Comparison of Magnetic Resonant Coupling Wireless Power Transfer Systems within Aligned and Unaligned Positions and Determining their Limits

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In this study, the efficiencies for both the angular aligned and unaligned positions of the receiver and transmitter coils of wireless power transfer (WPT) systems are examined. Some parameters of the equivalent circuit were calculated with Maxwell 3D software. The analytical solution of the circuit was calculated in MATLAB program through the composition of the system's mathematical modeling. The numerical solution of the system, however, was calculated using PSIM, which is circuit simulation software. In addition, with the use of the finite element method (FEM) in Maxwell 3D software, transient analysis of the three-dimensional system was performed. The efficiency of the system was estimated through the calculation of input and output power. The results demonstrated that power was efficiently transmitted to a certain extent in aligned and unaligned positions. The results also revealed that, for aligned positions, high efficiency with air gaps of 15-20 cm can be obtained and that the efficiency quickly dropped with air gaps of more than 20 cm. For spatially unaligned positions, it was observed that wireless power transfer could be realized with high efficiency with air gaps of up to 10 cm and that efficiency quickly dropped with air gaps of more than 10 cm.

Keywords : wireless power transfer, magnetic resonant coupling, alignment of coils, system efficiency

1. Introduction

Although wireless power transfer (WPT) has been a research topic for more than 200 years, it has not been actualized in the culture of electrical and electronic engineering, which can be seen as a critical problem. Since it was first proposed by Nicola Tesla in 1890, WPT has gradually increased in importance with the progress of technology as a multidisciplinary field and as a shared domain for different branches of science [1, 2]. Moreover, WPT plays a substantial role in the implementation of various applications such as electrical appliances, home electronics, and medical devices, all of which can provide solutions for possible problems in the future.

So far, wireless energy transfer has been practiced with electromagnetic radiation, microwaves, lasers, electromagnetic induction, and magnetic resonant coupling. The first studies on WPT were initiated by Nicola Tesla in an attempt to convey wireless electrical energy to the whole world with electromagnetic radiation. However, the studies

could not be finalized due to the sponsors' withdrawal from the project [1-3].

The idea of using microwaves in WPT emerged with the development of high-powered microwave transmitters after World War II. One of the pioneers in microwave power transfer, William Brown, designed a model helicopter, of which all the cruising power was provided by microwave beams [4].

Sahai and Graham actualized power transfer using lasers, which works at low efficiency in high distances as a type of wireless energy. However, the laser radiation, which is more suitable for space applications, is quite harmful, causing blindness even at low power, and killing living creatures through partial heating at high power [5].

Zhao and his colleagues have conducted research on electromagnetic induction theory, reaching high efficiencies, in which the active working distance from the primary coil to the secondary coil is only a few centimeters. However, the excessive proximity and the difficulty in aligning the secondary coil with the primary coil are the disadvantages of this method [6]. The theory of magnetic resonant coupling started with Massachusetts Institute of Technology (MIT) scientists' invention in 2007, called 'WiTricity', which revolutionized the technology

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of WPT. Using magnetic resonant coupling, a 60 Watt bulb could be lit from a distance of more than 2 meters and without using any wires, achieving roughly 40 % efficiency. In this way, mid-range WPT was actualized. In the WiTricity system, energy is transferred via magnetic resonant coupling. The power in the primary resonance coil is fully utilized by the secondary resonance coil in the optimal operation. Consequently, the power that is transferred can be efficiently shared among resonance objects, and weakly shared among non-resonance objects [7, 8].

Since previous researches that utilize inductive power transfer based on magnetic induction theory have low efficiency, their popularity has been dwindled and replaced in recent years by magnetic resonant coupling.

This study demonstrates the differences in the efficiencies of positional and angular aligned and unaligned conditions with respect to different air gaps and different angles. The study also demonstrates the limits of air gaps and angles in the aligned and unaligned positions, the change of mutual inductance and resonance frequency, and the differences in input and output current. The equivalent circuit simulation of the magnetic resonant coupling system was performed using PSIM software. In addition, the receiving and transmitting inductances were designed with Maxwell 3D software. The equivalent circuit of the magnetic resonance coupling system was set up in the Maxwell Circuit Editor (MCE) program. Using the receiver and transmitter coils in the Maxwell 3D software and the circuit in the MCE program, the transient analysis of the WPT system was performed in this study with the finite element method (FEM).

