

$\mu = 0$ Freund 가 Weier(1981), Hanagal Kale(1992), Hanagal(1996)

가 , 가 .
 가 (1) n 가
 가 가 가

- $n :$ ()
- $x :$ 1
- $y :$ 2
- $z_r :$ n 가 r , $r = 1, 2, \dots, n$
- $C_1, C_2 :$ 1 2
- $D_1, D_2 :$ z_r 1 2
- $D_{12} :$ 1 2 ,
- $D_{21} :$ 2가 1 ,
- $r_1 :$ $C_1 \cap D_2$
- $r_2 :$ $C_2 \cap D_1$
- $r_3 :$ $C_1 \cap C_2$
- $d_i, d_{ij} :$ D_i D_{ij} , $i, j = 1, 2$

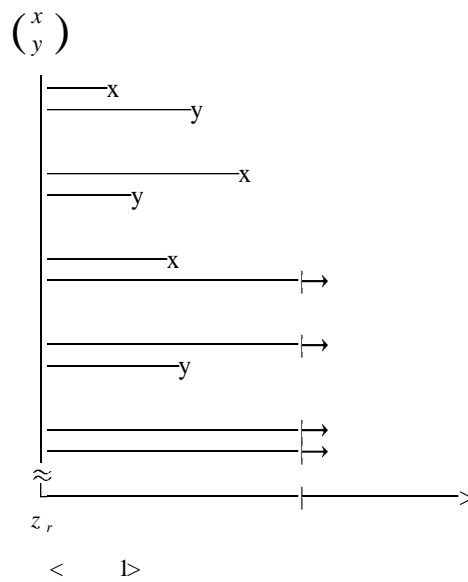
2.

2.1

$$\max(X, Y)$$

가

가 ,
 ,
 ,
 가 (1) n r
 ,
 가 $< 1 >$
 가 , 1 2 (D_{12})
 $(D_{21}),$ 1 2가 $(C_2 \cap D_1)$
 $(C_1 \cap D_2),$ $(C_1 \cap C_2)$. 가
 가 , 가
 가 가 .



2.2

n 가 ,
 i) 가 ,
 ii) 가 , iii)
 가 i) ii) .

2.2.1

z_r

가

(a) $\mu < x < y < z_r$:

1 2 μ x α β 가 , 1 x x
 y 2 β' .

$$\alpha \exp(-\alpha(x-\mu)) \exp(-\beta(x-\mu)) \beta' \exp(-\beta'(y-x))$$

$$= \alpha \beta' \exp\{-(\alpha+\beta-\beta')(x-\mu) - \beta'(y-\mu)\}$$

d_{12}

$$L_a = (\alpha\beta')^{d_{12}} \exp\left\{-(\alpha+\beta-\beta') \sum_{i \in D_{12}} (x_i - \mu) - \beta' \sum_{i \in D_{12}} (y_i - \mu)\right\} \quad (2)$$

(b) $\mu < y < x < z_r$:

(a) d_{21}

$$L_b = (\alpha'\beta)^{d_{21}} \exp\left\{-(\alpha+\beta-\alpha') \sum_{i \in D_{21}} (y_i - \mu) - \alpha' \sum_{i \in D_{21}} (x_i - \mu)\right\} \quad (3)$$

(c) $\mu < x < z_r < y$:

1 2가 r_2

$$L_c = \alpha^{r_2} \exp\left\{-(\alpha+\beta-\beta') \sum_{i \in C_1 \cap D_1} x_i - \beta' r_2 (z_r - \mu)\right\} \quad (4)$$

(d) $\mu < y < z_r < x$:

(c) r_1

(8)

2.2.2

가

가

 z_r

가

$$\mu < x < z_r < y \quad x = p_1 z_r \quad (0 \leq p_1 \leq 1) \quad (4)$$

$$L_{c'} = \alpha^{r_2} \exp \{ - (\alpha + \beta - \beta') r_2 p_1 (z_r - \mu) - \beta' r_2 (z_r - \mu) \} \quad (9)$$

$$\mu < y < z_r < x \quad y = p_2 z_r \quad (0 \leq p_2 \leq 1) \quad (5)$$

$$L_{d'} = \beta^{r_1} \exp \{ - (\alpha + \beta - \alpha') r_1 p_2 (z_r - \mu) - \alpha' r_1 (z_r - \mu) \} \quad (10)$$

(2), (3), (6) (9), (10)

$$\begin{aligned} \ln L &= (d_{12} + r_2) \ln \alpha + (d_{21} + r_1) \ln \beta + d_{21} \ln \alpha' + d_{12} \ln \beta' \\ &- (\alpha + \beta) \left(\sum_{i \in D_{12}} (x_i - \mu) + \sum_{i \in D_{21}} (y_i - \mu) + r_2 p_1 (z_r - \mu) + r_1 p_2 (z_r - \mu) + r_3 (z_r - \mu) \right) \\ &+ \alpha' \left(\sum_{i \in D_{21}} (y_i - \mu) - \sum_{i \in D_{21}} (x_i - \mu) + r_1 p_2 (z_r - \mu) - r_1 (z_r - \mu) \right) \\ &+ \beta' \left(\sum_{i \in D_{12}} (x_i - \mu) - \sum_{i \in D_{12}} (y_i - \mu) + r_2 p_1 (z_r - \mu) - r_2 (z_r - \mu) \right) \end{aligned} \quad (11)$$

(11)

$$\hat{\mu} = \min \min (x_i, y_i) \quad (12a)$$

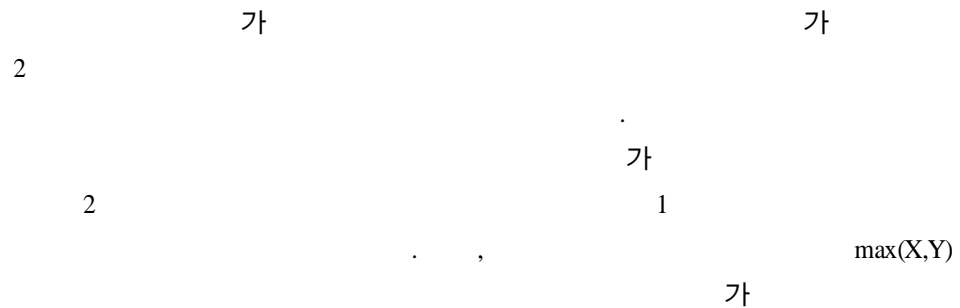
$$\hat{\alpha} = \frac{d_{12} + r_2}{\sum_{i \in D_{12} \cup D_3} (\min(x_i, y_i) - \hat{\mu}) + (r_2 p_1 + r_1 p_2 + r_3)(z_r - \hat{\mu})} \quad (12b)$$

$$\hat{\beta} = \frac{d_{21} + r_1}{\sum_{i \in D_{12} \cup D_3} (\min(x_i, y_i) - \hat{\mu}) + (r_2 p_1 + r_1 p_2 + r_3)(z_r - \hat{\mu})} \quad (12c)$$

$$\hat{\alpha}' = \frac{d_{21}}{\sum_{i \in D_{21}} (x_i - y_i) + (1 - p_2) r_1 (z_r - \hat{\mu})} \quad (12d)$$

$$\hat{\beta}' = \frac{d_{12}}{\sum_{i \in D_{12}} (y_i - x_i) + (1 - p_1) r_2 (z_r - \hat{\mu})} \quad (12e)$$

4.



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