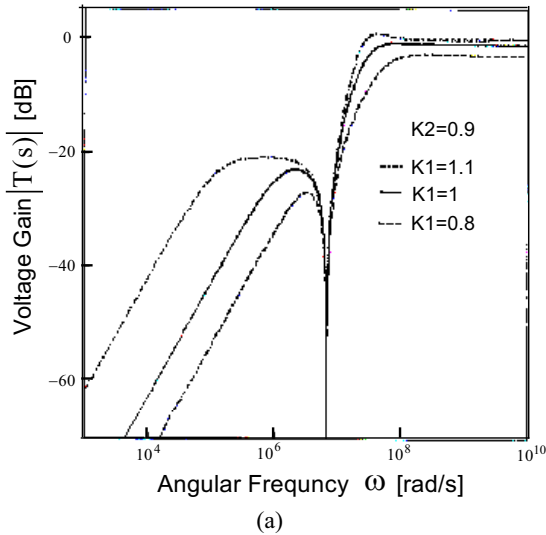


Fig. 3(a), (b) Magnitude frequency response.

From Fig. 3(a), 3(b) it is seen that for  $K_2 = 0.9, \beta = 17.786$  and  $K_1 = 1$  will give a high pass filter with steeper slope at the pass band without producing pass band peak.

### 3.3 Example

Herein, we consider a high pass transfer function. Let  $K_1 = 1, K_2 = 0.9$  for an experiment, we choose the values of the circuit parameters as follows:

$$\left. \begin{aligned} R_1 &= 10K\Omega, & R_2 &= 100K\Omega, \\ C_1 &= 10pF, & C_2 &= 100pF, \\ C_0 &= 5.622pF \end{aligned} \right\} \quad (5)$$

The experimental results for the frequency charecteristics is shown in Fig. 4. The results gives good agreement with theoretical values.

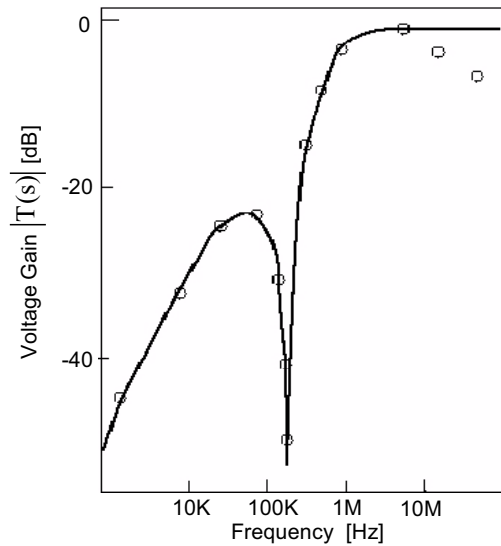


Fig. 4 Frequency response.

### 3.4 Sensitivity

The sensitivity  $S_{X_j}^T$  is defined as the ration of the normalized incremental change of the transfer function  $T(p)$ , due to the normalized change of the circuit parameter  $X_j$ .

$$S_{X_j}^T = \frac{d T(p)}{d X_j} \cdot \frac{X_j}{T(p)} \quad (6)$$

Magnitude sensitivity is defined as follow:

$$S_{X_j}^{|T|} = \text{Re } S_{X_j}^T \quad (7)$$

We can calculation the magnitude sensitivity for the change of  $K_1, K_2$ . The sensitivity  $S_{K_1}^T$  for the voltage gain  $K_1$  is shownas follow:

$$S_{K_1}^{|T|} = \frac{\cosh P_1 \{ \chi - \beta K_2 - \beta P_2 \sinh P_2 \}}{(P_2 \sinh P_2 + \beta) K_1 K_2 + \cosh P_1 \{ \chi - \beta K_2 - \beta P_2 \sinh P_2 \}} \quad (8)$$

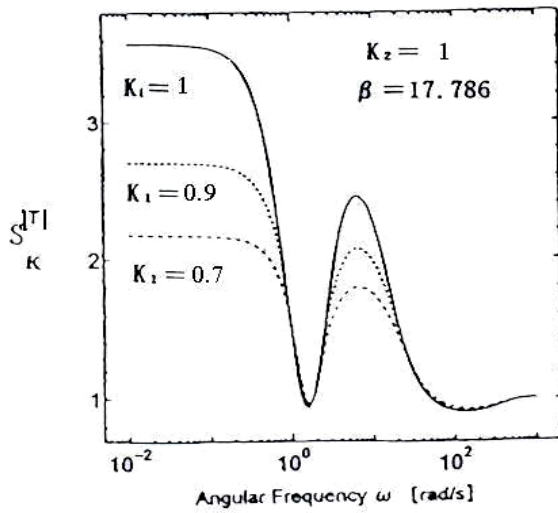
Where  $\chi = \beta \cosh P_2 (K_2 - 1)$

The sensitivity  $S_{K_2}^T$  for the voltage gain  $K_2$  is shown as follow:

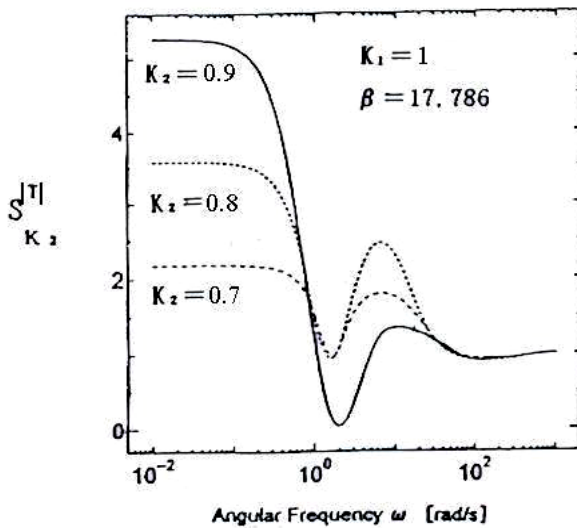
$$S_{K_2}^{|T|} = \frac{-\cosh P_1 \{ \beta \cosh P_2 + P_2 \sinh P_2 \}}{(P_2 \sinh P_2 + \beta) K_1 K_2 + \cosh P_1 \{ \chi - \beta K_2 - \beta P_2 \sinh P_2 \}} \quad (9)$$

Where  $\chi = \beta \cosh P_2 (K_2 - 1)$

Fig. 5(a), (b) shown magnitude sensitivity of  $T(j\omega)$  for amplifier  $K_1, K_2$ .



(a)



(b)

Fig. 5(a), (b) Magnitude sensitivities for The active element  $K_1, K_2$

From Fig. 5(a) and 5(b), it is seen that the sensitivities of positive gain  $K_1$  are sensible than does the positive gain  $K_2$  at the pass band.

#### 4. CONCLUSIONS

The novel active distributed RC HPF using URC elements are proposed and discussed. The experimental results of the frequency characteristics and the simulation by H-SPICE showed good agreements with theoretical.

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