2. Calculation of Efficiency and Equivalent Impedance with Equivalent Circuit of Magnetic Resonant Coupling

In this section, the simple theory of the equivalent circuit will be explained. In order to analytically represent

Fig. 1. The equivalent circuit of the wireless power transfer system [9, 10].

the input impedance, power transfer, and efficiency, a simplified equivalent circuit of the WPT is used, as illustrated in Fig. 1.

In this equivalent circuit, I_1 represents the input current (transmitting current), I_2 represents the output current (receiving current), V_1 represents the input voltage, R represents the internal resistances of the receiving and transmitting system, C represents the receiving and transmitting resonance capacity, L_1 represents the transmitter coil, L_2 represents the receiver coil, L_m represents the mutual inductance, and Z_{load} (Z_0) represents the load impedance (characteristic impedance). To simplify the calculations of the resonant frequencies, R is ignored. The circuit shown in Fig. 1 is a model of a wireless power system created using a pair of magnetically coupled resonators. To calculate the resonant frequencies, it is advantageous to derive an alternative equivalent circuit.

Eq. (1) illustrates the circumference of the transmitting part, while Eq. (2) depicts the circumference equation of the receiving part.

$$V_1 = I_1 \left(R + jL_1\omega + \left(\frac{1}{j\omega C} \right) \right) - I_2(jL_m\omega) \quad (1)$$

$$0 = I_2 \left(jL_2\omega + \left(\frac{1}{j\omega C} \right) + Z_0 + R \right) - I_1(jL_m\omega) \quad (2)$$

From Eq. (2), the relationship between the currents of receiver and transmitter coils can be derived as shown in Eq. (3).

$$I_2 = I_1 \frac{jL_m\omega}{jL_2\omega + \left(\frac{1}{j\omega C} \right) + Z_0 + R} \quad (3)$$

The equivalent impedance can be obtained by placing Eq. (3) in Eq. (1) and dividing the generated voltage formula by the input current as to obtain Eq. (4).

$$Z_{eq} = Z_{in} = R + jL_1\omega + \left(\frac{1}{j\omega C} \right) + \frac{L_m^2\omega^2}{jL_2\omega + \left(\frac{1}{j\omega C} \right) + Z_0 + R} \quad (4)$$

The equivalent circuit in Fig. 1 can also be shown with

Fig. 2. T-type equivalent circuit of the WPT system.

Fig. 3. (Color online) Equivalent circuit of magnetic resonant coupling in PSIM Circuit Simulation Software.

Fig. 4. (Color online) Maxwell Circuit Editor Model.

3D. The inductances of coils and the mutual inductance between two coils are calculated by Maxwell 3D. After calculating inductance, the resonance frequencies are calculated by the MATLAB program and the circuit of the WPT system is simulated with PSIM and Maxwell 3D.

3.1. Comparing Spatially Aligned and Unaligned Positions

In the system, L is a nonlinear parameter and varies according to the current. Each parameter of the system for the aligned position was obtained as shown in Table 1.

Fig. 5. (Color online) Aligned (a) and unaligned (b) Maxwell 3D Models of receiver and transmitter.

Table 3. Efficiency of WPT system established in aligned and unaligned positions for different air gaps.

Aligned		Efficiency (%)						
Air Gap	1 cm	5 cm	10 cm	15 cm	20 cm	30 cm	40 cm	50 cm
MATLAB	91.75	91.75	91.75	91.75	87.15	37.29	12.21	3.63
PSIM	90.94	91.93	91.93	91.80	89.80	72.01	43.22	17.77
Maxwell 3D	66.89	67.79	65.29	71.30	62.76	21.07	7.38	1.42
Unaligned		Efficiency (%)						
Air Gap	1 cm	5 cm	10 cm	15 cm	20 cm	30 cm	40 cm	50 cm
MATLAB	91.75	91.75	91.66	77.88	51.21	19.13	7.00	2.45
PSIM	91.90	91.90	91.71	87.3	79.23	55.07	29.91	12.71
Maxwell 3D	65.49	69.67	66.05	53.45	33.44	11.87	4.19	1.42

For the unaligned position, each parameter of the system was obtained as shown in Table 2.

In the circuit simulation, the WPT system was fed from a sinusoidal voltage source, the peak voltage of which was 100 V. The model illustrated in Fig. 3 was completed in PSIM circuit simulation software.

The same circuit was modeled as shown in Fig. 4 with the Maxwell Circuit Editor (MCE) program. The circuits of the receiver and transmitter coils were modeled with

Fig. 6. (Color online) Graphs of efficiency for aligned and unaligned positions varying by different air gaps.

the MCE program, while the receiver and transmitter coils were modeled with the Maxwell 3D program, as shown in Fig. 5(a) and Fig. 5(b).

The efficiency of the WPT system that works with magnetic resonant coupling, established in aligned and unaligned positions for different air gaps, is shown in 3 separate programs in Table 3. In addition, the change of the efficiency with respect to the air gap is illustrated in Fig. 6.

The distributions of the magnetic flux are modeled with Maxwell 3D, as shown in Fig. 7. For each air gap value and positional aligned and unaligned condition, the input and output flow of the system, the peak voltage to which the capacities of receiving and transmitting resonance are exposed, the input and output voltage, and the input and output power are shown in Table 4.

3.2. Comparison of Aligned and Unaligned Positions

This section discusses the efficiency rates for angularly aligned positions and for positions which are not aligned according to different angles. Here, an air gap of 10 cm was chosen. This is because the receiver and the transmitter intertwine when the angles of alignment in the system are changed in air gaps narrower than 10 cm. In the system, L is a parameter that is not linear and varies according to the current of the system. Each parameter of the system for angularly aligned and unaligned positions

Table 4. Input and output current, voltage and power of the WPT system obtained in aligned and unaligned positions for different air gaps.

Maxwell 3D		Aligned Results						
Air Gap	1 cm	5 cm	10 cm	15 cm	20 cm	30 cm	40 cm	50 cm
Transmitter Current (A)	8.89	10.15	10.69	8.90	18.05	40.19	45.99	48.34
Receiver Current (A)	8.48	9.87	9.75	9.43	12.63	10.97	6.87	3.45
Input Voltage (V)	70.71	70.71	70.71	70.71	70.71	70.71	70.71	70.71
Output Voltage (V)	42.42	49.35	48.75	47.14	63.14	54.83	34.35	17.24
Input Power (W)	1158	1430.5	1461	1246.9	2549	5707	6503	6835
Output Power (W)	720	974	953.6	889	1595	1203	480	121
Transmitter Capacitor Peak (V)	1357	1411	1397	1150	2283	5071	5867	6153
Receiver Capacitor Peak (V)	1346	1383	1307	1239	1604	1387	892	447
Maxwell 3D		Unaligned Results						
Air Gap	1 cm	5 cm	10 cm	15 cm	20 cm	30 cm	40 cm	50 cm
Transmitter Current (A)	12.08	10.56	13.81	24.26	34.54	44.34	47.59	48.53
Receiver Current (A)	10.52	10.17	11.3A	13.52	12.72	8.65	5.33	3.12
Input Voltage (V)	70.71	70.71	70.71	70.71	70.71	70.71	70.71	70.71
Output Voltage (V)	52.59	50.86	56.51	67.62	63.62	43.26	26.65	15.62
Input Power (V)	1689	1485	1934	3422	4885	6304	6772	6861
Output Power (W)	1106	1035	1277	1829	1634	748	284	97
Transmitter Capacitor Peak (V)	1619	1368	1733	3053	4423	5606	6006	6172
Receiver Capacitor Peak (V)	1428	1330	1435	1709	1646	1095	673	397

Fig. 7. (Color online) Distributions of the magnetic flux density both aligned and unaligned positions.

Table 5. System parameters obtained by Maxwell 3D software in the different angle positions.

Parameter/Angle	0°	10°	20°	30°
L [nH]	983.8	1023.2	1000.3	984.5
L_m [nH]	128.3	6.8	2.7	1.5
C [pF]	124	124	124	124

Table 6. Efficiency rates of the WPT system for angularly aligned and unaligned positions.

10 cm Air Gap	Efficiency (%)			
Angle	0°	10°	20°	30°
MATLAB solved equations results	91.75	23.07	4.66	0.756
PSIM results	91.93	23.07	4.64	1.5153
Maxwell 3D results	65.29	0.0144	0.0026	0.0007

Fig. 8. (Color online) Receiving and transmitting positions of Maxwell 3D: which is Aligned (a), 10° Unaligned (b), 20° Unaligned (b) and 30° Unaligned (d).

was calculated as shown in Table 5.

In the circuit simulation, the WPT system was directly fed with a sinusoidal voltage source, the peak voltage was 100 V, as shown in Fig. 3. The model study illustrated in Fig. 3 was completed by PSIM circuit simulation software.

The same circuit was modeled as shown in Fig. 4 in the

Fig. 9. (Color online) Efficiency for various angles.

MCE program. The receiver and transmitter coils were modeled in the Maxwell 3D program as shown in Fig. 8, and the circuits of the receiver and transmitter coils were modeled in the MCE program.

The efficiency rates of the WPT systems that work with magnetic resonant coupling are shown in 3 different programs in Table 6. The change of efficiency with respect to the angle is also illustrated in Fig. 9.

Fig. 10. (Color online) Distribution of magnetic flux density: Aligned (a), 10° Unaligned (b), 20° Unaligned (c) and 30° Unaligned (d).

Table 7. Input and output current, voltage and power values obtained in aligned and unaligned positions for different angles for 10 cm air gap in Maxwell 3D.

Angle	0°	10°	20°	30°
Transmitter Current (A)	10.69	48.96	49.24	49.44
Receiver Current (A)	9.75	0.33	0.19	0.1
Input Voltage (V)	70.71	70.71	70.71	70.71
Output Voltage (V)	48.75	1.63	0.935	0.525
Input Power (W)	1461	6924	6964	7040
Output Power (W)	953.6	1	0.18	0.05
Transmitter Capacitor Peak (V)	1397	6268	6233	6294
Receiver Capacitor Peak (V)	1307	41.9	16.8	9.3

Distributions of the magnetic flux with respect to different angles of alignment are modeled with Maxwell 3D, as shown in Fig. 10.

With Maxwell 3D software, the input and output currents of the system, the peak voltage to which the capacities of the receiving and transmitting resonance are exposed, the

input and output voltages, and the angularly aligned and unaligned positions are illustrated in Table 7.

Corresponding to some of the definite geometrical dimensions of the WPT system, the efficiency and power values are very close to zero, when the alignment angle increases. This should be avoided in the design of the system. Indeed, according to the software used, the efficiency rates vary. While the difference is almost negligible for MATLAB and PSIM, which enables numerical analysis, the Maxwell 3D software results are considerably disparate owing to the analytic solver ground.

When the alignment angle is small, the distribution of magnetic flux density is roughly uniform and the power ratio is reasonable; as the angle is increased, the efficiency decreases due to the scattered magnetic flux density.

4. Conclusion

This study shows the limits of positional and angular

aligned and unaligned conditions for the WPT system which works with magnetic resonant coupling. In the design, it was observed that, for aligned positions, power could be transferred with high efficiency within air gaps of 15-20 cm and that efficiency quickly decreased within air gaps of more than 20 cm. For the spatially unaligned positions, it was observed that WPT could be realized with high efficiency with air gaps of up to 10 cm and that the efficiency quickly decreased with air gaps of more than 10 cm. Angularly aligned and unaligned positions were also examined in this study. Because the mutual inductance and efficiency diminished excessively, the significance of wireless energy transfer in the aligned positions could be observed. However, it was also demonstrated that WPT could also be realized in high efficiency in unaligned positions up to specific values of air gap. Again, when the simulation results were examined, it could be seen that in MATLAB (where the analytical solution was calculated) and in PSIM circuit simulation (where the numerical solution was calculated) the efficiency was greater than the results in Maxwell 3D. This was because the skin effect and the proximity effect in the receiver and transmitter coils of the WPT system were ignored in the results of MATLAB and PSIM. In the Maxwell 3D software, however, these effects were taken into consideration. Because a cable with a single wire was used instead of a multiple conductor cable, the skin effect and the proximity effect considerably reduced the efficiency. For future studies, the significance placed on this subject will become more of an issue in the design of

WPT systems with the use of multiple wire cables.

In this study, the detection of the system's resonance frequency for each air gap was between 13-14 MHz. In order to investigate higher air gaps, a design with a higher resonance frequency needs to be proposed.

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